# Firm Productivity and Learning with Digital Technologies: Evidence from Cloud Computing\*

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#### **Abstract**

We study firm productivity and learning in cloud computing by leveraging CPU utilization data from over one billion virtual machines used by nearly 100,000 firms. We find large and persistent dispersion in firms' productivity with cloud computing, similar to canonical results in the literature. More productive firms respond better to demand fluctuations, show higher attentiveness to resource utilization, and use a wider variety of specialized machines. New adopters learn to be more productive with the cloud over time, improving 33.0% in their first year, but it takes four years for them to reach a steady state, slower than many previously studied settings. Our results indicate substantial aggregate implications of inefficiencies in computing: improving firm productivity reduces the use of computing resources by up to 35% and electricity by up to 28%.

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#### 1 Introduction

The evolution of firm productivity has long been a central focus in economic research, with an extensive literature documenting its dispersion, persistence, and underlying mechanisms (Syverson, 2004a,b; Foster et al., 2008). An important driver of productivity is technological progress, which often leads firms to adopt new production processes. A recent example is the digital revolution, which has transformed firm production across all sectors as firms increasingly rely on computation and data (Brynjolfsson and McElheran, 2016; Goldfarb and Tucker, 2019; McElheran et al., 2023; Kalyani et al., 2025).

While a substantial literature documents the impact of digitization and IT on overall firm outcomes such as productivity, revenue, and output (Brynjolfsson and Hitt, 2003; Bartel et al., 2007; Bloom et al., 2012), there is less micro-level evidence on how efficiently firms use these technologies. A key reason for this gap is the lack of large-scale, granular data tracking the way in which firms use digital technologies. Most production datasets allow researchers to estimate total factor productivity (TFP), which, as a residual measure, captures various unobserved factors affecting productivity rather than measuring a specific aspect of production (Syverson, 2011). This underscores the importance of developing complementary measures that directly capture how firms use new technologies.

In this paper, we study firm productivity and learning with new technologies in the context of cloud computing. Our analysis draws on high-frequency utilization data from over one billion virtual machines (VMs) used by nearly 100,000 firms across various industries and countries. Using this dataset, we develop a measure of productivity that quantifies the extent to which firms could produce the same computing output with fewer computing inputs. We call this measure *compute productivity*. With this measure, we analyze productivity dispersion in computing both across and within firms, as well as the process by which firms learn to use computing more productively.

We begin our paper by providing background information on cloud computing. Cloud computing allows firms to have on-demand access to IT resources over the Internet. Instead of making periodic capital investments in their servers, firms rent IT resources from cloud providers, which shifts IT from a fixed cost to a variable cost. Cloud computing is one of the most widely adopted technologies in recent times, with nearly 80% of US firms using the cloud in some form (Zolas et al., 2021; Kalyani et al., 2025). As such, it represents a substantial and growing share of firms' costs across sectors (Demirer et al., 2024).

In cloud computing, VMs serve as the primary unit of production, corresponding to partitions of a physical server temporarily used by firms to run their IT operations. A key feature of VM deployment is that firms can dynamically adjust compute resources within

seconds in response to changing demand. This flexibility eliminates the need to provision resources in advance and maintain excess capacity. For a given VM, firms pay a fixed rate per unit of time the VM is allocated to them regardless of its use case or utilization.

As a transformative technology reshaping how firms use IT, cloud computing requires firm adaptation for efficient use. Such adaptations include complementary organizational investments to accommodate the new cost structure and develop monitoring mechanisms (Bresnahan and Trajtenberg, 1995; Bresnahan et al., 2002), as well as skill development specific to cloud technology (Griliches, 1969; Bartel et al., 2007). Existing evidence highlights the difficulty of these adjustments and their value to firms: industry studies find persistent compute underutilization on the cloud (Cortez et al., 2017; Flexera, 2023), which has fueled a multi-billion dollar consulting industry helping firms adopt efficient practices.

With these characteristics, cloud computing provides an ideal setting for studying firm productivity, both in the context of new technologies and more broadly. First, despite its widespread use, its variable input nature and global uniformity minimize the role of dynamic frictions and other external factors that typically complicate large-scale productivity analysis (Syverson, 2011; Asker et al., 2014). Second, our data enable productivity estimation at the machine level, offering insights into the mechanisms driving productivity dispersion and learning. Third, we can estimate productivity for individual divisions within firms, improving our understanding of within-firm heterogeneity. Finally, we can quantify wasted economic resources such as computing hardware and electricity due to inefficiencies, as our productivity measure is quantity-based and attributable to a specific aspect of production.

To implement the empirical analysis, we construct our firm-level compute productivity measure using VM utilization data collected at 5-minute intervals. In the context of production theory, this measure quantifies a firm's compute resource usage relative to that of a cost-minimizing firm with the same compute output and choice set of VMs. At a high level, our measure tracks how efficiently firms use computing resources, analogous to other factor productivity measures such as labor productivity (Baily et al., 2001; Demirer, 2022). Following industry practice, we define our measure using CPU utilization patterns, which measure the share of a VM's compute capacity actually used by the firm over time.

Our compute productivity measure incorporates two sources of inefficient compute usage: idle and overprovisioned VMs. We define a VM as *idle* if the firm never uses it and *overprovisioned* if its peak compute load would fit within the capacity of a smaller but readily substitutable VM. The underlying idea is that firms could eliminate idle VMs or downsize overprovisioned ones without impacting their compute output, thus saving resources and money. Importantly, these concepts are defined using peak utilization over

a seven-day period, ensuring that low average utilization due to volatile demand is not interpreted as inefficiency. By aggregating both sources of VM-level inefficiency, we obtain monthly firm- and division-level compute productivity estimates.

Using this measure, we first document new empirical facts about productivity in computing. We find significant dispersion in compute productivity across firms that is persistent in short-term (1-month) and long-term (5-year) horizons. Controlling for industry, firms at the 90th percentile of the distribution are 3.5 times more productive at using compute than those at the 10th percentile. Substantial productivity dispersion also exists within firms: 55.7% of the variation in compute productivity is explained by within-firm heterogeneity. The levels of dispersion and persistence in compute productivity are comparable to findings in the literature (Syverson, 2011; Cunningham et al., 2023) and are not simply explained by observables such as industry, firm size, and VM characteristics.

We next ask what makes firms more productive in computing. Although the scale of our study prevents us from observing managerial practices, we analyze differences in VM deployment patterns that reflect heterogeneity in firm behavior. Three patterns differentiate high- from low-productivity firms. First, high-productivity (above-median) firms adjust better to demand fluctuations: they reduce their provisioned compute resources by 75.2% more than low-productivity firms on weekends, during which compute demand declines substantially. Second, they have better monitoring capabilities: when resources remain idle, they are more than twice as likely to detect and shut down idle VMs as low-productivity firms. Finally, they demonstrate greater expertise in VM selection: they use a greater variety of VMs and are less likely to put all of their jobs on a single VM type.

We then shift our focus to productivity dynamics, investigating whether firms improve their compute productivity as they gain experience with the cloud. We analyze the productivity trajectories of firms over time, considering both short- and long-term learning.

We find that new cloud adopters improve their compute productivity substantially over time. Firms with one year of experience are 32.6% more productive than they were initially on average. The rate of improvement slows after the initial year, with firms exhibiting 44.0% higher compute productivity by the end of their fourth year and making no improvements thereafter. The extended time to reach steady-state productivity is longer than previous estimates from learning-by-doing studies (Benkard, 2000; Levitt et al., 2013), which could reflect the need for complementary investments and practices, as is widely documented in the literature (Bresnahan et al., 2002; Bloom et al., 2012).

Our analysis also reveals that learning significantly influences productivity dispersion. As firms gain experience, the 90–10th percentile productivity ratio declines from 7.2 in their first year to 2.7 after six years. This trend is driven by differences in learning rates:

firms that are initially less productive learn much faster than their more productive counterparts (but still do not catch up). Moreover, heterogeneity in the timing of adoption, through the presence of both more and less experienced firms at a given point in time, also increases cross-sectional productivity dispersion. Overall, these findings underscore that the maturity of production technology is a crucial determinant of the level and dynamics of productivity dispersion.

Next, we explore the mechanisms behind *how* firms learn. We decompose firms' compute productivity growth into (i) within-division learning, (ii) across-division reallocation, and (iii) division entry and exit (Foster et al., 2001). We find that firm-level learning is driven primarily by division-level learning, rather than by reallocation across divisions. At any level of firm experience, new divisions start with lower productivity than the firm as a whole, gradually improve their productivity over time, and are more likely to exit the cloud if their productivity remains below the firm's productivity. This pattern highlights the limited role of within-firm knowledge transfer—even in experienced firms with existing high-productivity divisions, new divisions begin at a lower level of productivity and improve over time.

When examining how divisions improve their productivity, we observe that learning is partly driven by experimentation. Divisions try many new VM types with which they are on average less productive than with their current VMs, but discard the ones they are unproductive with and become more productive with the ones they retain. In addition, experienced divisions achieve higher initial productivity with new VM types compared to new divisions, suggesting that divisions partially transfer knowledge across VM types.

Our final analysis quantifies the aggregate impact of inefficient compute use on economic resources, capturing both private costs to firms (compute resources) as well as social costs (electricity). We find substantial aggregate resource savings resulting from counterfactual productivity improvements. Raising all firms' productivity to the 80th percentile reduces compute resource use by 21.0% and electricity use by 16.5%, which reach further to 35.4% and 28.3% if all firms attain the highest possible productivity.

We take several steps to ensure our method accurately captures compute productivity while minimizing potential confounding factors. First, we intentionally adopt a conservative approach by considering peak CPU utilization measured over a seven-day period. Focusing on peak utilization accounts for many factors that may lower overall utilization without indicating true inefficiency, such as fluctuating demand. Second, we show that

<sup>&</sup>lt;sup>1</sup>An input to this analysis is the relationship between a VM's utilization and its electricity consumption, which we estimate using a separate dataset. We find that idle VMs consume electricity at around 50% of the rate of full-load consumption, with consumption increasing linearly as utilization rises.

our results remain similar when controlling for a rich set of VM characteristics and firmlevel observables, suggesting that compute productivity is not mechanically explained by observable factors. Third, we extensively review industry literature to demonstrate that our measure closely aligns with how firms measure inefficiency in practice. Fourth, we estimate compute productivity using publicly available utilization data from various cloud providers and find similar dispersion levels. Fifth, we analyze other utilization metrics in computing (memory and networking) and find similar results.

We nevertheless acknowledge some limitations of our study. Our approach does not capture all forms of compute inefficiency, such as inefficiently written code or inefficiently run data centers. While important, such inefficiencies are fundamentally different from the one we study, as they pertain to changing the production process rather than resource deployment. Moreover, our dataset is limited to compute inputs and does not include other firm inputs or outputs. We believe this is a worthwhile tradeoff given the extensive research on IT's impact on various firm-level measures (e.g., profit, revenue, employment), while micro-analysis of IT usage remains scarce.

Contribution to the Literature. First and foremost, this paper contributes to the large literature on firm productivity (e.g., Syverson, 2004a,b; Bloom and Van Reenen, 2007; Hsieh and Klenow, 2009; Syverson, 2011).<sup>2</sup> This literature has documented large dispersion in firm productivity and analyzed factors driving this dispersion. Our paper extends this literature by studying firm productivity in computing, an input of increasing importance for modern firms. We document several empirical facts about compute productivity that parallel findings in the literature, quantify the link between productivity and resource usage, and analyze productivity dynamics at a relatively granular level.

Our paper also contributes to the literature studying the effect of IT on firm outcomes (Brynjolfsson and Hitt, 1995, 1996, 2000, 2003; Black and Lynch, 2001; Bartel et al., 2007; Bloom et al., 2012; Tambe and Hitt, 2012; Brynjolfsson and McElheran, 2016; Brynjolfsson et al., 2023).<sup>3</sup> While this literature emphasizes the heterogeneous impact of IT across firms and the need for complementary investments to use IT effectively (Bresnahan et al., 2002), our paper directly measures how efficiently firms use a transformative digital technology at a large scale. As such, we provide detailed evidence on firms' use of an IT technology

<sup>&</sup>lt;sup>2</sup>While many papers in this literature use plant-level TFP of manufacturing firms as their primary productivity measure, several define productivity measures based on efficient utilization of inputs, as we do (Hubbard, 2003; Braguinsky et al., 2015; Butters, 2020).

<sup>&</sup>lt;sup>3</sup>Other contributions to this literature include case studies that investigate the mechanisms through which IT affects firm outcomes (Baker and Hubbard, 2004; Miller and Tucker, 2011), studies focusing on the decline in IT prices and their impact on firms' production technology (Lashkari et al., 2024), macro-level studies (Jorgenson, 2001; Stiroh, 2002), and those studying the slow impact of IT on aggregate statistics (Basu et al., 2004; Brynjolfsson et al., 2021).

and complement the canonical findings in this literature.

By studying firm learning in cloud computing, our paper contributes to the empirical literature on learning-by-doing (Darr et al., 1995; Benkard, 2000; Thornton and Thompson, 2001; Kellogg, 2011; Levitt et al., 2013; Hendel and Spiegel, 2014; Tadelis et al., 2023). Much of this literature analyzes a single firm or a small number of firms within narrowly defined industries, showing that productivity improves with firm experience. Our study instead focuses on learning in the context of a widely adopted and rapidly evolving technology, thus linking the learning-by-doing literature to the literature on general-purpose technologies (Bresnahan and Trajtenberg, 1995; Helpman and Trajtenberg, 1998). We find a longer learning period than much of the existing literature, which we attribute to cloud technology requiring organizational investments to be utilized efficiently.

Finally, we contribute to the growing literature on the economics of cloud computing by analyzing productivity and learning in the cloud (Byrne et al., 2018; Greenstein and Fang, 2020; DeStefano et al., 2023; Jin et al., 2023; Demirer et al., 2024; Lu et al., 2024; Jin and McElheran, 2024).

# 2 The Role of Computing in Firm Production

This section provides an overview of how firms use computing in production, with particular emphasis on cloud computing. Additional details are provided in Appendix A.

# 2.1 Background on Computing

Computing is an essential input to firm production across all industries. At a fundamental level, computing enables firms to process data and perform tasks that require calculations using a combination of hardware and software.

Firms' use of computing falls into three broad categories: production, development, and administrative tasks. In production, which represents the majority of the usage (Cortez et al., 2017), computing directly enables digital services such as streaming, mobile applications, and websites (Greenstein, 2020) while serving as a complementary input for non-digital services through functions like payment processing, customer relationship management, and data analytics (Zolas et al., 2021). Examples of compute use for development include product simulations in software and computer-aided design in manufacturing (Leigh et al., 2020). Finally, computing supports a range of administrative operations, including HR, finance, sales, and internal communications (Davenport, 1998).

<sup>&</sup>lt;sup>4</sup>While there are multiple definitions of general-purpose technology in the literature, one basic characterization is that it is (i) widely used, (ii) capable of ongoing technical improvement, and (iii) enables innovation in application sectors (Bresnahan, 2010). Cloud computing clearly satisfies these conditions.

Figure 1: Sample of VM Choices on Amazon Web Services

Instance name	On-Demand hourly  rate   ▽	vCPU ▽	Memory ▽	Storage ▽	Network performance	▽
t4g.nano	\$0.0042	2	0.5 GiB	EBS Only	Up to 5 Gigabit	
t4g.micro	\$0.0084	2	1 GiB	EBS Only	Up to 5 Gigabit	
t4g.small	\$0.0168	2	2 GiB	EBS Only	Up to 5 Gigabit	
t4g.medium	\$0.0336	2	4 GiB	EBS Only	Up to 5 Gigabit	
t4g.large	\$0.0672	2	8 GiB	EBS Only	Up to 5 Gigabit	
t4g.xlarge	\$0.1344	4	16 GiB	EBS Only	Up to 5 Gigabit	

*Notes*: This figure displays a selection of VM options from a specific Amazon Web Services machine series and details the configuration of each VM.

## 2.2 Background on Cloud Computing and Virtual Machines

Traditionally, computing was performed on servers purchased and maintained by individual firms, known as "on-prem" computing. More recently, advancements in server and networking technology have given rise to cloud computing, which allows firms to access IT resources remotely over the Internet. In this model, the physical resources are owned and maintained by cloud providers, and firms have on-demand access to these resources via a rental market. Cloud computing has become widely adopted, with nearly 80% of firms using the cloud for at least one IT function (Zolas et al., 2021; Kalyani et al., 2025).<sup>5</sup>

While a wide range of products are available in cloud computing, virtual machines (VMs) are the primary cloud computing resource used by firms. Cloud providers separate their physical servers into distinct partitions, each running its own isolated operating system. A VM is one such partition, allocated to a firm upon request and remaining active until the firm terminates it. In this way, VMs serve as a modern alternative to on-prem IT, offering similar levels of control with the added benefits of scalability and minimal infrastructure costs (Jin and McElheran, 2024).

Cloud providers offer a vast array of VM options, even within a single VM series, as illustrated in Figure 1. Each VM comes with a configuration specifying memory, storage, networking capabilities, and cores (CPU). Within a VM series, computing capacity is determined by the number of cores—independent processing units that execute tasks simultaneously. Multiplying the number of cores by the duration of the VM gives *core*-

<sup>&</sup>lt;sup>5</sup>According to Gartner, enterprise spending on cloud computing was 41% of IT spending in 2022 and was expected to increase to 51% in 2025. Gartner—Cloud Usage.

<sup>&</sup>lt;sup>6</sup>VMs fall under the category of Infrastructure as a Service (IaaS) products. Cloud providers also offer less customizable products that fall under Platform as a Service (PaaS), such as "serverless computing" and "containers." These products typically have narrower adoption, as they require specialized knowledge and are suitable only for some applications. Appendix A.1 provides an overview of these PaaS cloud products.

*hours*, the unit of compute resource we use throughout the paper.

Firms typically use tens or even hundreds of VMs simultaneously for their IT operations. When choosing VMs, firms must evaluate factors such as price, memory, and storage against their needs. The pricing of VMs depends on attributes including the hardware model, operating system, and geographic region the VM is hosted (Hummel and Schwarz, 2022). However, for a given VM, firms are usually charged a fixed rate per unit of time the VM is allocated to them regardless of the use case or actual utilization.<sup>7</sup> Once requested, VMs are typically deployed within seconds (Nguyen and Lebre, 2017; Tirmazi et al., 2020).<sup>8</sup>

A key advantage of cloud computing is that firms can automatically deploy VMs without direct human intervention. This feature, known as autoscaling, allows firms to specify rules to adjust compute resources based on demand fluctuations. For example, an online retailer can schedule additional VM deployment every Monday morning when its traffic peaks, whereas if demand is unpredictable, firms can set rules to add more VMs when the average utilization of existing VMs exceeds a certain threshold. This feature eliminates the need to maintain excess capacity to meet peak demand. All major cloud providers offer autoscaling with no additional fees on their platforms (Fazli et al., 2018).

## 2.3 The Economics of Cloud versus On-Prem Computing

The advent of cloud computing has dramatically transformed the economics of IT (Etro, 2015). In the traditional on-prem IT paradigm, computing resources are capital expenditures: firms make periodic investments under uncertainty in servers that depreciate over time (Pindyck, 1986). This creates a classical peak-load problem where firms must invest in enough fixed capacity to handle peak demand, leading to underutilization during off-peak periods (Carlton, 1977). As a result, firms face a tradeoff between the costs of maintaining excess capacity and the risks of having insufficient capacity to meet demand.

Cloud computing flips this paradigm by shifting computing from a capital expenditure to a variable cost. Firms no longer need to worry about capacity investment or resource constraints, as capacity is always available on demand. <sup>10</sup> This allows firms to accommodate

<sup>&</sup>lt;sup>7</sup>Cloud providers offer discounts to firms that commit to using their services for a specified duration, typically one or three years. These are known as "reserved instance" or "committed use" discounts and are applied to list prices uniformly across customers except for very large ones. For more details, see Appendix A.1.

<sup>&</sup>lt;sup>8</sup>We provide more details on VMs and VM deployment in Appendix A.2. For technically-oriented readers, Appendix A.3 describes VM use for two real-world applications in web development and machine learning. 
<sup>9</sup>In addition, cloud providers offer predictive autoscaling algorithms to spin up additional capacity in advance of, rather than in response to, demand spikes. All the major cloud platforms offer predictive autoscaling; see AWS; Azure; Google Cloud. Another important tool enabling automatic scaling is the load balancer, which allocates incoming traffic across multiple VMs. See Figure OA-8 for an illustration of a load balancer.

allocates incoming traffic across multiple VMs. See Figure OA-8 for an illustration of a load balancer. <sup>10</sup>In practice, firms initially request a quota, and the capacity is available up to this quota. Except for a few specialized types of VMs, firms can choose a quota that is high enough to meet their peak computing needs. Cloud providers balance supply and demand by offering spot VMs, which are available at a discount but can

sudden spikes in traffic, handle increased workloads during peak periods, and scale down resources when no longer needed, all without maintaining physical capital.

In summary, linear pricing, near-instant scalability, and minimal transaction costs make cloud computing a variable input with negligible adjustment costs and dynamic frictions (Asker et al., 2014). Moreover, all firms have access to the same technology and pricing model regardless of their location or industry. These features make the cloud an ideal setting for studying how firms integrate and use new technologies, as we can abstract away from many of the frictions associated with dynamic inputs and rule out external factors that directly affect productivity (Syverson, 2011; Restuccia and Rogerson, 2017).

## **Determinants of Productivity in Cloud Computing**

While cloud computing offers numerous advantages, it also introduces challenges that firms must address for efficient use. Academic literature and industry sources highlight two main challenges: the need for complementary organizational investments and the development of skills specific to cloud technology.

First, cloud computing can exacerbate latent monitoring problems within organizations. Unlike on-prem computing, cloud computing has a positive marginal cost, making monitoring of compute usage far more important. Engineers who manage VMs may not naturally have an incentive to be cost-conscious, creating principal-agent problems for the firm (Holmström, 1979; Grossman and Hart, 1992). Organizational inertia can make it hard to address these problems, as transitioning to the cloud requires new management practices and complementary investments, referred to as "digital capital" by Tambe et al. (2020), that may be difficult or take time to implement (Bresnahan et al., 2002; Garicano, 2010; Bloom et al., 2012). 11 For example, 81% of respondents in an industry survey report that "their development teams are embracing the cloud . . . faster than the rest of the organization can adopt and manage them" (Couchbase, 2022). Another example is "shadow IT," the widespread practice where different units of the firm use IT resources without the oversight or knowledge of the IT department (Haag and Eckhardt, 2017).

Second, like many other technologies, cloud computing requires new skills (Griliches, 1969; Caselli and Coleman, 2001; Bartel et al., 2007). Chief among these is choosing the right VM and effectively using various tools available in the cloud, both of which require employee adaptation and learning. Indeed, one industry report states that finding the best match for a workload in a cloud provider's inventory is "easier said than done," with

be reclaimed by the provider at short notice. Spot VMs account for a small share of usage, and we exclude

them from our sample. For details, see CloudBank Project — Cloud Quotas and Appendix A.1. 

11 These challenges were also observed in the previous major shift in computing, the transition from mainframe to client/server architectures, as documented by Bresnahan et al. (1996).

many teams "simply choos[ing] instances they know and have used before," which tends to "underutiliz[e] other resources that they have paid for" (CAST AI, 2024).

The challenge of optimizing cloud usage has led to the development of a plethora of first-and third-party tools to help firms become more efficient. First, cloud platforms themselves offer firms various ways to view and manage their usage and costs, often proposing steps to eliminate underutilized VMs. We provide an overview of these tools in Appendix A.2. Second, a large and fast-growing cloud optimization consulting industry offers services to analyze firms' cloud usage and recommend ways to improve efficiency. These consultants engage more deeply with the firm and provide more tailored recommendations than first-party tools do. This market was estimated to be worth \$17.6 billion in 2022 and is projected to reach over \$80 billion by 2030.<sup>12</sup>

To sum up, it is important to make clear that while firms face obstacles to using the cloud optimally, these obstacles are not a feature of the technology itself. Instead, economic factors are the primary explanations for inefficiency on the cloud, as discussed above. These factors have long been understood as key drivers of productivity dispersion among firms using seemingly identical inputs (Leibenstein, 1966; Syverson, 2011). Moreover, the existence of the large and growing cloud consulting industry, combined with numerous surveys where firms themselves report that compute optimization is a priority, indicates both strong firm demand for productivity improvements and that such improvements are viewed as technologically feasible (Flexera, 2023). Finally, the potential savings from more efficient compute use are likely substantial for most firms, as IT represents a large and growing share of firms' costs across sectors.<sup>13</sup>

# 3 Data and Summary Statistics

This section introduces the datasets used in our analysis and presents summary statistics. <sup>14</sup> We provide a more detailed description of the data in Appendix B.

<sup>&</sup>lt;sup>12</sup>Yahoo Finance— Global Cloud Computing Report. For an example of the tools provided by one of the startups in this industry, see Figure OA-7. Several case studies document significant cost savings from implementing best practices; for example How 6 Companies Saved up to 80% on Cloud Costs – Case Studies. <sup>13</sup>For example, IT accounted for 11.8% and 5% of costs in the software and services industries in 2018, respectively—a share that is likely even higher during our sample period (Demirer et al., 2024).

<sup>&</sup>lt;sup>14</sup>Empirical studies of IT typically use data on firm-level IT investments or technology adoption. These include surveys conducted by market research firms such as the Computer Intelligence Intercorp and Harte-Hanks (Bresnahan et al., 2002; Bloom et al., 2012) or administrative datasets such as granular IT expenditures in France (Lashkari et al., 2024) and firm usage of advanced technologies in the US (Zolas et al., 2021). Although our dataset is less comprehensive, as we observe only one IT technology from a single provider, it provides more granular information, making it a useful complement to existing datasets.

#### 3.1 CPU Utilization Data

Our primary dataset includes CPU utilization information of over one billion VMs provided by a global cloud computing provider. <sup>15</sup> CPU utilization measures the percentage of a computer's processing capacity currently in use relative to its maximum capacity and is a critical metric for evaluating computing efficiency (Mason et al., 2018). CPU utilization is typically recorded at 5 or 10-minute intervals by computer systems. To make this raw data more manageable, we aggregate it to the VM-day level by recording the CDF of CPU utilization for each day the VM is active. We then impose sample restrictions to remove short-lived VMs as described in Appendix B.5.

The CPU utilization data cover nearly 100,000 firms intermittently between 2017 and 2023, with varying durations each year. In 2017, the dataset covers approximately 60 non-consecutive days, while in 2018 and 2019, it includes a 30-day period each year. Although no data are available for 2020 and 2021, we have 12 months of data from July 2022 to June 2023. While the intermittent nature of the data restricts some analyses, it still allows us to estimate both short-term and long-term productivity dynamics over a six-year period.

For each VM in our dataset, we observe its duration, the anonymized ID of the firm using the VM, and the anonymized unit ID for multi-unit firms. A "unit" in our data refers to a group of users who share a billing account with the cloud provider and an administrative structure overseeing the VMs. These units may correspond to product teams or functional divisions within the company, though no further information is available. As such, we will maintain the "unit" terminology in the rest of the paper.

We also observe various VM attributes, including an identifier that indicates the hardware manufacturer and model, operating system, memory, and number of cores. The data also include the region of the data center hosting the VM (EU, US, or other) and an anonymized data center ID. Using this information, we categorize VMs into *family* (broad categories of workloads the VM is optimized for, like compute- or memory-intensive), *series* (groupings based on performance or hardware), and *configuration* (the combination of memory, cores, operating system, VM series, and data center).<sup>16</sup>

#### 3.2 Firm and Unit Level Data

Although our CPU utilization data are an unbalanced panel, we have a balanced panel with the monthly cloud usage of all of the firms and units in our sample. These data

<sup>&</sup>lt;sup>15</sup>The company stored these data for independent reasons and made them available to us for research. The dataset is sampled to reduce its size, remove firms with very low cloud usage, and minimize the inclusion of confidential information. See Appendix B.4 for details on the sampling procedure. Due to the sensitivity of our data, we do not report exact numbers of observations or levels of certain variables throughout the paper. <sup>16</sup>Appendix B.2 contains more details on each of these categories.

cover the period from 2017 to mid-2023 and include each firm's and unit's normalized total computation in each month. With this information, we can track firms' entry/exit into or out of the cloud and changes in compute usage over time.<sup>17</sup> In addition, we observe the firm and unit region (EU, US, or other), whether the firm is multinational, industry (2-digit SIC), and quartiles of a firm size measure.<sup>18</sup>

## 3.3 Publicly Available Cloud Data

We supplement our main dataset with publicly available CPU utilization data from Google Cloud and Microsoft Azure. These datasets provide additional information not present in our main data and allow us to validate our findings in other cloud computing environments. One such dataset is the 2019 Power Traces from Google Cloud, which records electricity consumption and CPU utilization of VMs at 5-minute intervals within a data center. Using this dataset, we estimate the relationship between CPU utilization and electricity consumption to quantify potential electricity savings from productivity improvements.

## 3.4 Summary Statistics

Table 1 presents summary statistics as observed in 2020, the midpoint of our sample. Panel A shows industry categories based on 1-digit SIC codes, highlighting the predominant sectors such as services and software, which account for 36.2% and 23.2% of firms, respectively. Although smaller in share, our sample also includes more traditional industries such as manufacturing and transportation. Column (2) reports that the share of firms with multiple units that use the cloud ranges from 26.7% to 48.3% across industries, indicating that we can observe compute productivity at the unit level in many firms. Column (3) shows that firms' average cloud experience is only a few years, with little variation across industries.

Panel B reports the firm distribution by region, showing that 31.2% are located in the US, 21.4% in the EU, and 6.2% are classified as multinational. As expected, multinational firms are more likely to be multi-unit and have 0.7 years more experience than domestic firms on average. Lastly, Panel C presents summary statistics at the VM level. The average lifespan of a VM is 2.5 days, with a standard deviation of 13.7, indicating substantial heterogeneity in VM duration. Similarly, we observe considerable variation in the number of cores (mean = 7.9, s.d. = 12.0), which reflects the availability of VMs with different

<sup>&</sup>lt;sup>17</sup>We observe data from one cloud provider only, and therefore cannot tell if a firm used a different cloud provider beforehand. As such, our measure of cloud experience is a lower bound on firms' actual experience. <sup>18</sup>The 2-digit SIC industry classifications we observe are broader than the 3- or 4-digit classifications commonly used in the literature. Although this is a limitation of our dataset, it is likely less restrictive than in other settings because we study a productivity measure obtained from a uniform input that does not require production function estimation.

**Table 1:** Summary Statistics in Mid-Sample (2020)

	Share (%)	Multi-unit (%)	Average Cloud Experience (Years)	
	(1)	(2)	(3)	
	Pan	el A. Industry Categor	y (1-digit SIC)	
Services	36.20	26.72	1.97	
IT/Software	23.15	43.06	2.73	
Retail Trade	12.29	32.28	2.00	
Manufacturing	9.11	43.27	2.24	
Public Administration	7.48	47.20	2.52	
Transportation and Communications	6.10	44.11	2.38	
Finance, Insurance, and Real Estate	4.54	48.33	2.25	
Other	1.12	32.62	1.96	
	Panel B. Firm Region			
Other	41.12	29.54	1.90	
US	31.22	26.24	1.97	
EU	21.43	29.77	1.93	
Multinational	6.22	59.81	2.65	
		Panel C. VM Statistics		
	Mean	SD	Mode	
Duration (days)	2.52	13.75	1	
Number of cores	7.88	12.04	4	
Share downsizable	0.72	0.45	1	

*Notes*: Panels A and B report summary statistics for firm industry and region in our sample in June 2020, the midpoint of our sample. Industries are classified by 1-digit SIC codes, with the exception of software firms, which are carved out of the services industry. Column (1) reports the unweighted share of firms in each category. Column (2) reports the share of firms with multiple units in each category, and Column (3) reports the average number of years since the firm first used the cloud as of June 2020. Panel C provides unweighted summary statistics for VMs created during a week in 2022, including their duration, number of cores, and the share of downsizable VMs. The definition of downsizability is provided in Section 4.1.

capacities. Finally, 72% of the VMs are downsizable, as defined in Section 4.1, meaning that in most cases, firms can choose smaller-capacity substitute VMs if they overprovision.

# 4 Measurement of Productivity in Computing

This section describes our approach to measuring compute productivity. Our goal is to quantify how efficiently firms use computing to study firm productivity in the context of a new technology. As such, instead of focusing on the entire production function, we analyze a single input in minute detail, measuring firms' compute productivity at the machine level using high-frequency data. Nonetheless, in Appendix C.2, we demonstrate that our measure can be interpreted as compute-augmenting productivity in a full production function (Doraszelski and Jaumandreu, 2018; Demirer, 2022).

**Table 2:** Example of Cloud Usage for a Hypothetical Firm

VM	Capacity	Duration	Actual Input Use	Peak Util.	Peak Job Load	Efficient Usage	Efficient Input Use	Efficiency
	[a]	[b]	$[c] = [a] \times [b]$	[d]	$[e] = [a] \times [d]$		[f]	$[g] = [f] \div [c]$
A	2-core	10h	20 ch	0%	0 cores	Eliminate	0 ch	0%
В	4-core	5h	20 ch	25%	1 core	Downsize	10 ch	50%
C	8-core	10h	80 ch	75%	6 cores	Maintain	80 ch	100%
Total			120 ch				90 ch	75%

*Notes*: This table presents CPU utilization data for three different VMs used by a hypothetical firm. VM A, with a 2-core capacity and no utilization, suggests idleness (0% peak utilization). VM B, with a 4-core capacity used at 25% peak utilization, indicates overprovisioning. VM C shows the use of an 8-core capacity at 75% peak utilization, labeled as properly provisioned. The total CPU input across all VMs accumulates to 120 core-hours, whereas the efficient use is 90 core-hours, reflecting an overall efficiency of 75%.

In developing our measure, we ask the following question: how would a cost-minimizing firm that has the same compute needs and faces the same menu of VM choices as a given firm deploy compute resources in the cloud? The share of resources this cost-minimizing firm uses relative to the firm's actual usage defines compute productivity. <sup>19</sup> Importantly, this approach goes beyond simply using the utilization rate as an efficiency measure and instead considers the environment the firm faces when deploying compute resources.

In what follows, we first describe how we measure compute productivity. We then argue that our method aligns with industry practices and has first-order relevance to measuring productivity in computing. Finally, we discuss the strengths and weaknesses of our measure relative to TFP. Appendix C.1 provides a formal exposition of our measure, and Appendix D.1 presents additional implementation details omitted from the text.

# 4.1 Constructing Compute Productivity

To illustrate our measure, consider the usage pattern of a hypothetical firm documented in Table 2. Suppose there are three sizes of VMs available to the firm: 2-core, 4-core, and 8-core. The firm runs jobs on three VMs: VM A, a 2-core machine; VM B, a 4-core machine; and VM C, an 8-core machine. VMs A and C are active for 10 hours, and VM B lasts 5 hours. Therefore, the total computing resource the firm pays for—the firm's total input use—is  $2 \times 10 + 4 \times 5 + 8 \times 10 = 120$  core-hours.

Now suppose that we observe the following utilization patterns. The firm did not actually utilize VM A at all; the peak load for the job was 0 cores. While the firm did use VM B, it utilized at most 25% of the computing capacity at any given moment. Therefore,

<sup>&</sup>lt;sup>19</sup>Our cost minimization framework is distinct from yet similar to the traditional cost-minimization assumption in neoclassical production theory (Shephard, 1953). Instead of firms taking input prices as given and minimizing costs to produce an output level, in our framework, they take a menu of VMs as given and find the VM that minimizes the cost of producing a given compute output.

the peak load of the job was  $25\% \times 4 = 1$  core. Finally, on VM C, the peak utilization was 75%, meaning the peak load of the job was  $75\% \times 8 = 6$  cores. These peak loads define the number of cores that were needed to perform the observed workloads.<sup>20</sup>

What would a perfectly cost-minimizing firm have done if it had the same computing needs and faced the same set of available VMs? First, it would not provision VM A, which the firm did not use to compute anything. By doing so, the firm can avoid paying for 20 core-hours of compute. Second, given that the job run on VM B only requires a capacity of 1 core at peak, the firm would downsize it to a 2-core machine, reducing the input usage from 20 core-hours to 10 core-hours. Finally, since the job run on VM C requires a peak capacity of 6 cores, it cannot be downsized (the next smallest available machine is 4 cores); the cost-minimizing firm would provision the same 8-core machine and use the same 80 core-hours of input. Overall, a cost-minimizing firm would have only used 90 core-hours, while this firm actually used 120 core-hours. As such, we conclude that this firm could have used 75% of the input it actually used to get the same output.

Our measure of compute productivity generalizes the logic of this example. We assign each VM j run by firm i on day t a productivity  $\omega_{ijt} \in [0, 1]$ , where, at a high level,

$$\omega_{ijt} = \frac{\text{Minimum number of cores needed for VM } j\text{'s job}}{\text{Actual cores used for VM } j}.$$

To determine the minimum number of cores needed for VM j's job, we use its peak utilization over a seven-day period.<sup>21</sup> Focusing on peak utilization accounts for many factors that may lower overall utilization without reflecting any actual inefficiency. For instance, our approach does not consider low average utilization due to fluctuating demand as inefficient, nor does it credit potential efficiency gains from turning a briefly idle VM off and on. We take peak utilization to be the 95th percentile of the CPU utilization distribution, following the recommendations made by cloud providers, as well as those in the computing literature (Reiss et al., 2012; Cortez et al., 2017).<sup>22</sup>

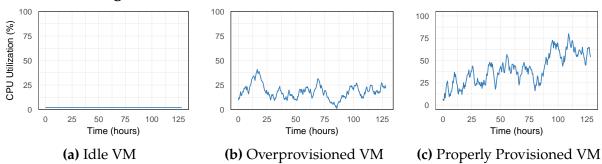
Our method identifies two distinct sources of inefficient VMs: idleness and overprovisioning. VM j is idle if its peak utilization is under 10%. This low level of utilization is explained by background CPU processes rather than any actual CPU usage by the user

<sup>&</sup>lt;sup>20</sup>If the job's peak load exceeds the CPU capacity of the VM, the job will take longer to complete as tasks are added to the processor's execution queue faster than they can be executed (Hennessy and Patterson, 2012). This is different from exceeding the memory capacity, which can lead the job to crash.

<sup>&</sup>lt;sup>21</sup>A job is defined as the total computation performed over the course of a VM's duration. For VMs shorter than seven days, we use the peak utilization over the life of the VM. Appendix D.1 provides more details as well as two examples from our data.

<sup>&</sup>lt;sup>22</sup>The 95th percentile is less sensitive to measurement errors or spikes stemming from random events like software updates than the maximum CPU utilization.

Figure 2: Illustration of Different CPU Utilization Patterns



*Notes*: This figure displays three different CPU utilization patterns. Panel (a) shows the CPU utilization of an idle VM, maintaining a utilization near 0% throughout its duration. Panel (b) shows an overprovisioned VM with a peak utilization of about 40%. Panel (c) shows a properly provisioned VM with peak utilization above 75%.

(Breitgand et al., 2014). Because an idle VM does not have any compute output, the minimum number of cores needed for its job is zero, hence  $\omega_{iit} = 0$ .

VM j is overprovisioned if its job would have reached a peak utilization of 90% or less on a VM that has fewer cores but is otherwise similar (and VM j is not idle). In this case, the minimum number of cores needed to run the job is that of the smallest such VM that fits the job's peak load. If such a smaller substitute exists—that is, if there exists a configuration with fewer cores but the same machine family, memory, data center, and operating system—we call the VM downsizable.<sup>23</sup> Typically, cores scale in powers of two, so an overprovisioned VM will often be resized to a VM with half the number of cores, in which case  $\omega_{ijt} = 0.5$ .<sup>24</sup> Finally, if a VM is neither idle nor overprovisioned, it is *properly provisioned*. In this case,  $\omega_{ijt} = 1$ .

Figure 2 is another illustration of our measure, with each panel displaying the CPU utilization of a VM over time. Panel (a) is an idle VM. While it was not utilized by the firm that provisioned it, this VM still consumes around 50% of the electricity of a fully utilized VM and is not typically allocated to another firm by the provider (Kansal et al., 2010).<sup>25</sup> Panel (b) is a potentially overprovisioned VM. Although the VM was continuously used, it

<sup>&</sup>lt;sup>23</sup>See Figure OA-5 for an illustration of downsizability. We focus on these characteristics because VMs that share them are readily substitutable. We discuss downsizability further in Appendix E.5 and show our results are robust to alternative definitions. Although networking is an attribute of a VM, we do not use it in our downsizability definition since it often does not change within a VM series (see Figure 1).

<sup>&</sup>lt;sup>24</sup>In addition, in some cases, it is possible to downsize to a quarter of the number of cores, i.e., if the peak utilization is 20% and a VM with one-fourth of the number of cores is available. In this case  $\omega_{ijt} = 0.25$ . Although we omit this category from the description for brevity, as it is rarely observed in the data, we include it in our productivity calculations.

<sup>&</sup>lt;sup>25</sup>See, for example, Azure, which states that it does not oversubscribe resources, and Google Cloud and AWS, which explicitly list a small number of products that are technically feasible to oversubscribe. Cloud providers have service-level agreements (SLAs) with their clients, committing to maintain availability with extremely high probability (e.g., 99.99%, commonly referred to as "four 9s"). Therefore, reallocating idle VMs could risk violating these SLAs and pose monetary and reputational risks (Perez-Salazar et al., 2022).

could have also fit on a substitute VM with half the number of cores, and would be marked as overprovisioned if such a VM exists. Finally, panel (c) is a properly provisioned VM with a peak utilization of 75%, which means the job would not fit on a smaller VM.<sup>26</sup>

After calculating VM-day-level productivity estimates, we aggregate them to construct a firm-level productivity measure as in the example in Table 2. The productivity of firm i in month m with VMs  $J_{im}$  is the core-hour weighted average of VM-day-level productivities:

$$\omega_{im} = \frac{\sum_{j \in J_{im}} \sum_{t} \omega_{ijt} c h_{ijt}}{\sum_{j \in J_{im}} \sum_{t} c h_{ijt}}$$
(1)

where  $ch_{ijt}$  is the core-hours of VM j on day t. This measure essentially quantifies (the inverse of) the share of resources wasted by the firm in month m. Using the same procedure, we also estimate unit-month and firm-VM type-month level productivity to analyze the productivity of units within a firm and firms' productivity with different VM types.

In addition, we estimate separate productivity measures for idleness and overprovisioning. Each measure is defined as one minus the share of idle or overprovisioned core hours, so that higher values indicate greater efficiency. These measures are useful because they likely capture the distinct sources of inefficiencies discussed in Section 2. Idleness can mainly be attributed to incentive and monitoring problems within the firm, whereas overprovisioning may also stem from insufficient skills in VM selection.

Finally, as described in Appendix D.1, we reestimate all our productivity measures using fixed-effect regressions that control for job- and time-specific factors—such as the VM type and day of the week—to isolate the impact of observables on productivity.<sup>27</sup> Although we use the estimates without controls from Equation (1) for our baseline results, as the choice of VM may itself reflect productivity, we report our main results with various controls in Appendix H.

# 4.2 Discussion and Limitations of Compute Productivity

To measure compute productivity, we used the hypothetical cost-minimizing firm that can match its compute resources to its needs as a benchmark.<sup>28</sup> However, our measure

<sup>&</sup>lt;sup>26</sup>In practice, our data are at the VM-day level. Therefore, we classify each VM-day based on the peak utilization over the seven-day periods it is a part of. For example, we mark a VM-day as idle if it is part of a seven-day period in which the peak utilization is under 10%.

<sup>&</sup>lt;sup>27</sup>The firm fixed effects estimates from these regressions without any controls correspond to our baseline measures in Equation (1). In these fixed effect regressions, we can only compare the fixed effects of firms within a connected set (Abowd et al., 1999; Metcalfe et al., 2023). We find that across these specifications, there is either one connected set or that the largest connected set covers more than 99% of the firms.

<sup>&</sup>lt;sup>28</sup>While we use the hypothetical cost-minimizing firm as a theoretical benchmark to measure productivity, our empirical analysis mainly focuses on firms' relative performance within the productivity distribution.

does not require an assumption that firms can perfectly predict their compute needs. As discussed in Section 2.4, firms can use tools to automatically adjust compute resources in response to demand changes, meaning that perfect demand forecasting is not needed to provision VMs efficiently in the cloud. Failing to take advantage of these tools should be viewed as an inefficiency in and of itself, which is captured by our measure.<sup>29</sup>

While our measure of compute productivity is novel to the economics literature, it aligns closely with industry practices and bears similarity to previously developed utilization-based efficiency measures in economics. First, cloud providers' definitions of compute efficiency are similar to our own; for example, Microsoft Azure's API generates a "resize" recommendation if the 95th percentile CPU utilization of a job would be under 80% on a less expensive VM, nearly identical to our overprovisioning definition.<sup>30</sup> Second, the cloud optimization consultants described in Section 2 also focus on idleness and overprovisioning; one such startup states that the "best practices for optimizing cloud costs" are to "identify underutilized resources, detect idle resources, [and] rightsize cloud resources," while another lists as the most common mistakes "picking oversize instances," "provisioning too many instances," "leaving instances running idle," and "forgetting to clean up stale resources." Finally, the idea behind our measure—that the extent to which firms utilize their inputs is a dimension of firms' productivity—has been used to study productivity in several other contexts in economics (Hubbard, 2003; Braguinsky et al., 2015; Butters, 2020, for example).<sup>32</sup>

Nevertheless, there are three caveats to note about our measure. First, it does not capture other kinds of computing inefficiencies like poorly written code that consumes excess compute, meaning some VMs we deem properly provisioned would actually be overprovisioned if the code were optimized. Our measure should therefore be viewed as productivity due to provisioning decisions, conditional on code efficiency and all other factors affecting CPU utilization. Second, our measure uses CPU utilization and does not capture other dimensions of VM utilization. We focus on CPU utilization because it is the standard metric in the industry and the main determinant of energy consumption (Rivoire

<sup>&</sup>lt;sup>29</sup>In specific scenarios, such as algorithmic high-frequency trading or online game launches, even a few-second latency impact may be costly, making reactive autoscaling alone insufficient. However, in such exceptional cases, focusing on peak utilization over a seven-day period may help address potential measurement issues due to demand volatility that is not fixable by autoscaling.

 <sup>&</sup>lt;sup>30</sup>Azure— How-to Guides. AWS and Google Cloud have their own similar definitions of idleness and over-provisioning. AWS—API Reference; Google Cloud—Overprovisioned VMs; Google Cloud—Idle VMs.
 <sup>31</sup>CASTAI— Cloud Cost Optimization and TechCrunch—The 10 Biggest Mistakes Made With AWS.

<sup>&</sup>lt;sup>32</sup>The key difference between our measure and those previously developed in the literature is that these papers tend to consider capacity as fixed in the short run and load as variable, while in our context, we think of load as fixed and the provisioned computing capacity as variable. Nevertheless, the common source of inefficiency is a mismatch between load and capacity.

et al., 2008). However, we perform robustness checks with our limited data on memory and network utilization in Appendix E.1. Finally, we do not account for more elaborate potential efficiency improvements, such as consolidating multiple VMs with 70% peak utilization into fewer VMs. While theoretically possible, such improvements may not be practical and would require additional implementation assumptions.

## 4.3 Comparison of Compute Productivity with TFP

Since the productivity literature has overwhelmingly focused on TFP, it is important to discuss the relative strengths and weaknesses of our compute productivity measure. TFP is defined as the residual in the production function after accounting for the contributions of observed inputs (Syverson, 2011). As the "unexplained" part of the output, it can correspond to various unobserved factors such as technology and management, offering limited insight into specific mechanisms by itself (Solow, 1957). Moreover, TFP estimation faces well-documented measurement challenges, including the conflation of physical productivity with revenue productivity (Foster et al., 2008), reliance on aggregate inputs (Orr, 2022), measurement errors (Collard-Wexler and De Loecker, 2022), and lack of high-frequency data.

While compute productivity is narrower in scope than TFP, as it does not take into account the full set of inputs and total output, it is attributable to a single input with a clear interpretation. Further, it is a physical productivity measure obtained directly from the minimal unit of production (VM). As a result, we can link our productivity measure to actual resource usage (core-hours and electricity) and analyze the mechanisms underlying inefficiencies. These advantages make it possible to study aspects of productivity that are hard to analyze using TFP, thereby complementing existing evidence on firm productivity.

# 5 Empirical Facts on Compute Productivity

We begin our analysis by presenting several facts about dispersion, persistence, and other aspects of compute productivity. Our goal in doing so is to compare and contrast canonical findings from the productivity literature to their counterparts in our setting. In the subsequent sections, we explore the mechanisms that make firms more productive in computing in more detail and analyze the evolution of productivity after cloud adoption.

# 5.1 Dispersion and Persistence of Compute Productivity

Figure 3 shows the unconditional distribution of firm-level compute productivity, while Table 3 reports various dispersion statistics estimated under different controls. We find substantial heterogeneity in compute productivity across firms. Productivity estimates

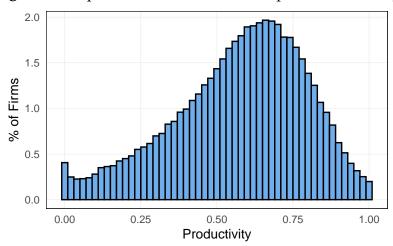


Figure 3: Dispersion of Firm-Level Compute Productivity

*Notes*: This figure shows the distribution of firm-level compute productivity as described in Section 4.1. The x-axis represents productivity levels ranging from 0 to 1, while the y-axis shows the percentage of firms. Productivity dispersion by industry is reported in Figure OA-4.

range from 0 to 1, where 0 indicates consistently idle VMs, and 1 represents fully efficient VM provisioning without idleness or overprovisioning. The productivity distribution is approximately normal, with a median of 0.62 and a mean of 0.60, suggesting that firms use only 60% of their provisioned compute resources productively on average. However, there is substantial dispersion around this mean: controlling for industry and time, the 90-10th percentile ratio is 3.53 and the interquartile range is 1.73, indicating that some firms use compute resources much more efficiently than others.

Next, we examine the within-firm productivity dispersion reported in Table 3. Different units within the same firm exhibit significantly different compute productivity: 55.7% of productivity dispersion is explained by within-firm variation. We further decompose this within-firm variation into within- and between-region components using data from multinational firms and find that cross-region heterogeneity accounts for 18.2% of the within-firm variation. Although this percentage is modest, it indicates that geographic location plays a non-negligible role in productivity differences, even within the same firm. These regional differences could be driven by human capital heterogeneity, the timing of the cloud adoption, or differences in management practices, as documented in Bloom et al. (2012). The large within-firm productivity dispersion emphasizes the importance of within-firm productivity dynamics, which we will revisit in Section 7.33

<sup>&</sup>lt;sup>33</sup>Another important aspect relating to within-firm heterogeneity previously studied in the IT context is the degree of organizational centralization (McElheran, 2014). While more centralized decision-making could alleviate monitoring frictions, it could also reduce local information advantages. In Table OA-5, we find a positive correlation between the amount of centralization and productivity among multi-unit firms, suggesting that monitoring frictions may dominate in cloud computing.

**Table 3:** Dispersion and Persistence of Compute Productivity

	A. Productivit	y Dispersion	ı Statistics	
0.60				
0.60				
0.00	-	-	-	
0.62	-	-	-	
3.51	3.49	3.53	3.53	
1.72	1.72	1.73	1.73	
-	0.009	0.002	0.012	
33.08	32.33	44.28	43.57	
66.92	67.67	55.72	56.43	
):				
5.88	-	18.22	_	
94.12	-	81.78	-	
Pane	nel B. Persistence (AR(1) Coefficients)			
0.93	0.93	0.93	0.93	
(0.00)	(0.00)	(0.00)	(0.00)	
0.64	0.63	0.64	0.63	
			(0.00)	
, ,	` '	` ,	0.30	
			(0.01)	
	3.51 1.72 - 33.08 66.92 ): 5.88 94.12 Pane	0.62 - 3.51 3.49 1.72 1.72 - 0.009  33.08 32.33 66.92 67.67  ):  5.88 - 94.12 -  Panel B. Persistence  0.93 0.93 (0.00) (0.00) 0.64 0.63 (0.00) (0.00) 0.32 0.30	0.62	

*Notes*: This table reports the dispersion and persistence of compute productivity conditional on different sets of control variables. Panel A presents statistics on the distribution of productivity, the decomposition of productivity dispersion into within- and between-firm components, and the decomposition of within-firm dispersion into between- and within-region components. Panel B shows the persistence of compute productivity through 1-month, 1-year, and 5-year AR(1) coefficients, with standard errors clustered at the firm level in parentheses. The industry refers to a 2-digit SIC code, and time refers to month. Further details on the estimation are provided in Appendix D.2, along with a visualization of persistence in Figure OA-6.

It is worth discussing our results in the context of the broader literature on productivity. We should expect compute productivity dispersion to be directionally ambiguous relative to canonical results: while focusing on a single input may reduce dispersion, the evolving nature of computing technology could lead to larger dispersion. Our findings indicate that dispersion in compute productivity is comparable to other estimates in the literature. For instance, Syverson (2004b) reports an average 90–10th percentile ratio of 2.45 in the US manufacturing sector, while other estimates include an interquartile range of 1.76 in US retail (Foster et al., 2006) and a 90–10 ratio of 5 in Chinese and Indian manufacturing industries (Hsieh and Klenow, 2009).<sup>34</sup> Our estimates of within-firm heterogeneity are

<sup>&</sup>lt;sup>34</sup>There are also estimates of productivity dispersion focusing on a specific input similar to ours. Fox and Smeets (2011) study labor productivity using Danish employer-employee data and finds a 90-10 ratio of 3.36,

also consistent with limited empirical evidence in the literature: Kehrig and Vincent (2024) and Orr (2022) find that within-firm dispersion explains 60% of the variation in capital's marginal product and 40% of the variation in product-specific productivity, respectively.

We next investigate another canonical finding on productivity: its persistence over time. The AR(1) coefficient estimates in Panel B of Table 3 suggest that compute productivity is highly persistent across different horizons. In 1-month and 1-year horizons, AR(1) coefficients are 0.93 and 0.64, respectively. Although persistence declines over longer horizons, it remains significant, as evidenced by a 5-year AR(1) coefficient of 0.32.<sup>35</sup>

Finally, we examine the extent to which observables explain the dispersion and persistence in compute productivity. The  $R^2$  estimates in Panel A suggest a limited role of observable factors: they explain at most 1.2% of variation in firm productivity, and the magnitudes of dispersion and persistence are similar across various control specifications. These results point to the role of unobserved heterogeneity across firms, mirroring common findings in the productivity literature (Fox and Smeets, 2011; Metcalfe et al., 2023). Moreover, it is consistent with Murciano-Goroff et al. (2024), who find similar evidence in the digital economy by showing that observable firm characteristics explain little variation in firms' propensity to use software with known vulnerabilities.

# 5.2 Productivity Differences by Firm Characteristics

This section examines how compute productivity varies by key firm characteristics, such as size and location. The drivers of compute productivity described in Section 2 suggest no clear *a priori* relationship between firm size and compute productivity. While larger firms may benefit from greater resources for complementary investments and skill development, they might also face more organizational frictions. Our findings in Table 4 support this intuition: there is no consistent relationship between firm size and compute productivity. While firms in the 2nd and 3rd quartiles of the size distribution are 1.0% and 2.8% more productive than those in the 1st quartile respectively, the largest firms are 3.8% less productive than the smallest firms. However, when we examine the components of productivity, the largest firms show 6.0% lower idleness productivity but 7.5% higher overprovisioning productivity compared to the smallest firms (i.e., larger firms are more likely to leave VMs idle but less likely to overprovision them). This pattern may reflect that larger firms face greater monitoring and incentive problems, potentially resulting in more idle VMs, while their superior IT capabilities reduce overprovisioning.

while Davis et al. (2008) report a 90-10 ratio of 7.3 in electricity productivity in the US Census.

<sup>&</sup>lt;sup>35</sup>Moreover, as shown in Table OA-6, the different components of productivity—idleness and overprovisioning—are also persistent, with idleness being more persistent than overprovisioning in the long run.

**Table 4:** Productivity Differences by Firm Characteristics

	Compute Prod.	Idleness Prod.	Overprov Prod
	(1)	(2)	(3)
	Panel A: Firm	ı Size (% difference relativ	e to 1st quartile)
2 <sup>nd</sup> quartile	0.010	-0.009	0.061
•	(0.003)	(0.002)	(0.005)
3 <sup>rd</sup> quartile	0.028	-0.007	0.127
•	(0.003)	(0.002)	(0.004)
4 <sup>th</sup> quartile	-0.038	-0.060	0.075
-	(0.003)	(0.002)	(0.004)
	Panel B:	Region (% difference relat	tive to EU)
US firms	0.052	0.048	0.033
	(0.004)	(0.003)	(0.002)
Industry FE	X	Х	Х
Time FÉ	X	Χ	X

Notes: This table reports productivity differences by firm size and region. Panel A presents the productivity estimates for firms in different size quartiles relative to the 1st quartile, obtained from a regression of the logarithm of outcome variables on size quartiles. Panel B shows the differences between US firms and EU firms using the same method. Columns (1-3) report the results for compute productivity, idleness productivity, and overprovisioning productivity, respectively. The estimates are obtained from firm-month level regressions, where the outcome variable is the logarithm of productivity specified in columns, with the control variables specified in the bottom panel table. The construction of firm-month level productivity estimates is described in Section 4.1 and Appendix D.1. Standard errors are calculated using the delta method, clustered at the firm level, and reported in parentheses.

Panel B focuses on firm location and reports the productivity differences between US and EU firms. We find that US firms outperform their European counterparts, achieving 3.3% to 5.2% higher compute productivity across different measures. This finding is consistent with Bloom et al. (2012), who find that "Americans do IT better," mainly due to differences in management practices.

Taken together, the empirical evidence on compute productivity aligns broadly with the extensive literature on firm productivity, despite differences in measurement approaches and our focus on computing. In this way, our paper complements the prior literature by showing that persistent productivity differences continue to exist with digital inputs.

# 5.3 Robustness Checks and Ruling Out Alternative Explanations

Several alternative explanations could generate the dispersion in compute productivity we observe. In Appendix E, we go over these explanations and present robustness checks that indicate they are unlikely to generate our results. We describe these robustness checks below.

The most important potential explanations are demand volatility and risk aversion:

seemingly inefficient firms may purposefully maintain idle and overprovisioned VMs as a precaution against rare demand spikes that ultimately do not materialize. As discussed in Section 4.2, we view this as a form of inefficiency in cloud computing, given the available tools that can automatically scale compute resources. Nevertheless, we conduct two exercises to show that this concern is unlikely to explain our results. First, we estimate multiple measures of firm-level demand volatility using our data and find that they explain less than 1% of productivity dispersion. Second, we calculate the probability that firms reach the capacity of their chosen VM and find that high-productivity (above-median) firms do not reach capacity more frequently than low-productivity firms.

Another explanation is that firms use computing for different purposes, which could inherently have different productivity patterns. Cloud providers offer a vast menu of VMs with different observable characteristics that are often tailored for different use cases. Hence, while we have already shown that industry has little explanatory power, controlling for VM characteristics—such as type and memory—can further help us condition on firms' use cases. We find that while VM characteristics have some explanatory power, more than 75% of productivity variation is among VMs with identical configurations.<sup>36</sup>

Our additional exercises also confirm the robustness of the results. First, we repeat our analysis using alternative definitions for downsizability and peak utilization and find that the results are robust to these choices. Second, we extend our analysis to other dimensions of VM utilization, memory and network, and find that they are positively correlated with CPU utilization, indicating that VMs identified as CPU-inefficient also tend to be inefficient in these dimensions. Third, we show that idleness and overprovisioning productivity, which likely have different sensitivities to alternative explanations, are positively correlated. Fourth, we estimate compute productivity using publicly available datasets from Google Cloud and Microsoft Azure and find comparable magnitudes of dispersion. Finally, as an external validity check, we find that firms with below-median productivity are 60.0% more likely to exit the cloud than those above the median, similar to existing results in the productivity literature (Foster et al., 2016).<sup>37</sup>

Beyond these empirical tests, many of our results support that productivity differences are not mechanical. For example, there is significant short- and long-term learning at

<sup>&</sup>lt;sup>36</sup>As reported in Figure OA-2, machine family and memory explain 4.1% and 6.8% of the variation, respectively. Even controlling for the precise configuration of a VM explains only 23.9% of the observed variation in compute productivity, some of which is mechanical given that configuration nests downsizability, a necessary condition for a VM to be overprovisioned. One would also expect VM characteristics to explain some productivity variation if choosing VM characteristics correctly is an aspect of productivity.

<sup>&</sup>lt;sup>37</sup>Such a result would be inconsistent with the demand volatility explanation for productivity dispersion. Cloud is especially beneficial for firms facing large demand volatility. If demand volatility were the primary driver of low productivity, we would expect low-productivity firms to be less likely to exit the cloud.

both firm and unit levels (Section 7), indicating that productivity is not solely determined by time-invariant firm characteristics. Moreover, the existence of productivity dispersion within firms and even within units suggests productivity differences do not arise only from use case differences across firms. Finally, the extensive evidence of productivity dispersion in various industries makes heterogeneity in compute productivity plausible, and the similarity between the established results and our findings further strengthens this conclusion.

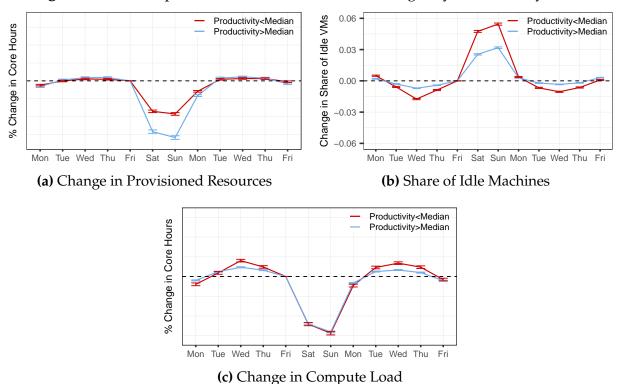
#### 6 Mechanisms: What Do More Productive Firms Do?

We have now established that firms differ dramatically in how efficiently they use computing resources, and that these differences are persistent. The economic literature and industry sources reviewed in Section 2.4 point to two primary drivers of these productivity differences: complementary organizational investments and cloud-specific skills. Since we lack data on managerial practices and complementary investments within firms, we cannot directly test the extent to which these factors explain productivity differences. However, each factor is likely to generate distinct patterns in VM provisioning behavior, which can be used to evaluate what makes firms more productive in computing indirectly.

In this section, we examine the association between three such patterns and productivity: responsiveness to demand changes, attentiveness to idle resources, and usage of a wider variety of VM types. First, firms that leverage cloud capabilities more effectively should be better at responding to changes in demand. To test this, we study provisioning decisions on weekends, when firms face a sizable drop in computing demand, and analyze whether more productive firms manage these short-term fluctuations more efficiently. Second, when there are mistakes and resources are left idle, firms with better monitoring capabilities should shut down these idle resources faster. Finally, firms with more knowledgeable employees likely match VM types to jobs more effectively, deploying a broader array of VM types rather than placing all workloads on a single type.

To study these factors, we perform the following out-of-sample exercise. We first classify firms as "high" or "low" productivity based on their productivity in 2022 relative to their industry's median productivity. We then analyze the differences in VM provisioning behavior between these two groups in 2023. In a similar manner to difference-in-differences, our analyses compare certain aspects of the VM provisioning behavior of high- and low-productivity firms relative to their within-group baseline, which avoids our results being mechanically driven by the level differences that are used to classify firms into productivity groups.

Figure 4: Firm Responses to Weekend Demand Changes by Productivity Level



*Notes*: These figures show the estimates of  $\beta_k^H$  and  $\beta_k^L$  from Equation (2), for three outcome variables: log provisioned resources, the share of idle VMs, and log compute load. Firms are classified as above- and below-median using productivity estimates from the 2022 sample, while the regressions are estimated using the 2023 sample. The crossbars represent 95% confidence intervals clustered at the firm level. The y-axes of Panels (a) and (c) are obfuscated for confidentiality reasons.

# 6.1 Responsiveness to Demand Changes

To analyze differences in responses to demand changes, we employ an event study approach and estimate the following specification:

$$y_{it} = \sum_{k=-6}^{7} \beta_k^H D_{i,t-k}^H + \sum_{k=-6}^{7} \beta_k^L D_{i,t-k}^L + \alpha_i + \gamma_{w(t)} + \varepsilon_{it}.$$
 (2)

Here,  $y_{it}$  denotes the outcome variable for firm i on day t.  $D_{i,t-k}^H$  and  $D_{i,t-k}^L$  are indicator variables for high- and low-productivity firms, respectively, where k indicates the position of each day relative to the first Friday within a two-week period. We include firm fixed effects ( $\alpha_i$ ) to account for time-invariant firm characteristics and time fixed effects ( $\gamma_{w(t)}$ ) for every two weeks to control for common time trends. The coefficients of interest,  $\beta_k^H$  and  $\beta_k^L$ , represent the average change in the outcome variable relative to Friday for high-and low-productivity firms, respectively. We estimate this regression for two outcome variables: the logarithm of total provisioned core-hours and the share of idle VMs.

Panels (a) and (b) of Figure 4 plot the coefficient estimates separately for high-productivity and low-productivity firms. Both groups use fewer resources and are more likely to leave VMs idle on weekends. However, high-productivity firms reduce computing resources by 75.2% more than low-productivity firms, resulting in significantly lower use of computing resources. High-productivity firms also utilize their provisioned resources more effectively: their probability of leaving VMs idle rises by only 2.6 pp on weekends, compared to a 4.7 pp increase for low-productivity firms.

One potential concern is that these results are driven by systematic differences in compute needs during weekends between low- and high-productivity firms. To address this, we run the same specification using the logarithm of compute load as the dependent variable and plot the results in Figure 4(c).<sup>38</sup> As expected, both groups experience declines in compute load during weekends. Notably, the magnitude of this decline is nearly identical across groups, indicating that differences in weekend provisioning behavior are not attributed to underlying weekend compute needs.<sup>39</sup>

#### 6.2 Attentiveness to Idle Resources

The second mechanism we study is how quickly low- and high-productivity firms detect and shut down idle resources. As previously discussed, idle resources are a common and well-documented phenomenon in the cloud that can occur when firms deploy VMs but fail to shut them off after use. Given that firms often run many VMs simultaneously, it may not be trivial to identify idle VMs, and firms with better monitoring capabilities should be better able to do so.

To test this, we estimate the speed at which low- and high-productivity firms shut down idle machines. We first identify all VMs that are idle for at least one day at the end of their lifespan. We then calculate, separately for low- and high-productivity firms, the probability that a VM that has remained idle for a given number of days is shut down the following day. Put another way, we compute the hazard rate of shutting down an idle VM. If more productive firms are better at identifying idle resources, then they should shut down idle VMs faster, resulting in higher hazard rates.

Figure 5 shows that high-productivity firms are significantly more likely to shut down

<sup>&</sup>lt;sup>38</sup>For each VM-day, load is given by multiplying the average CPU utilization with the VM's core-hours. The firm's total daily compute load is then determined by summing these VM-day loads across all active VMs. <sup>39</sup>We interpret load as primarily driven by demand. One potential concern with this interpretation is that not

<sup>&</sup>lt;sup>39</sup>We interpret load as primarily driven by demand. One potential concern with this interpretation is that not all compute load is demand-driven—firms can have control over the timing of some compute needs such as those for product development. To address this concern, we repeat the analysis focusing on software firms whose compute loads are more likely to be driven by customer demand and find similar results.

<sup>&</sup>lt;sup>40</sup>While the base rate of idle resources is higher for less productive firms by construction, conditioning on a resource being idle eliminates this mechanical correlation from our analysis.

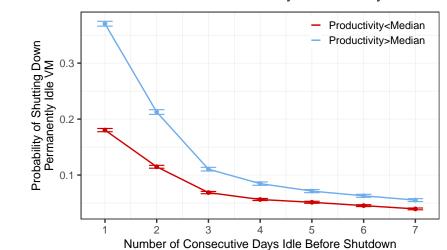


Figure 5: Shutdown Probabilities of Permanently Idle VMs by Productivity Level

*Notes*: This figure displays the probability that a VM that is idle for multiple days at the end of its life is shut down after each given number of days, conditional on being idle for at least that many days. The red line represents low-productivity firms, while the blue line represents high-productivity firms. The productivity levels are estimated using 2022 data, while the probabilities are estimated using 2023 data. The crossbars are 95% confidence intervals, with standard errors clustered by firm. Only VMs that last longer than one day and that end before the end of our sample period are included.

idle VMs promptly. They exhibit a 37.0% probability of shutting down a VM on the day it becomes idle, compared to only 18.0% for low-productivity firms. Even if a VM is not shut down on the day it becomes idle, high-productivity firms are more likely to shut it down on any subsequent day within the next week, if it gets to that day. Since this analysis conditions on VMs being idle, it abstracts away from factors that lead to idle VMs in the first place; therefore, it speaks more directly to differences in firms' monitoring capabilities.

#### 6.3 Usage of a Variety of VM Types

Firms have access to various types of VMs, many of which are optimized for specific workloads. While the quantity of provisioned resources can be automated with tools like autoscaling, selecting the appropriate VM type typically requires active, manual decisions by cloud users. As such, all else equal, firms with employees who are more knowledgeable about VM types would be expected to deploy a broader range of VM types.

With this idea in mind, we investigate VM selection behavior by testing whether more productive firms tend to use a wider array of VM series. To do so, we estimate the following regression at the firm level:

$$y_i = \beta D_i^H + Z_i' \gamma + \varepsilon_i. \tag{3}$$

Here,  $y_i$  represents a measure of dispersion in firms' usage of different VM series, including the Herfindahl–Hirschman Index (HHI; the sum of firms' squared usage shares), an

**Table 5:** Propensity to Use Different VM Series by Productivity Level

Dependent variable	prod >median	% of mean	prod >median	% of mean
HHI of usage across VM series	-0.095 (0.002)	-16.0	-0.068 (0.002)	-11.4
1(all usage on one VM series)	-0.119 (0.002)	-54.9	-0.093 (0.002)	-42.9
Number of VM series used	1.291 (0.029)	29.2	0.785 (0.026)	17.8
Adoption quarter/firm size FE Industry/region FE			X X	X X

*Notes*: This table displays the estimate of coefficient  $\beta$  from the regression shown in Equation (3), along with the ratio between the coefficient and the mean of the dependent variable. The left set of columns includes the raw difference between the groups, while the right set controls for cloud adoption quarter fixed effects, industry (2-digit SIC code) fixed effects, region fixed effects, and firm size quartile fixed effects. Firms are classified as above- and below-median using productivity estimates from the 2022 sample, while the regressions are estimated using the 2023 sample. Standard errors clustered at the firm level are in parentheses.

indicator for whether the firm only uses one VM series, and the number of VM series the firm uses. The coefficient of interest,  $\beta$ , multiplies a binary variable  $D_i^H$  that indicates whether the firm is high-productivity. Finally,  $Z_i$  includes firm-level controls: firm size quartiles, industry, region, and cohort quarter fixed effects.

Table 5 displays the results. We consistently find that more productive firms tend to use a wider array of VM series, both unconditionally and after controlling for firm-level covariates. For example, high-productivity firms exhibit a VM series HHI that is 0.067 lower than low-productivity firms—more than 11% of the mean HHI across firms. They also use a greater number of VM series and are significantly less likely to put all their usage on one VM series. These results suggest important differences in the sophistication between high- and low-productivity firms; high-productivity firms are more aware of the full range of VMs offered by cloud providers and are better able to take advantage of them.

In summary, this section documents significant differences in behavior among firms. Some firms use resources more productively both in steady-state and with changing demand, more effectively monitor and shut down idle resources, and deploy a broader array of VM types. These differences point to inherent factors that are not tied to a specific external mechanism but rather seem to be internal to the firm: some firms appear better at navigating internal frictions to reduce their costs (Leibenstein, 1966; Perelman, 2011). It is natural to expect that these factors evolve over time in the context of new technologies, as firms can monitor and improve their performance. We next analyze the extent to which this is the case.

# 7 Learning: How Firm Productivity Changes With Experience

In this section, we study learning: whether firms increase their productivity with experience and, if so, at what rate. It is natural to study learning in our setting because cloud computing is a relatively new technology, and firms typically require time to fully utilize and benefit from new technologies (Arrow, 1962; Forman and Goldfarb, 2006). We aim to provide evidence on how firms learn to use a general-purpose technology that may require complementary investments to use efficiently.

We present two sets of results. First, we document that firms improve their productivity over time—there is a strong relationship between a firm's productivity and its experience with the cloud. However, the learning process is slow, especially compared to existing evidence on learning-by-doing. Doubling a firm's experience increases its productivity by only 12.4% on average, and it takes approximately four years for firms to reach steady-state productivity. We explore potential reasons for this discrepancy by comparing our setting to those studied in prior research.

Second, we demonstrate *how* firms learn. By decomposing firm-level productivity growth, we find that nearly all productivity improvements occur due to the learning of individual units, with no contribution from reallocation across units. We further decompose within-unit productivity growth by examining how productively units use different VM types. We find that while units improve their productivity with the VM types they initially choose, even experienced units try new VM types, increasing usage of those that perform well and dropping those that they use poorly, suggesting that experimentation plays a role in the learning process.

# 7.1 Learning at the Firm Level

We study learning through two complementary approaches: (i) a cross-sectional analysis, which examines how productivity varies with firms' experience at a given point in time, and (ii) a cohort analysis, which tracks productivity over time within a group of firms.

At a given point in time, more experienced firms are substantially more productive than less experienced firms. Figure 6 plots the normalized average firm productivity from July to September 2022 against the duration each firm has been using the cloud as of that quarter.<sup>41</sup> The productivity gap is stark: firms with one year of experience are 34.6% more productive than firms that are new to the cloud. Experience is still positively correlated with productivity after the first year, but the relationship is weaker. Four-year-old firms

<sup>&</sup>lt;sup>41</sup>We focus on a three month period to balance the stability of our estimates against minimizing the amount of time-series variation incorporated into our cross-sectional analysis.

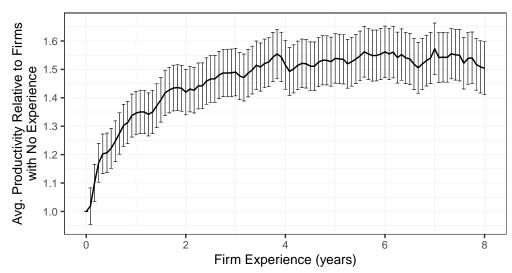


Figure 6: Productivity vs. Firm Experience in July-September 2022

*Notes:* This figure shows the average productivity level as a function of firm experience, measured in years since the firm first began using the cloud. The productivity level in the initial month (month 0) is normalized to 1. The crossbars indicate the 95% confidence intervals. The analysis is based on data from July-September 2022. The details of the estimation are provided in Appendix D.3.

are 51.6% more productive than brand-new firms, with relatively minimal productivity gains thereafter.

While suggestive, the cross-sectional relationship between experience and compute productivity alone does not establish the existence of learning. Two potential forms of selection bias warrant consideration. First, early adopters of cloud technology may have done so because they anticipated higher productivity. Second, there might be survivorship bias if less productive firms tend to exit, which increases the average productivity of surviving firms over time independent of any actual learning effects.

To address both forms of selection, we focus on the productivity growth of individual firm cohorts over time, conditional on survival to the end of our sample. Figure 7 plots the productivity over the second half of 2022 and the first half of 2023 for four cohorts of firms: those that adopted the cloud in June-July 2022, 2021, 2020, and 2019. We find that firms' productivity dynamics over time exhibit similar patterns to the cross-sectional pattern discussed above.<sup>42</sup> Firms that started in the middle of 2022 experienced a productivity increase of 33.1% during their first year. Their productivity at the end of their first year was similar to the productivity of the 2021 cohort at the start of their second year, suggesting

<sup>&</sup>lt;sup>42</sup>Figure 7 still includes some cross-sectional variation across different cohorts. We follow this approach because we do not have continuous productivity measures over four years due to the sparsity of our data. However, we are able to characterize long-term learning for the cohort that adopted the cloud in 2019 over four years in a way that only uses within-firm variation over time. This analysis still reveals clear evidence of learning among this cohort of firms in the long run. See Appendix E.9 for this result.

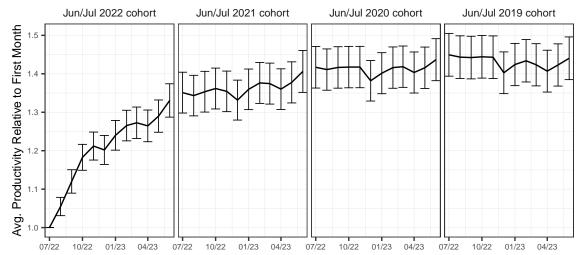


Figure 7: Changes in Firm Productivity Over Time by Cohort

*Notes*: This figure displays monthly average productivity estimates for four different cohorts of firms with different levels of experience (0-1, 1-2, 2-3, and 3-4 years) during the period between July 2022 and June 2023. The average productivity for the June-July 2022 cohort in July 2022 is normalized to 1. To be included in the analysis, a firm must have had nonzero usage every month from July 2022 to June 2023. Error bars indicate the 95% confidence intervals, with standard errors clustered by firm. The details of the estimation can be found in Appendix D.3.

that productivity dynamics are similar across cohorts.<sup>43</sup>

Over the subsequent years, the pace of learning slows substantially. Firms increase their productivity by 4.1% in their second year and by just 1.4% in their third year of cloud usage. Learning eventually plateaus, as evidenced by the 2019 cohort, which experiences no productivity gains in its fourth year. The relatively flat productivity level of older cohorts also suggests that learning is not driven by aggregate productivity trends in the cloud industry; if this were the case, then older cohorts would be getting more productive, too.

Having presented visual evidence of learning, we next estimate a standard power-law specification to allow direct comparison between our findings and prior estimates from the learning-by-doing literature (Thompson, 2012; Levitt et al., 2013). In this analysis, productivity is modeled as a function of experience according to the following form:

$$\log(\omega_{im}) = \alpha + \beta \log(E_{im}) + \varepsilon_{im}, \tag{4}$$

where  $\omega_{im}$  is firm i's productivity in month m and  $E_{im}$  is firm i's experience as measured by the length of time firm i has used the cloud as of month m. The parameter  $\beta$  reflects the rate at which firm productivity improves with experience, with higher values indicating

<sup>&</sup>lt;sup>43</sup>Across all cohorts, we observe seasonality in the estimates, with productivity consistently declining every December. This pattern resembles the weekend effect analyzed in Section 6.1 and can be attributed to reduced demand during the holiday period.

**Table 6:** Estimates of Learning Rate from Power Law Specification

	(1)	(2)	(3)	(4)	(5)	
		Panel A: Cross-sectional analysis				
Learning rate ( $\beta$ )	0.162 (0.004)	0.162 (0.004)	0.134 (0.003)	0.140 (0.003)	0.100 (0.003)	
		Panel B: Cohort analysis				
Learning rate ( $\beta$ )	0.169 (0.011)	0.169 (0.011)	0.146 (0.009)	0.151 (0.010)	0.137 (0.008)	
Day of week + holiday FEs VM family FEs		X	X X	X	X	
VM family x data center region FEs VM series x data center x OS FEs				Χ	Х	

*Notes:* This table displays the slope coefficient from a regression of log productivity on log experience (in months) given in Equation (4). In panel A, we include all firms in July-September 2022, while in panel B, we include only firms that started using the cloud in June-July 2022, 2021, 2020, or 2019 and include data from July 2022-June 2023. To be included in Panel B, a firm must have had nonzero usage every month from July 2022 to June 2023. Each column includes a different set of controls when estimating firm-month level productivity as detailed in Appendix D.1. Clustered standard errors by firm in parentheses.

## faster learning.44

Table 6 displays the results. Column (1) reports estimates using our baseline productivity measure as the dependent variable, while the remaining columns use the productivity estimates obtained under various controls as described in Appendix D.3. Each panel reflects a distinct source of variation; Panel A uses the cross-sectional variation reported in Figure 6, whereas Panel B uses the cohort-based variation shown in Figure 7.

Our baseline estimates from the cohort analysis imply that when a firm's experience doubles, its productivity increases on average by  $2^{0.169} - 1 = 12.4\%$ . While controlling for time variables does not affect these results, controlling for VM characteristics slightly reduces the learning rate in both analyses, which is consistent with the interpretation that part of the productivity increases reflects firms becoming better at selecting VMs. These results are similar to the cross-sectional analysis reported in Panel A.

Overall, our findings suggest that the rate at which firms learn to use the cloud is

<sup>&</sup>lt;sup>44</sup>In the learning-by-doing literature, it is common to measure experience either with (calendar) time or cumulative production. We focus on calendar time for our main analyses as there is substantial heterogeneity in firms' compute usage, making a cross-sectional analysis of productivity improvements as a function of cumulative usage difficult. However, as a robustness check, we redo the analysis in Panel B, column (1) of Table 6 using cumulative usage in core-hours as  $E_{im}$ , adding firm fixed effects to control for heterogeneity in the level of compute demand. We estimate  $\beta = 0.149$  (SE = 0.009), similar to the time-based estimate of  $\beta = 0.169$  (0.011).

slower than that observed in other contexts in the learning-by-doing literature. For example, while we estimate that productivity flattens out after four years, Levitt et al. (2013) study a car manufacturing plant whose productivity in producing a new model plateaued after eight weeks; Kellogg (2011) finds that cost reductions of pairs of oil producers and drillers flattened out after 20 weeks; and Thompson (2012) reviews evidence showing that the productivity of new shipyards in World War II converged within roughly two years. Another commonly reported metric in the learning-by-doing literature is the progress ratio, defined as the proportional increase in experience required for productivity to double, corresponding to  $2^{-\beta}$  in the power law model. Our estimates imply a progress ratio of 88.9%, which indicates slower learning relative to Levitt et al. (2013)'s finding of 81.2%, Benkard (2000)'s estimates of up to 81.8%, and much of the literature reviewed by Thompson (2012).

We attribute the slower pace of learning in our setting relative to the literature to the nature of the technology learned by the firm. Cloud computing is a general-purpose technology that simultaneously affects multiple parts of the firm and often requires structural changes to realize its full potential (Bresnahan and Trajtenberg, 1995; Brynjolfsson et al., 2024). This contrasts with most other learning settings where firms or employees need to learn a new manufacturing technique.<sup>45</sup> With this interpretation, our results suggest that firms require more time to implement structural changes compared to production-process-related improvements.

# 7.2 How Learning Affects Productivity Dispersion

While experience increases productivity on average, it is also important to consider its impact on the productivity distribution as a whole. Figure 8 analyzes this question in two ways. Panel (a) reports the evolution of average productivity across initial productivity quintiles over the first year of usage, whereas Panel (b) reports the 90th-10th percentile productivity ratio by firms' experience levels.

Panel (a) shows that learning is driven mainly by the initially low-productivity firms, which exhibit faster learning relative to the top. The average productivity gain of the firms in the bottom three quintiles in their first year is 116.3%. In contrast, firms in the top two quintiles exhibit relatively stable productivity trajectories (after an initial drop-off for the top quintile, which could be attributed to mean reversion after a favorable initial

<sup>&</sup>lt;sup>45</sup>A notable exception is Doraszelski et al. (2018), who study the evolution of firm strategies after a change in the market structure. Similar to us, they find a learning duration of three-and-a-half to four years. Another useful comparison is the literature studying learning at the individual worker level (Jovanovic and Nyarko, 1995; Haggag et al., 2017). This literature finds an even shorter learning period, suggesting that as the size of the learning unit increases, the duration of learning also increases.

Productivity Quintile in First Month

1.5

Overall 90–10th Percentile Ratio

Overall 90–10th Percentile Ratio

Overall 90–10th Percentile Ratio

Figure 8: How Learning Affects Productivity Dispersion

(a) Learning by Initial Productivity Level

Date

**(b)** Dispersion by Cloud Experience

Experience (years) as of July 2022

*Notes*: Panel (a) displays monthly average productivity estimates for five equally sized groups of firms in the June-July 2022 cohort during the period between July 2022 and June 2023. The groups are divided based on their productivity in July 2022. The average productivity for the third initial productivity quintile of the June-July 2022 cohort in July 2022 is normalized to 1. To be included in the analysis, a firm must have had nonzero usage every month from July 2022 to June 2023. Panel (b) displays the ratio between the 90th percentile productivity and the 10th percentile productivity over July 2022-June 2023 within cloud experience bins as of July 2022. The dashed line is the value in the sample as a whole, 3.51. The details of the estimation are provided in Appendix D.3.

draw). Despite the significant improvement among initially lower-productivity firms, the productivity ranking is preserved by the end of the period, consistent with persistent productivity differences.

Panel (b) directly analyzes the cross-sectional dispersion by calculating the 90th-10th percentile productivity ratio by firms' experience levels. We see that inexperienced firms have a significantly larger productivity dispersion than experienced firms do: dispersion is at 7.21 for firms without experience and steadily declines as we look at firms with more experience. Indeed, among firms with six years or more of experience, the 90-10 productivity ratio falls to 2.66, much closer to the US manufacturing average of 2.45 (Syverson, 2004b).

These results suggest that learning is an important determinant of the cross-sectional dispersion patterns discussed in Section 5. In particular, the dispersion in compute productivity can be partly attributed to cloud computing being a new technology with two contributing factors: there is heterogeneity in both the timing of adoption (which creates cross-sectional productivity dispersion across experience levels) and the rate at which firms improve their productivity (which creates within-cohort dispersion). As the technology becomes mature, we would expect both forms of dispersion to decrease over time.

#### 7.3 Decomposing Firm-Level Learning Across Units

While our results so far establish that firms improve their compute productivity over time, they do not reveal the mechanisms behind these improvements. In the remainder of this section, we investigate how firms learn by decomposing their productivity growth.

We begin by studying whether productivity improvements happen primarily across or within units. On one hand, learning might be driven by firms devoting more resources to more productive units (across-unit); on the other, individual units themselves may become more productive (within-unit). To quantify these mechanisms, we decompose firm-level monthly productivity growth using the method from Foster et al. (2001). Firm i has a set of units  $K_{im}$  in month m; each unit  $k \in K_{im}$  has monthly productivity  $\omega_{ikm}$ . We can express firm i's productivity in month m as the core-hour weighted average productivity of its units; that is, letting  $s_{ikm}$  be the core-hour share of unit k in month m,

$$\omega_{im} = \sum_{k \in K_{im}} s_{ikm} \omega_{ikm}. \tag{5}$$

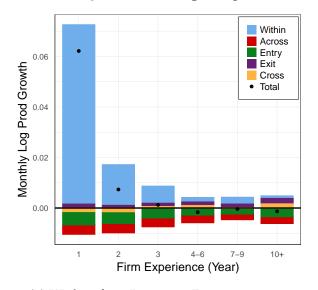
We are interested in decomposing  $\Delta \omega_{im} = \omega_{im} - \omega_{i(m-1)}$ , the change in firm i's productivity from month m-1 to month m. For ease of notation, we set m=1. Let  $S_{i1}=K_{i0}\cap K_{i1}$  be the set of units in firm i that used the cloud in both month 0 and month 1;  $X_{i1}=K_{i0}\setminus K_{i1}$  the set of units that stopped using the cloud in month 1; and  $E_{i1}=K_{i1}\setminus K_{i0}$  the set of units that started using the cloud in month 1. We can decompose  $\Delta \omega_{i1}$  as follows:

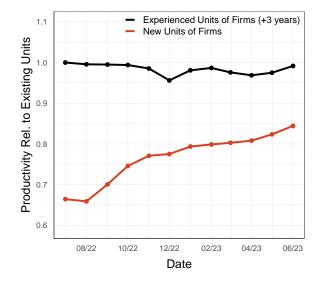
$$\Delta\omega_{i1} = \sum_{k \in S_{i1}} s_{ik0}(\omega_{ik1} - \omega_{ik0}) + \sum_{k \in S_{i1}} (s_{ik1} - s_{ik0})(\omega_{ik0} - \omega_{i0}) + \sum_{k \in S_{i1}} (s_{ik1} - s_{ik0})(\omega_{ik1} - \omega_{ik0}) + \sum_{k \in S_{i1}} s_{ik1}(\omega_{ik1} - \omega_{i0}) + \sum_{k \in X_{i1}} s_{ik0}(\omega_{i0} - \omega_{ik0}).$$

$$= Entry = Exit$$
(6)

The first term, *Within*, reflects the productivity growth coming from within-unit learning. The second term, *Across*, captures the productivity growth from the reallocation of compute resources across units and is positive when units that grow are more productive than the firm's average productivity. The third term, *Cross*, represents the correlation between unit-level productivity growth and the growth of the unit's share. The fourth term, *Entry*, represents the contribution of units that are new to the cloud and would be positive if their initial productivity is higher than the firm. Finally, *Exit* reflects the contribution of units that stop using the cloud and would be positive if they are less productive than the firm.

Figure 9: Decomposing Firm-Level Learning Within and Across Units





(a) Within-firm Learning Decomposition

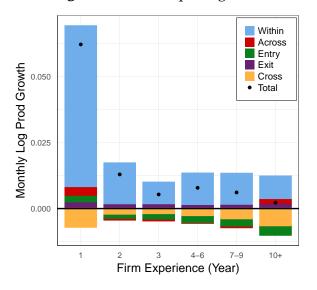
**(b)** New vs. Existing Unit Productivity

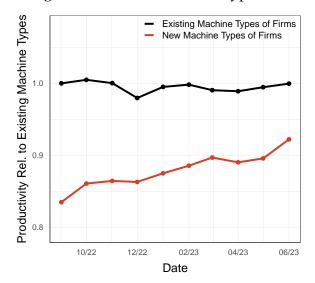
*Notes*: Panel (a) presents the decomposition of monthly log productivity growth by firms' years of experience with cloud computing, displaying the five components of Equation (6): within-unit, across-unit, entry, exit, and cross. The x-axis represents the firm's cloud experience in years, while the y-axis shows the monthly log productivity growth. The black dots indicate the average month-to-month productivity growth at the firm-level, whereas each bar represents a component of the decomposition. Panel (b) plots the average productivity of the units that joined in June-July 2022 against the average productivity of the older units in the same firm. The productivity of existing units in July 2022 is normalized to 1. The details of the estimation procedure are provided in Appendix D.4.

We apply this decomposition to each firm separately and then average the components across firms. Figure 9(a) plots these averages by firms' years of experience with cloud computing (colored bars) together with the overall average monthly productivity growth (black dots). The results suggest that the observed flattening-out of compute productivity over time masks substantial within-firm productivity dynamics. The *Within* components are large and positive during the first three years of the firm and remain positive yet small thereafter, indicating that (i) nearly all learning comes from units learning to be more productive and (ii) even if overall firm productivity growth plateaus after three years, individual units continue learning.

Other patterns in the data further confirm the role of within-unit learning. In Figure 9(b), we plot the productivity of units that newly adopt the cloud in the firm relative to the firm's existing units with at least three years of experience. New units start out with productivity 34.3% lower than experienced units in the same firm, yet they close about two-thirds of this gap within their first year. This magnitude is similar to the overall pace of firm-level learning shown in Figures 6 and 7, suggesting that new units in experienced firms do not learn differently compared to new firms. Thus, our analysis provides limited evidence for within-firm knowledge transfer and suggests that the changes required for efficient

Figure 10: Decomposing Unit-Level Learning Within and Across VM Types





(a) Within-unit Learning Decomposition

**(b)** New vs. Existing VM Productivity

*Notes*: Panel (a) presents the decomposition of monthly log unit-level productivity growth, displaying the five components of equation (6): within-type, across-type, entry, exit, and cross. The x-axis represents the firm's cloud experience in years, while the y-axis shows the monthly log productivity growth of the unit. The black dots indicate the average month-to-month productivity growth at the unit level, whereas each bar represents a component of the decomposition. Panel (b) plots the average productivity of the machine types that firms start using in August-September 2022 against the average productivity of the older machines in the same firm. The productivity of existing VMs in September 2022 is normalized to 1. The details of the estimation are provided in Appendix D.4.

computing use must occur at the unit level.<sup>46</sup> These patterns provide empirical evidence to the growing literature that highlights the importance of within-firm organizational structure (Crawford et al., 2018; Hortaçsu et al., 2024).

#### 7.4 Decomposing Unit-Level Learning Across VM Types

We further decompose learning within units to analyze how they become more productive. This time, we apply the decomposition in Equation (6) to within-unit productivity growth, breaking it down into VM-type components using the estimates of units' productivity in using different VM types from Section 4.<sup>47</sup> This analysis reveals how changes in a unit's productivity across different VM types contribute to the unit's overall productivity growth.

Results are reported in Figure 10(a). Units are broken out by the firm's cloud experience as before, and the black dots show the total within-unit component, which corresponds

<sup>&</sup>lt;sup>46</sup>In Appendix Figure OA-3, we further explore within-firm knowledge transfer by looking at whether new units' learning depends on the firm's productivity. We find that while new units at more productive firms exhibit higher productivity levels overall, their rate of productivity growth does not vary with the firm's productivity.

<sup>&</sup>lt;sup>47</sup>În this analysis, a VM type corresponds to a combination of VM series, data center, and operating system, which represent the primary VM dimensions along which learning can occur.

to the *Within* term of Figure 9(a). The results reveal that units' machine choices are not static; even more experienced firms try new machines and improve their productivity with the machine types they adopt. The *Entry* term is negative, reflecting the fact that units are less productive when they try machines for the first time. Units discard the less productive machines (the *Exit* term is positive) and get more productive with the machines they retain (the *Within* term is positive). Meanwhile, the *Cross* term is negative, reflecting that as firms add new machines, the share of their existing machines with increasing productivity declines, leading to a negative correlation between productivity and share changes.

Figure 10(b) provides deeper insight into the *Within* component by comparing the average productivity level of machine types with which units have at least three years of experience (black) to that of machine types they newly adopt (red). Units are 16.5% less productive with newly adopted machines compared to their existing ones. This productivity gap is notably smaller than the 34.3% difference observed between the productivity of new and existing units in Figure 9(b), indicating that even though there is learning at the machine level, units can transfer some of the productivity gains across machine types.

Overall, the patterns in the unit-level productivity decomposition in Figure 10 highlight long-run learning dynamics driven partly by experimentation. Aggregate productivity gains at the unit level are a compositional effect of productivity declines due to experimentation with newly-adopted machines, and productivity increases from learning to use the new machines efficiently and discontinuing the less productive ones that were tried. These findings mirror the experimentation-driven productivity dispersion documented by Foster et al. (2019) in innovation-intensive industries, demonstrating that such patterns are also at play in cloud computing.

# 8 Aggregate Impacts on Electricity and Compute Resources

This section analyzes the aggregate impacts of productivity dispersion in computing using a simple quantification exercise. Specifically, we estimate potential savings in compute resources and electricity usage if all firms were to reach a benchmark productivity level. Given that electricity is the main input in computing, our analysis captures not only the private costs of inefficient compute use incurred by firms but also the social costs resulting from increased electricity consumption. We note that this analysis is a partial equilibrium exercise that does not consider several important factors, including cloud providers' capacity constraints, potential price adjustments, or firms' behavioral responses to productivity improvements. As such, this section should be viewed as a quantitative exercise designed to illustrate the importance of productivity dispersion in computing

rather than a full modeling of the cloud market.

In our method, whose details are provided in Appendix D.6, we quantify the potential savings in core-hours and electricity consumption if all firms currently below the benchmark productivity level  $\bar{\omega}_m^c$  were to reach this benchmark. Formally, the counterfactual productivity of firm i in month m is given by:

$$\omega_{im}^c = \bar{\omega}_m^c \cdot \mathbf{1}(\omega_{im} < \bar{\omega}_m^c) + \omega_{im} \cdot \mathbf{1}(\omega_{im} \ge \bar{\omega}_m^c). \tag{7}$$

Calculating the core-hours consumed under counterfactual productivity is straightforward as it does not depend on how firms achieve benchmark productivity. In particular, the reduction in core-hours resulting from productivity improvements is not affected by whether a firm reduces idleness or overprovisioning. We therefore calculate the number of core-hours each firm frees up by reaching the benchmark productivity and then aggregate these savings across firms.

To estimate the counterfactual electricity usage, we first need to establish the relationship between electricity consumption and VM utilization. In Appendix D.5, we estimate this relationship using data from Google Cloud, which includes 5-minute power consumption readings from 57 power domains and corresponding CPU utilization of all VMs within these power domains. Our estimation shows that idle VMs consume approximately 50% of their maximum power, and each percentage-point increase in VM utilization results in an additional 0.5 pp increase in power consumption. Based on these findings, we propose the following functional form for the relationship between power usage and VM utilization:

$$\mathbb{E}[p_{jt}] = (0.5 + 0.5u_{jt})k_j^{max},\tag{8}$$

where  $k_j^{max}$  denotes the power consumption when VM j is utilized at 100%,  $u_{jt} \in [0,1]$  denotes the CPU utilization of VM j at time t and  $p_{jt} \in [0,k_j^{max}]$  represents the power usage at  $u_{jt}$  utilization. Following the computing literature (Bertran et al., 2010), we further assume that power consumption scales linearly with the number of cores, so we impose  $k_j^{max} = k^{max}c_j$ , where  $c_j$  is the number of cores in VM j, and  $k^{max}$  denotes maximum percore power consumption. Under these assumptions and using the calculations detailed in Appendix D.6, we estimate the total electricity savings if all firms attain the benchmark productivity level.

Figure 11 summarizes our results, showing resource savings (in percent) on the y-axis and benchmark productivity levels (ranging from the 50th to the 100th percentile of firm productivity) on the x-axis. The findings reveal large potential savings from increased

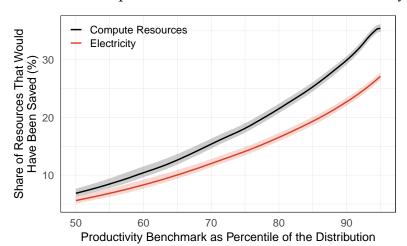


Figure 11: Resource Impacts Under Counterfactual Productivity Levels

*Notes*: This figure illustrates the changes in the shares of core-hours and electricity under a counterfactual increase in productivity. The x-axis represents the productivity benchmark as a percentile of its distribution, while the y-axis shows the percentage of resources that would be saved under different scenarios. The blue line indicates the percentage change in core-hours, and the red line indicates the percentage change in electricity consumption. Shaded regions surrounding each line represent the 95% confidence intervals obtained using a bootstrap procedure. The details of the estimation are provided in Appendix D.6.

productivity; simply raising all firms to median productivity leads to a 6.9% decline in compute resources and a 5.6% decrease in electricity use. These savings grow to 21.0% and 16.5%, respectively, at the 80th productivity percentile and ultimately reach 35.4% and 28.3% if all firms were to exhibit cost-minimizing behavior at full efficiency.

The results also highlight a nonlinear relationship between productivity improvements and resource savings, with core-hour savings consistently exceeding electricity savings. This gap arises because idle VMs fully use core-hours but only partially consume electricity. Further, the gap between compute and electricity savings grows as benchmark productivity rises, reflecting different elasticities of these resources with respect to productivity. These findings emphasize the importance of directly linking productivity to resource consumption to quantify the private and social costs of productivity dispersion.<sup>48</sup>

# 9 Concluding Remarks

A robust finding from the productivity literature is the high degree of dispersion in various firm outcomes, including productivity, markups, and the share of labor (Syverson, 2011; Van Reenen, 2018; Autor et al., 2020). In this paper, we show that similar differences

<sup>&</sup>lt;sup>48</sup>These estimates also enable us to quantify potential cost savings at the industry-level. Multiplying the core-hour savings by industry-level cost shares given in Section 2.4 indicates total potential cost reductions of up to 3.9% in the software industry and 1.8% in the services industry. These cost savings are even higher for low-productivity firms due to larger potential efficiency improvements and are likely to increase as computing becomes more widespread throughout the economy.

exist in how productively firms use new technologies by analyzing evidence from cloud computing. We also document firm learning that, while significant in magnitude, takes longer than previously studied learning-by-doing settings.

Our study uses CPU utilization data from over 1 billion VMs employed by nearly 100,000 firms. We develop a novel compute productivity measure and show substantial dispersion in the efficiency of computation usage across and within firms. To better understand this dispersion, we study the specific practices that separate high- from low-productivity firms, finding that more productive firms are better at adjusting compute resources in response to demand fluctuations, are more attentive to idle resources, and use a wider variety of compute inputs. Finally, we study learning after cloud adoption and find that firms that start using the cloud improve their productivity substantially in their first year and attain a stable productivity level within four years.

Our results have several implications for the broader productivity literature. First, although our productivity measure is specific to a single input and is derived from more granular data than is typical, our estimates of productivity dispersion and persistence corroborate the general magnitudes seen in other studies. Second, we find that productivity dispersion is dynamic in the context of a new technology—initial dispersion is extremely high, but shrinks over time due to heterogeneous learning rates across firms and saturation of the technology as a whole. Finally, our learning results demonstrate that within-firm dynamics play an important role in the evolution of aggregate productivity and its dispersion when adopting a new technology, reinforcing that efficient use of a new technology can take time even after widespread adoption.

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# Firm Productivity and Learning with Digital Technologies: Evidence from Cloud Computing

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# Appendix - For Online Publication

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#### A Additional Institutional Details

In this Appendix, we provide additional details about cloud computing that were omitted from the main text. This information was primarily compiled from the websites of major cloud computing providers and our conversations with industry professionals. This section aims to reflect the widely adopted practices in cloud computing that are relatively common across cloud providers. However, it may not apply universally to all providers.

#### A.1 Details on Cloud Computing

#### A.1.1 Types of Cloud Computing Products

Cloud computing products can be classified into three categories: Software as a Service (SaaS), Platform as a Service (PaaS), and Infrastructure as a Service (IaaS). SaaS differs fundamentally from PaaS and IaaS, as it encompasses a broader range of applications—including email services and productivity tools—and often targets end consumers rather than exclusively businesses. Therefore, we limit the discussion in this section to PaaS and IaaS.

PaaS products encompass a range of services that abstract away from the underlying infrastructure, allowing users to focus more on application development and deployment rather than managing physical or virtual hardware. Examples of these services include containers and serverless computing. Containers package applications with their dependencies, ensuring consistent and reliable performance across different environments, while container orchestration tools manage the deployment, scaling, and operation of these containers. Serverless computing enables developers to run code without provisioning or managing servers, as the cloud provider handles the infrastructure, scaling, and execution of code in response to events.

Despite the convenience of PaaS services, IaaS remains more common among firms, especially during our sample period, because it provides a high degree of flexibility and control, allowing users to tailor the underlying infrastructure to their specific needs. This level of control is important for complex, custom applications and enterprise environments that require precise configurations. Additionally, IaaS can accommodate a wide range of workloads, from legacy applications to modern microservices, making it more versatile than PaaS services.

#### A.1.2 Resource Availability in Cloud Computing

In cloud computing, firms typically request a quota that specifies the maximum amount of computing resources they may provision at any given time. Once this quota is established,

users can access the resources up to the quota whenever they need them. Except for a few specialized VMs, firms can adjust their quota at any time, at no additional costs, and quickly. Even though the quota cannot guarantee the immediate availability of resources, the high reliability of cloud services ensures that firms rarely face situations where their resource requests cannot be fulfilled.

Cloud computing providers ensure sufficient capacity is available by investing in data centers. While predicting the needs of individual firms can be challenging, cloud providers can more accurately forecast aggregate demand across all users by leveraging the law of large numbers. Therefore, they can predict compute demand more accurately than individual firms and invest accordingly to maintain sufficient infrastructure.

However, aggregate demand remains volatile, requiring cloud providers to balance supply and demand in real time. Cloud providers use a mechanism known as spot instances to manage this. Via spot instances, cloud providers rent out unused capacity at steep discounts, offering a cost-effective option for firms with workloads that are less sensitive to interruptions. However, these instances come with the caveat that they can be reclaimed at any time with short notice. Essentially, cloud providers invest in infrastructure to ensure they can meet peak demand and then monetize the temporary excess capacity due to demand volatility through the spot market.

#### A.1.3 Pricing in Cloud Computing

Cloud computing primarily employs an on-demand pricing model, allowing users to pay solely for the resources they actually provision. This model typically involves linear prices, meaning that costs scale directly with the amount of resource requested—whether it is computing power, storage, or bandwidth.

For VMs, providers implement a granular billing model based on per-minute—or in some cases, per-second—usage rather than billing in hourly increments. The billing system records the precise start and termination times of each VM and computes the total active duration in the time intervals. If the active period falls below a defined minimum unit, the usage is rounded up to that smallest increment. The applicable rate per time unit is determined by the VM's configuration details, including the number of virtual CPUs, the amount of allocated memory, storage type, and the geographic region in which the VM is deployed.

In addition to this on-demand structure, cloud providers offer more specialized pricing options tailored to different usage patterns. Reserved instances, for example, enable users to commit to a specified amount of resource usage over an extended period in exchange for discounted rates, benefiting workloads that are predictable and steady. Alternatively, as

described above, spot instances provide resources at significantly reduced rates but with the caveat that providers can reclaim those resources with minimal notice. Despite these varied pricing strategies, cloud costs can still be thought of as mainly variable costs from the firms' point of view, as the price paid (negotiated or not) is directly tied to the level of resource consumption.

#### A.2 Details of VM Deployment

This section provides details of deploying VMs separately for (i) manually through browser-based platforms and (ii) automatically through tools like autoscaling.

#### A.2.1 VM Creation and Selection

All cloud providers offer a browser-based platform with step-by-step instructions for generating a VM. These instructions typically apply for first-time VM creation and may not be as relevant for firms' day-to-day VM deployments. In this section, we detail the steps involved in selecting a VM. In the following subsection, we review the tools commonly used by firms for VM deployment and management.

**Account Creation:** Before deploying VMs, an account needs to be created and configured—this can be either an individual user account or a business account. This involves setting up the necessary permissions and roles to ensure that users or services have the appropriate access levels to manage and interact with the VMs.

**Resource Allocation:** During deployment, specific amounts of CPU, memory, and storage must be chosen for the VM.

**Network Configuration:** If the VM needs connectivity, a network connection step is needed. This involves assigning IP addresses, configuring network interfaces, and setting up necessary VLANs (Virtual Local Area Networks).

**Storage Provisioning:** VMs require storage for the operating system, applications, and data. This can involve allocating space on local disks or choosing a storage system linked to the VM.

**Security Settings:** Security configurations need to be applied during deployment. This includes setting up firewalls, defining access controls, and implementing any required encryption.

**Region Choice:** The user selects the geographic region of the data center for the VM. This choice can impact performance due to latency and varying redundancy policies.

This procedure applies when creating a VM for the first time. In practice, developers use VM images, which are templates that store information such as the OS, security settings, and pre-installed software, allowing users to create VMs without redefining these

parameters. Firms often maintain a library of standardized images for various purposes, facilitating the VM deployment process.

#### A.2.2 Automated Tools For VM Deployment

As we argue in Section 2.4, there are many available tools in cloud computing that help dynamically adjust compute capacity both horizontally and vertically. In this section, we list some of these tools and provide a brief description.<sup>49</sup>

Cloning a VM: Cloning technology allows users to create new VMs from the running state of an existing VM. The cloned VM is identical to the source VM and can be created quickly at any point in time. This method is suitable for large-scale applications and enables the creation of many VMs on a single host. All major cloud providers offer some form of cloning capability.

**Auto Shutdown:** In cloud computing, users have the capability to schedule or automatically shut down VMs to help manage costs and optimize resource usage. This functionality allows users to define specific times for VMs to stop and start, eliminating the need for constant monitoring.

**Live Migration:** Live migration allows users to move running VMs from one physical host to another without downtime. With this technology, applications can continue to operate during maintenance, load balancing, or hardware upgrades.

Automatic Redundancy and Fault Tolerance: Cloud providers offer built-in automatic redundancy and fault tolerance to ensure high availability and reliability of services. These features include distributing data and workloads across multiple servers, data centers, or geographic regions to prevent single points of failure. In case of hardware or software failures, automatic failover mechanisms can redirect traffic to healthy instances, minimizing downtime and maintaining service continuity.

Autoscaling: Autoscaling refers to the automatic adjustment of compute resources based on the current demand. This capability allows cloud environments to dynamically allocate or deallocate resources such as CPU, memory, and storage to applications or services as needed. When demand increases, autoscaling provisions additional instances to handle the load, ensuring that applications can maintain performance levels. Conversely, when demand decreases, it reduces the number of active instances, scaling down the resources in use. The process of autoscaling involves automatic monitoring of the performance metrics and resource utilization of applications. Firms can set autoscaling rules and policies based on their specific requirements, such as thresholds for CPU usage, memory consumption, or network traffic. For example, if CPU utilization exceeds a certain threshold, the autoscaling

<sup>&</sup>lt;sup>49</sup> AWS—Cost Optimization; Azure—Deployment Optimizer; Google Cloud—Cost Management.

mechanism adds more instances to distribute the load. Similarly, if resource usage falls below a specified level, it scales back the instances. These rules can be configured through cloud provider dashboards or APIs.

**Predictive Autoscaling:** Rather than adjusting compute resources in response to current demand, predictive autoscaling attempts to adjust compute resources in advance of upcoming demand fluctuations. This is suitable for latency-sensitive workloads such as streaming platforms. All major cloud providers offer some form of predictive autoscaling, in which they attempt to predict users' workloads based on past workload patterns of both those users and other similar users. Users are also able to develop their own predictive models themselves.

**Load Balancers:** Load balancers distribute incoming network traffic across multiple VMs. By evenly distributing the load, load balancers ensure that no single server hits capacity. They achieve this by monitoring the health of instances and redirecting traffic away from failing or underperforming instances. Load balancers complement autoscaling by working together to optimize resource utilization and application performance. While autoscaling dynamically adjusts the number of active VMs based on demand, load balancers distribute the incoming traffic among these VMs.

Cost Monitoring Tools: Cloud providers offer a range of tools to help users monitor and manage their resource utilization and costs. For example, AWS CloudWatch provides monitoring for resources and applications across AWS environments. It includes visualization tools, automated alarms, and integration with other AWS services to help identify and manage idle resources. Similarly, Google Cloud Operations offers integrated monitoring, logging, and tracing for applications and systems on Google Cloud. These tools may also include the observability of metrics specific to detecting and managing idle resources.

# A.3 Two Examples of VM Deployment

In this section, we provide two examples of deploying IT resources in cloud computing to help readers understand their use cases. While this section is quite technical, it may help inform readers about the day-to-day work of software developers in cloud environments.

#### A.3.1 "Create, Read, Update, Delete" Application

The first toy example we consider is the deployment of a simple CRUD (Create, Read, Update, Delete) application. This refers to a general class of applications that provide a user interface for the typical operations involved in persistent storage. A common example of this application is a blog or message board. In this example, "Create" corresponds to a user making a new post or comment, "Read" corresponds to the functionality of listing all

posts and comments corresponding to some filter, "Update" corresponds to editing posts or profile information, and "Delete" corresponds to the deletion of posts or comments. The basic components of the architecture of this application include a web server, which is accessible by users on the public internet, and a database server, which is typically only accessible by the web server itself. The web server's responsibilities include authenticating users, producing HTML that provides the information and features available to the user, and issuing control commands and queries to the database based on the user's request.

We describe specific deployment scenarios of this application type on the Microsoft Azure cloud. For the first example, we consider hosting this application only in a single region, with a fixed resource footprint, and with manual processes to deploy resources. To complete this deployment, we:

- 1. Create a Resource Group (RG), a logical group that will contain all of the resources for this deployment.
- 2. Create a Virtual Network (VNet) and create a subnet within this VNet.
- 3. Select and provision an appropriate VM to run the web application based on our application's requirements, budget, and account quota. Additionally, we must:
  - (a) Select the proper region and operating system for the application.
  - (b) Add the VM's network interface to the appropriate subnet within the VNet.
  - (c) Create a Network Security Group (NSG) and add rules that restrict the incoming traffic to SSH/RDP and HTTPS traffic from internet IP Addresses.
  - (d) Give the VM a static IP address. It is also possible to give it a human-readable alias using Azure DNS.
- 4. Create an Azure Database for PostgreSQL to serve as the persistent storage back-end for the application.
  - (a) Similar to the web server VM, we must choose an appropriate virtual core count, virtual memory amount, storage size, storage scale rule, and storage performance tier based on our requirements and budget.
  - (b) We will place the database in the same region as our web server.
  - (c) We will disallow public IP access to the database and integrate it into the existing VNet and the same or new subnet.

At this point, our resources are established and we can install the application onto the web server and complete the connection between the application and the database to be able to service user requests using the persistent storage. We can monitor the health and utilization of the instances using Azure Monitor.

The above architecture leans towards using IaaS solutions and is not capable of scaling horizontally. It is a simple deployment method that can be hard to maintain, and the architecture will likely be insufficient to handle dynamic loads. Since we can only control the size of a single instance for the web server and database, respectively, it will be challenging to avoid being under- or over-provisioned, and we will incur downtime in the application if we need to scale instances up or down. A common way to handle this is by using IaaS offerings for the web server, such as a Virtual Machine Scale Set (VMSS, Azure's autoscaling solution) and Load Balancer (LB). The VMSS is a collection of identical VMs in a single region. With this deployment method, we can define conditions on the pool of VMs that will trigger custom scale-up and scale-down actions. These rules or conditions are defined by statistics on the time series of instance-level counters such as CPU, Network, and Disk Utilization. The LB can be configured with a front-end IP address to accept user traffic and then given the VMSS as a back-end pool to distribute requests over. This architecture allows us to scale horizontally instead of vertically, increasing our ability to handle dynamic loads, making us less likely to be under or over-provisioned at any given time, and decreasing our application's expected downtime.

#### A.3.2 Data Analytics and Machine Learning Application

Another common use of modern public cloud infrastructure is building pipelines for data analytics and machine learning use cases. Since many of these use cases can be implemented purely as PaaS services, we will focus on a sample architecture that favors IaaS resources for batch training of a custom machine learning model or a numerical simulation. In these settings, it is common to have a highly parallelizable workload that consists of iterating over a set of parameters or hyperparameters for an underlying model or simulation, where for each parameter setting, we wish to construct the model or simulation according to the specified parameters, and then train the model or execute the simulation and store the relevant results from the process. We could implement a system like this using Azure Blob Storage or Azure Data Lake Storage (ADLS) to store the model or simulation parameter configurations and training/simulation results, Azure Batch to acquire the required capacity and allocate jobs to nodes, and then either a single dedicated VM or cluster of dedicated VMs that orchestrate the Azure Batch node pool and collate results from the storage. The exact steps to provision these resources and develop the

code to orchestrate and execute the jobs are involved, but we can describe an outline of the process and architecture:

- 1. Provision a storage account and create a container that will store model/simulation result blobs and another container to store blobs defining the model/simulation parameters.<sup>50</sup>
- 2. Provision an Azure Container Registry, construct a Docker image, which defines the functionality of the model or simulation given the parameter data, and write that Docker image into the container registry.<sup>51</sup>
- Given an estimate of model training time and the desired parameters to iterate over, estimate the number of worker nodes needed to complete the entire batch job in a reasonable time period.
- 4. From the orchestration nodes, construct the parameter data structures, write them to storage, and then define jobs using the Azure Batch API, which points to the parameters in storage and the image stored in the container registry.
- 5. Start the job and monitor the job status for task-level failures from the orchestration nodes.
- 6. Detect when the job completes and collate the results to make model parameter selection or generate simulation reports on the orchestration nodes.

This architecture still leverages some PaaS services to manage persistent storage and container images. Azure Batch is capable of acquiring very large amounts of capacity (tens of thousands of instances) relatively quickly and efficiently, allocating work to the acquired nodes.

All of the examples listed above comprise only a small fraction of all of the use cases of modern public clouds like Azure. However, even among this small sample, we see significant variability in terms of the PaaS services coupled with our deployed VMs and the potential utilization patterns of the deployed VMs themselves. The latter utilization variability by use case is relevant to the VM counter data examined in this paper. For example, in the CRUD application case, we are subject to an uncontrollable and variable

<sup>&</sup>lt;sup>50</sup>A blob, short for Binary Large Object, is a collection of binary data stored as a single entity in a database management system. In the context of cloud storage, blobs are used to store large amounts of unstructured data such as text, images, videos, or, in this case, model/simulation results and parameters.

<sup>&</sup>lt;sup>51</sup>Docker is a platform that uses OS-level virtualization to deliver software in packages called containers. These containers are lightweight, standalone, and executable packages of software that include everything needed to run an application: code, runtime, system tools, system libraries, and settings.

amount of user requests in the future and must design our architecture to handle both the expected and unexpected variability in this load. In the model training pipeline, we can learn more about the workload ahead of time. Instead, we need to focus on ensuring that the worker pool is sized correctly and that we efficiently pack jobs onto the nodes.

# B Data Appendix

#### **B.1** CPU Utilization Data

CPU utilization is a fundamental metric in computing that quantifies the workload on a computer's central processing unit. It is typically expressed as a percentage, representing the proportion of time the CPU spends executing non-idle tasks relative to its total available processing time (Gregg, 2014).

The most common method for measuring CPU utilization relies on system counters provided by the operating system. These counters continuously track the CPU's state, recording the time spent in various modes such as user mode (executing application code), system mode (executing kernel-level operations), and idle mode. By sampling these counters at regular intervals, typically every few milliseconds, the operating system can calculate the percentage of time the CPU spends in non-idle states (Gregg, 2014). These data are then aggregated over longer periods (e.g., seconds or minutes) to provide a meaningful representation of CPU usage.

The raw data we have access to are aggregations of counter readings to the 5-minute level, taking the maximum utilization reading in each 5-minute interval. Therefore, for each VM, at a 5-minute interval, we have the maximum CPU utilization. Since we have data on more than 1 billion VMs, the data at this granularity are not manageable, and we further aggregate these data to the VM-day level by calculating the inverse CDF of the distribution of max CPU utilization recordings in 5% intervals. In particular, for each 5% increment, we calculate the share of 5-minute max CPU utilization recordings under 5%, 10%, . . . , 95% utilization. We also record the maximum CPU utilization and the total number of hours the VM is running during that day. This sample forms the primary dataset for all analyses conducted in the paper.

#### **B.2** VM Data

Together with the information on CPU utilization of VMs, we also collect information on the important characteristics of VMs to understand their usage patterns and performance. Our data include the data center of the VM, which is anonymized for privacy and security reasons. However, we observe the geographical region of the data center, categorized into

US, EU, and Other. This helps identify the geographical location of the firm and whether firms and units run jobs outside of their domestic country. We also observe the series to which each VM belongs. Cloud providers group VMs of similar sizes, hardware, and features into the same families, typically referred to as machine series or instance types, depending on the cloud provider.<sup>52</sup> The VM series information is anonymized, and we only observe a unique identifier for confidentiality reasons.

Another important piece of information is the VM family, which categorizes VMs based on their primary purpose, such as general-purpose, compute-optimized, memory-optimized, and storage-optimized. We observe the actual values of these variables, allowing us to analyze the families of VMs used by each firm. In addition, we observe other key VM characteristics, including their operating system (Linux or Windows), memory, and number of cores.

These VM characteristics include the following set of VM groupings, which we use throughout the text.

- 1. The VM family, as described above, categorizes VMs based on their primary purpose. It takes the values of general-purpose, compute-optimized, memory-optimized, storage-optimized, HPC (high-performance computing), or GPU (graphics processing unit).
- 2. The *VM series* is a more granular indicator of the architecture of the VM. Each VM series is defined by a combination of hardware, such as the processing chip, and certain proportions or features, such as the available memory and CPU combinations. Generally speaking, VMs that are in the same VM series will only differ according to the data center they are physically located in, size attributes such as cores or memory, and their operating system; the VM series defines all other attributes of the VM.
- 3. The *VM product* is a unique combination of VM series, data center, and operating system. This variable reflects all of the characteristics of a VM besides its memory and CPU capacity.
- 4. The *VM configuration* is a unique combination of a VM series, data center, operating system, number of cores, and amount of memory. This variable represents the exact hardware and operating system that the VM user chooses and is the most granular variable that classifies a VM.

<sup>&</sup>lt;sup>52</sup>For examples of machine series from top providers, see these links: Google Cloud—Machine Families, AWS EC2—Instance Types

#### B.3 Firm and Unit Level Data

There are two ID variables associated with the creator of each VM in our CPU utilization data. The first one is unit ID. The unit ID collects all users that share a system administrative structure for oversight of the VMs and a payment/billing account with the cloud provider. Each unit ID is then associated with a higher-level firm ID.

Although our CPU utilization data are intermittent between 2017-2023, we have unit-month and firm-month level panel datasets that cover the entire sample period from 2017 until mid-2023. These panel datasets contain monthly normalized statistics on the cloud usage of each unit and firm, including the number of VMs deployed, the number of active VM days, a measure of cloud spend, and the total number of hours and core-hours across all VMs on the cloud. The values are normalized relative to the first usage month of each firm.

In addition to these panels, we also have datasets containing detailed information on each unit and firm in our sample, including their industry classification. Notably, our classification method differs from the standard NAICS and SIC systems; it follows what is known as the "vertical" definition—a common terminology in industry jargon. This vertical classification provides a level of granularity that falls between 2-digit and 3-digit SIC codes, which we subsequently map to 2-digit SIC codes.

Regarding location information, each firm is associated with a billing address. Although we do not have access to these addresses, we observe indicators showing whether a firm has a billing address in the US, EU, or other regions, as well as an indicator for whether a firm is multinational (i.e., has billing addresses in multiple countries). Additionally, we derive a "usage region" for each firm and unit based on the data center locations where they have the most VM usage. Because network latency increases with the distance between the user and the data center, cloud users typically select data centers within their own region. Thus, the region with the highest compute usage serves as a useful proxy for the firm's or unit's operational location. We use this information for a small number of firms for which the billing location is not available.

Finally, our data also includes quartiles of an independent and internal measure of firm size for each firm that proxies the number of employees of the firm. These quartiles are computed separately within each region-industry-year combination.

# **B.4** Sampling Details

In addition to aggregating our data to the VM-day level, we implement several additional measures to reduce data volume and fully anonymize firm identities. With our VM-day dataset, we perform three such sampling steps. First, we filter out the firms that fall

below fixed thresholds for total usage and consistency of usage. This step eliminates a small number of firms with negligible cloud usage. Second, we thin the right tail of the distribution by sampling the firms in the top few percentiles of the distribution (measured by total usage) at an undisclosed sample rate. This sampling is needed to (i) reduce the size of the data further because the firms in the top percentiles could have a very large number of VMs and (ii) eliminate the possibility of identifying large firms. This step still maintains a sample that is representative of a wide array of firms, only reducing the number of very large firms in the sample. Finally, we sample VM-day observations for every firm at a fixed undisclosed rate that is between 70% and 100%.

### **B.5** Data Cleaning Procedure

In addition to the initial cleaning and sampling applied to the raw data, we further filter the VM-day data to exclude firms with low usage and eliminate short-duration VMs.

First, we remove VMs with a duration of less than 20 minutes. Such VMs are typically used to initiate another job—like testing configurations, starting batch processing, or briefly scaling to manage temporary demand spikes—and they account for a negligible share of total core-hours. We also exclude a very small fraction (less than 0.01%) of VMs running operating systems other than Linux or Windows, or those missing key information such as memory or VM configuration.

At the firm level, we exclude firms that are inactive for more than 80% of the months between their cloud entry and exit month and those with less than 100 hours, 500 core hours, or 200 VM-days of usage. These criteria ensure that each firm included in our analysis has a sufficient sample size to accurately estimate their productivity. These cleaning steps affect fewer than 1% of the firms in the raw data.

# **B.6** Publicly Available CPU Utilization Data

There are a number of publicly available datasets detailing CPU utilization information pertaining to both cloud and cluster environments. These datasets are called *traces*. These traces often provide data on users and compute hardware as well.

Traces are collected from real-world computing environments. Providers of these computing resources make their traces publicly available for research, analysis, and educational purposes. Below, we describe three usage traces. The first dataset we describe was released by Google Cloud (GC) and is a trace of a high-performance computing cluster. The second dataset is a public *power* trace provided by GC (Google, 2019). The third was released by Microsoft Azure (Azure) and is a trace of a cloud computing environment.

As in the main text, the key variables in these datasets pertain to the characteristics of

provisioned VMs and their utilization information. Each of the datasets described in this section is a trace of cluster information about users' resources, compute activity and the networks within which their VMs run workloads.

#### B.6.1 Google Cloud Platform Cluster Trace

The contents of this trace allow studying of job scheduling and cluster management (Verma et al., 2015; Tirmazi et al., 2020). However, our main interest in these data is to use the information provided on CPU utilization to measure the compute productivity of users. The GC trace was sampled in May 2019 and pertains to eight clusters utilizing Google's *Borg* cluster manager. These clusters are located in data centers in New York and Chicago in North America, Helsinki and Brussels in Europe, and Singapore in Asia.

The unit of observation in the usage component of the trace data is a *task*. Tasks are processes that originate from programs running as part of jobs submitted to the cluster manager by users. The tasks detailed in this trace are either the result of jobs run by Google engineers, or they are run within resources available to Google services used by internal or external users (Wilkes et al., 2020). Tasks are executed either within resource allocations (similar to a VM) or directly on machines. Observations are recorded every five minutes.

On the user end, these data contain the requested VM, its usage statistics, and user-configured constraints on the requested resources. The resources users can request are memory (RAM) and CPU cores. CPU requests are measured in internal "Google Compute Units" (GCUs), which are similar to CPU cores but enable the comparison of compute hardware across machines in the data (Wilkes et al., 2020). The GCU measurements are reported after being normalized by a constant factor. CPU usage (i.e., GCU usage) is measured in CPU-seconds and reported after being normalized. Therefore, dividing the normalized CPU usage by the normalized CPU requested provides the utilization information. The data also contains information about machine attributes, machine availability, obfuscated user and job identifiers, and variables that track events, missing data, and reasons for task failures.

#### B.6.2 Google Cloud Platform Power Trace

The content of this trace complements the trace above in that it provides information on the power consumption of the physical machines from the GC cluster trace during the same sampling period, May 2019. This enables us to measure the relationship between CPU utilization and power consumption.

The power consumption data is available at the power distribution unit (PDU) level. The power that is drawn into the data center is stepped down into a PDU, which is the main

distributor of power in a data center. PDUs manage the flow of power to equipment and monitor environmental factors like temperature and humidity. Modern cluster computing produces large amounts of heat. Therefore, measuring power consumption requires accounting for the composite power supply to both IT (e.g., servers) and non-IT (e.g., coolers) resources (Singh et al., 2015; Athavale et al., 2018). Since PDUs manage power supplied to clusters and their supporting IT equipment, as well as non-IT equipment such as cooling resources, the power trace provided by GC incorporates both IT and non-IT power demands.

The GC dataset includes power utilization levels of 55 PDUs, which manage the power supply to each of the clusters in the GC cluster trace. The power for each cluster is managed by multiple PDUs. The data include two key variables: total power utilization and production power utilization. Total power utilization, measured in 5-minute intervals, indicates the percentage of available power capacity consumed through a PDU for all IT and non-IT equipment, including coolers. Similarly, production power utilization is an estimated measure provided by GC that details the power consumption attributable to production workloads, including power consumed by non-IT equipment.

#### B.6.3 Microsoft Azure Trace

Azure publicly provides a number of cloud traces. We focus on a 2019 trace containing a representative subset of Azure VM workloads (Microsoft Azure, 2019).

The dataset spans 30 consecutive days and covers over two million VMs. It is an unbalanced panel with 5-minute CPU utilization readings totaling nearly 1.25 billion measurements from more than five thousand users. Key variables include sanitized user, VM, and deployment IDs; timestamps in seconds that are recorded every 5 minutes; indicators for VM creation and deletion; the number of VMs created; deployment size; CPU utilization statistics (maximum, minimum, average, and 95th percentile); VM virtual core count; and requested VM memory in GB.

# C Additional Details on Productivity Measurement

In this Appendix, we first provide a formal definition of our compute productivity measure. Then, we provide some conditions under which compute productivity can be interpreted as factor-augmenting productivity in a full production function.

# C.1 Formal Exposition of Compute Productivity

As in the main text, index firms by i, jobs by j, and days by t. Firm i assigns job j, which runs for  $h_{ijt}$  hours on day t, to VM  $v_{ij}$ . Each VM v is defined by a tuple (c(v), x(v)), where

 $c(v) \in C \subset \mathbb{N}$  is the number of cores of VM v and  $x(v) \in X$  denotes the VM's characteristics, which include the VM's machine series, memory, data center, and operating system.

On day t, we observe  $n_{ijt}$  snapshots of CPU utilization  $\{u_{ijst}\}_{s=1}^{n_{ijt}}$ . By multiplying the utilization with the capacity of the chosen machine, we get  $n_{ijt}$  snapshots of the load of each job:  $\{\ell_{ijst}\}_{s=1}^{n_{ijt}}$ , where  $\ell_{ijst} := u_{ijst}c(v_{ij})$ . We assume that the load for each job is exogenous — that is, we take it as given that each firm must use the exact same amount of computing power that we observe them using in the data.

On each day, there is a set of VMs available for the firm to choose from. Let  $V_t$  be the set of VMs available on day t, and  $V_t(x) = \{v \in V_t : x(v) = x\}$  be the set of VMs available on day t that have characteristics x. We also define the outside option "VM"  $v_0$  as the 0-core VM that represents not running a job. Similar to the load, we assume that the characteristics x(v) of a VM are exogenous, and we take it as given that the firm chose these correctly. Therefore, we infer the choice set of firm i for job j on day t to be  $V_{ijt} = V_t(x(v_{ij})) \cup \{v_0\}$ .

We compare the firm's provisioning decision  $v_{ijt}$  with the decision of a hypothetical cost-minimizing firm  $v_{ijt}^*$ . To do so, we need to model the optimal provisioning process. For our baseline analysis, we assume the following:

**Assumption 1.** The cost-minimizing firm provisions based solely on the peak load of the VM, which we take to be the 95th percentile load over the period in which the VM is being provisioned.

**Assumption 2.** If a VM has a peak utilization of under 10% over a given time period, then the firm does not receive any benefit from that job over that time period.

**Assumption 3.** The cost-minimizing firm will downsize a machine only if the peak utilization on that machine would be less than 90%.

**Assumption 4.** After the initial provisioning decision, it is only worthwhile for a firm to change its provisioning decision if a VM is improperly provisioned over a seven-day period or longer.

As discussed in the main text, Assumption 1 is relatively standard, both in industry and literature definitions of improper provisioning. Assumption 2 is justified by a 10% peak CPU utilization being explainable by background processes of the CPU and not by any foreground processes run by the user. Assumption 3 comports with the rightsizing recommendations given by cloud providers to their clients. Finally, Assumption 4 is justified by firms facing sufficiently high switching costs from reconfiguring a job to a new type of VM.<sup>53</sup>

<sup>&</sup>lt;sup>53</sup>In practice, some major cloud providers have processes to reprovision running jobs to VMs of different sizes without any interruption in service. For example, see AWS—Resizing clusters. Thus, we view this assumption as conservative.

Let  $\mathfrak{T}_t^k = \{t, t+1, \ldots, t+k-1\}$  be defined as the set of k consecutive days starting with day t. Let  $\overline{\ell}_{ij}(\mathfrak{T}_t^k)$  be the peak load over  $\mathfrak{T}_t^k$ :

$$\overline{\ell}_{ij}(\mathcal{T}_t^k) = \max \left\{ \ell : \frac{\sum_{r=t}^{t+k-1} \sum_{s=1}^{n_{ijr}} \mathbf{1}(\ell > \ell_{ijsr})}{\sum_{r=t}^{t+k-1} n_{ijr}} \le 0.95 \right\}$$
(9)

Define the peak utilization  $\overline{u}_{ij}(\mathfrak{T}_t^k)$  analogously. Let T be the length of job j in days and, for ease of exposition, relabel the days so that job j lasts from day 1 to day T.

First, suppose  $T \ge 7$ . Given our assumption, the cost-minimizing firm's decision on each day t = 1, ..., T solves:

$$v_{ijt}^{*} = \arg\min_{v \in V_{ijt}} c(v)$$
s.t. 
$$\min_{r \in \{\max\{1, t-6\}, ..., \min\{t, T-6\}\}} \overline{\ell}_{ij}(\mathfrak{T}_{t-r}^{7}) \mathbf{1}(\overline{u}_{ij}(\mathfrak{T}_{t-r}^{7}) \le 0.1) \le c(v) - 0.1 \cdot \mathbf{1}(v \ne v_{ij})$$
(10)

It is easiest to interpret the constraint of expression (10) in words. The left-hand side of the constraint searches over all of the sets of seven consecutive days that include day t. If day t is part of a seven-day stretch in which the peak utilization is under 0.1, then it is idle, the left-hand side of the constraint will evaluate to zero, and any VM will cover the load over those seven days. In this case, the cost-minimizing firm will choose to deprovision the job, i.e., select  $v_{ijt}^* = v_0$  for those seven days. Otherwise, firm i will take the smallest VM that will cover the peak utilization of job j over a seven-day stretch that includes day t. This will always include as a possibility the actual VM that the firm chose,  $v_{ij}$ , but could include a smaller VM if the VM is downsizable (there exists a smaller VM with the same characteristics) and the peak load over the seven-day period is small enough to be covered by this smaller VM with at most a peak utilization of 90%. If this indeed is the case, then  $v_{ijt}^* \neq v_{ij}$  and we say that job j is overprovisioned over those seven days. In practice, because the number of cores in a given VM nearly always scales by powers of two, a VM will be overprovisioned if a smaller VM exists and its 95th percentile CPU utilization over a seven-day period is under 45%.

For VMs that are shorter than seven days (T < 7), we evaluate only the initial provisioning decision and do so over the entire length of the VM. That is, the cost-minimizing firm's provisioning decision solves

$$v_{ijt}^* = \arg\min_{v \in V_{ijt}} c(v) \quad \text{s.t.} \quad \overline{\ell}_{ij}(\mathfrak{I}_1^T) \mathbf{1}(\overline{u}_{ij}(\mathfrak{I}_1^T) \le 0.1) \le c(v) - 0.1 \cdot \mathbf{1}(v \ne v_{ij})$$
 (11)

As discussed in the main text, the final productivity measure  $\omega_{ijt}$  is the ratio between

resource usage of the cost-minimizing firm and firm i's actual resource usage on job j on the day t:  $\omega_{ijt} = c(v_{ijt}^*)/c(v_{ij})$ .

#### C.2 Microfoundation as Factor-Augmenting Productivity

We note that while  $\omega_{ijt}$  is fundamentally a measure of how effectively firm i solves a cost minimization problem, holding output fixed, it also has an interpretation as traditional factor-augmenting productivity.

Suppose that firm i produces a single product sold at an exogenous price normalized to 1. For ease of exposition, suppose the firm only uses compute for one job j. Let the firm's production function at a given moment in time s be  $f_{is}(\ell_{ijst}, z)$ , where  $\ell$  is compute load and z are other inputs that are assumed fixed in the short run. Assume the price of compute is linear in the amount of compute used with price p. Further, let the time length of each moment s be h hours. Then, the firm solves:

$$\max_{\{\ell_{ijst}\}_s, v} \sum_s f_{is}(\ell_{ijst}, z) - phc(v) \quad \text{s.t.} \quad v \text{ satisfies the constraint of (10)}.$$
 (12)

For a given path of compute load  $\{\ell_{ijst}\}_s$ , denote the cost-minimizing firm's choice of VMs as  $v_{iit}^*$ .

Now suppose that firm i choosing VM  $v_{ij}$  results in compute productivity  $\omega_{ijt}$  on day t. The definition of  $\omega_{ijt}$  implies that

$$\frac{p}{\omega_{ijt}}hc(v_{ijt}^*) = phc(v_{ij}). \tag{13}$$

As such, firm i's profits on day t are given by

$$\sum_{s} f_{is}(\ell_{ijst}, z) - phc(v_{ij}) = \sum_{s} f_{is}(\ell_{ijst}, z) - \frac{p}{\omega_{ijt}} hc(v_{ijt}^*).$$
(14)

As shown in Appendix A of Demirer (2022), this formulation of  $\omega_{ijt}$  is equivalent to factor-augmenting productivity because  $\omega_{ijt}$  scales the input price for compute.

#### D Additional Details on Estimation

This appendix provides the details of the estimation procedures used in the main text.

#### D.1 Details of Productivity Estimation

We use the following procedure to implement the compute productivity measures presented in Section 4. First, for each possible VM configuration (a combination of VM

series, data center, operating system, memory, and cores) a firm could choose, we evaluate whether that configuration is downsizable on each day (another VM configuration of the same family, data center, operating system, and memory, but half the number of cores is available on that day). We also evaluate whether the configuration is *twice downsizable*, which is defined as there existing a VM that the configuration could be downsized to that is itself downsizable. As discussed in the main text, cores scale in powers of two; therefore, if a VM is twice downsizable, this means there exists a VM with the same machine family, data center, operating system, and memory that has a quarter of the number of cores.

Second, for each VM on each day, using the daily inverse utilization CDF, we compute the peak (95th percentile) CPU utilization for all seven-day streaks that include that day. For VMs that last for fewer than seven days, we compute the peak CPU utilization over the life of the VM. We then assign the productivity measure  $\omega_{ijt}$  to each VM-day using the following hierarchical definition:

- 1. If a VM-day is part of a seven-day streak with a peak CPU utilization lower than 10%, it is idle and assigned a value of  $\omega_{ijt} = 0$ .
- 2. Else if a VM-day is part of a seven-day streak with a peak CPU utilization lower than 20% AND the VM configuration is twice downsizable, it is overprovisioned, with the correct configuration being a VM that is a quarter the size and assigned a value of  $\omega_{ijt} = 0.25$ .
- 3. Else if a VM-day is part of a seven-day streak with a peak CPU utilization lower than 45% AND the VM configuration is downsizable, it is overprovisioned, with the correct configuration being a VM half the size, and assigned a value of  $\omega_{ijt} = 0.5$ .
- 4. Else a VM-day is properly provisioned and assigned a value of  $\omega_{ijt} = 1$ .

Once we have defined the productivity of a VM-day  $\omega_{ijt}$ , we proceed by calculating the firm-month level productivity estimates using the aggregation given in Equation (1). This constitutes our baseline productivity measure that is used throughout the main text. In addition to these firm-month level estimates, we also calculate (i) firm, (ii) unit, (iii) unit-month, (iv) unit-month-VM product and (v) firm-month-VM product level.<sup>54</sup> These measures use the same formula as given in Equation (1)

$$\omega_{im} = \frac{\sum_{j \in J_{im}} \sum_{t} \omega_{ijt} c h_{ijt}}{\sum_{j \in J_{im}} \sum_{t} c h_{ijt}}$$
(15)

<sup>&</sup>lt;sup>54</sup>A VM product is a unique combination of VM series, data center, and operating system.

but instead of summing over the jobs used by the firm i in a given month m, it sums over the corresponding level of aggregation. For example, to calculate firm-month-VM product level productivity, we aggregate all  $\omega_{ijt}$  of the VMs that are used by the firm for a given VM product.

We also define alternative variables that decompose productivity from idleness and from overprovisioning separately. To study idleness, we define a dummy variable  $y_{ijt}^{idle} = \mathbf{1}(\omega_{ijt} = 0)$ , while to study overprovisioning, we use an indicator for whether the VM is overprovisioned  $y_{ijt}^{overprov} = \mathbf{1}(\omega_{ijt} \in (0,1))$ . We follow the analogous procedure to compute core-hour weighted averages of each firm's idleness inefficiency  $y_{im}^{idle}$  and overprovisioning inefficiency  $y_{im}^{overprov}$ . To remove the negative mechanical correlation between these two variables, we estimate a firm's overprovisioning inefficiency excluding all idle observations; that is, overprovisioning inefficiency will be the share of VMs that are overprovisioned, conditional on not being idle. Before analysis, we compute "idleness productivity" as  $\omega_{im}^{idle} = 1 - y_{im}^{idle}$  so that higher values continue to correspond to more efficient usage, and similarly for  $\omega_{im}^{overprov} = 1 - y_{im}^{overprov}$ .

We also calculate all of our productivity measures controlling for time- and machinevarying factors using fixed effects by regressing  $\omega_{ijt}$  on a fixed effect that is either at the firm, firm-month, firm-month-VM product, unit, unit-month, or unit-month-VM product level. These regressions use the following estimating equation (here, for firm-month level productivity):

$$\omega_{ijt} = \omega_{im} + Z'_{it}\beta + \varepsilon_{ijt}. \tag{16}$$

Here,  $Z_{jt}$  are the controls, and  $\omega_{im}$  are the firm-month-level productivity estimates as fixed effects. In these regressions, we weigh each observation by core-hours in order to properly account for the resources used by each VM on each day. Our baseline estimates in Equation (16) correspond to a regression with no controls since the resulting fixed effects simply represent the weighted average of the dependent variable. We run these regressions controlling for (i) day-of-week fixed effects and an indicator for whether there is a holiday in the region on the given date; (ii) day-of-week plus holiday plus machine family fixed effects; (iii) day-of-week plus holiday plus machine family interacted with data center region fixed effects; and (iv) day-of-week plus holiday plus VM product fixed effects. Results with these alternative levels of controls are located in Appendix H. We also use  $y_{ijt}^{idle}$  and  $y_{ijt}^{overprov}$  as dependent variables and convert the resulting fixed effects to idleness productivity and overprovisioning productivity by subtracting the fixed effects from 1 as above.

<sup>&</sup>lt;sup>55</sup>For the firm-month-VM product and unit-month-VM product regressions, the final three sets of controls are extraneous because they are nested by VM product.

In these regressions, a location normalization is to be made — one can add and subtract a constant from two different fixed effect levels and arrive at the exact estimates for all units. Our normalization is to make the average productivity according to each of these fixed effect regressions equal to the average productivity without controls. Finally, for all the alternative controls, we verify that the controls form a connected set, and therefore, the fixed effects resulting from the estimation procedure are directly interpretable and comparable with one another.

## D.1.1 Two Examples of Productivity Calculations

Table OA-1 presents usage data from two VMs in our sample to help describe how we compute our productivity estimates at the VM-day level. For each VM on each day, we display the amount of time in hours the VM was active, the core-hours used by that VM, and relevant selections from the inverse CDF of the VM's CPU utilization: the fraction of recordings the VM was less than 10% utilized, 20% utilized, and 45% utilized respectively. We also display  $\omega_{ijt}$ —the productivity we assign to each VM-day—which is a function of the shown columns.

Panel A displays a 4-core general-purpose Linux VM that is active over a three-day period. This VM's usage is volatile: it is highly utilized on the day it is created, as it is above 45% utilization approximately 5/6 of the time, but is essentially unused thereafter, spending nearly all its time under 10% utilization. However, since this VM is shorter than seven days, what matters for our productivity assignment is the total distribution of CPU utilization over the entire life of the VM, displayed in the bottom row. Because the peak utilization of this VM is above 45%—i.e., the value of the inverse CDF at 45% is under 0.95—this VM is marked as properly provisioned for its entire life, with  $\omega_{ijt}=1$  on every day.

Panel B displays an 8-core memory-optimized Linux VM that is active over a 10-day period. 2- and 4-core memory-optimized VMs with the same amount of memory and the same operating system were available in the same data center throughout this time period; therefore, this VM is twice downsizable. Because this VM is active for longer than seven days, the relevant distributions for assigning VM-day productivity are the running seven-day totals displayed in the bottom panel. Over days 1-7, the peak CPU utilization of the VM was above 20% (as the inverse CDF value at 20% was under 0.95) but below 45% (as the inverse CDF value at 45% was above 0.95). While this implies that the VM was

<sup>&</sup>lt;sup>56</sup>Though we do not show the remainder of the columns, our data include the inverse CDF in 5 percentage point increments. The only points on the inverse CDF that are relevant for our procedure are the ones displayed in the table.

**Table OA-1:** Example of CPU Utilization Data from Two VMs

			Share of CPU util recordings below X%				
Day	Hours active Core-hor		10%	20%	45%	$\omega_{ijt}$	
		Panel A:	VM 1 (3 d	lays)			
1	20.97	83.87	0.158	0.158	0.167	1	
2	24	96	0.985	0.996	1.000	1	
3	23.67	94.67	0.984	0.996	1.000	1	
Total			0.737	0.745	0.750		
		Panel B:	VM 2 (10 a	days)			
1	16.33	130.67	0.778	0.894	0.995	0.5	
2	24	192	0.304	0.485	0.996	0.5	
3	24	192	0.477	0.602	1.000	0.5	
4	24	192	0.996	1.000	1.000	0	
5	24	192	0.996	1.000	1.000	0	
6	24	192	0.992	1.000	1.000	0	
7	24	192	0.951	0.996	1.000	0	
8	24	192	0.964	0.996	1.000	0	
9	24	192	0.872	0.996	1.000	0	
10	21.03	168.27	0.991	1.000	1.000	0	
				7-day totals			
1-7			0.786	0.853	0.999		
2-8			0.811	0.868	0.999		
3-9			0.893	0.942	1.000		
4-10			0.966	0.998	1.000		

*Notes*: This table displays selected points from the inverse CDF of CPU utilization for two VMs in our data. VM 1 is a downsizable 4-core general-purpose Linux VM. Although it is rarely used on its second and third days of activity, its usage on the first day is enough such that it is marked as properly provisioned. VM 2 is a twice downsizable 8-core memory-optimized Linux VM. Its usage patterns result in being marked as overprovisioned on its first three days of usage and idle on its fourth through tenth days of usage.

not idle over this seven-day period, and the firm could not have downsized the VM to a 2-core machine, they could have downsized it to a 4-core machine and been under 90% utilization. Therefore, this 7-day streak is marked as (once) overprovisioned. By similar logic, the 7-day streaks starting on days 2 and 3 are also marked as overprovisioned. However, in the last seven days, the VM is active—days 4-10—the peak utilization of the VM is under 10%, meaning the VM is idle for these seven days. Thus, all days between 4-10 are assigned a productivity of  $\omega_{ijt}=0$ , as they are part of a 7-day period where the VM is marked as idle. Days 1-3 are not part of such a period, but they are each part of 7-day periods where the VM is marked as (once) overprovisioned, so they are assigned  $\omega_{ijt}=0.5$ .

## D.2 Details of Dispersion and Persistence Estimation

This section provides the details of the estimations presented in Table 3.

## D.2.1 Dispersion

In our dispersion analysis reported in Panel A, we employ firm-month level compute productivity estimates as detailed in Section D.1. We restrict our sample to firms with an average of at least 50 VM-day observations per month, ensuring that only firms with precisely estimated productivity levels are included. Column (1) reports statistics (mean, median, 90-10th percentile ratio, interquartile range, and  $R^2$ ) computed from the firmmonth data without any controls. For Columns (2)–(4), we calculate the same statistics within each reported group—namely by industry, month, and industry-by-month. We then calculate a weighted average of each statistic across these groups, using the number of firms in each group as weights. This approach prevents smaller industries with fewer firms from disproportionately influencing the overall statistics.

## D.2.2 Within-Firm Decomposition

In our within-firm decomposition analysis reported in Panel A, we estimate the variance explained by within-firm and between-firm heterogeneity as follows:

$$Var(\omega_{im}^{k} - \bar{\omega}_{m}) = Var(\omega_{im}^{k} - \bar{\omega}_{im}) + Var(\bar{\omega}_{im} - \bar{\omega}_{m})$$

where i denotes firm, k denotes unit, and m denotes month.  $\bar{\omega}_m$  denotes the mean productivity in month m and  $\bar{\omega}_{im}$  is the mean productivity of firm i in month m.

To implement these decompositions, we use a regression analysis and obtain the adjusted  $R^2$  from regressions. Specifically, for the within-firm decomposition, we regress unit-level productivity on firm fixed effects and take the  $R^2$  from that regression as the between-firm component. We repeat the same exercise while including the controls reported in Columns (2-4) of Table 3. For these specifications, the goal is to quantify the variance explained by firm fixed effects in unit-level variance after taking out the variance explained by the control variables. We implement this by first running the fully saturated regression with the control variables and recording the resulting  $R^2$  as  $R_0^2$ . Here,  $1 - R_0^2$  quantifies the remaining variance after including the control variables. Then, we include firm fixed effects by interacting them with the control variables and record the resulting  $R^2$  as  $R_1^2$ . To find the variance explained by between-firm variation, we calculate  $(R_1^2 - R_0^2)/(1 - R_0^2)$ .

## D.2.3 Within-Firm-Between-Region Decomposition

In our within-region across-region decomposition analysis reported in Panel A, we decompose the within-firm variance as follows:

$$\operatorname{Var}(\omega_{im}^k - \bar{\omega}_{im}) = \operatorname{Var}(\omega_{im}^{kr} - \bar{\omega}_{im}^r) + \operatorname{Var}(\bar{\omega}_{im}^r - \bar{\omega}_{im})$$

where r denotes a region. For this analysis, we only use multinational firms, which are firms that have units in multiple geographic regions, classified as US, EU, and domestic.

The calculation of within- and between-region decomposition is similar to the within-firm decomposition. We restrict the sample to multinational firms and estimate the variance explained by region-fixed effects after accounting for firm-fixed effects as between components, with or without control variables specified in the table. Since this analysis quantifies the contribution of the region in explaining variance within a firm, industry controls are fully absorbed and, therefore, do not apply. Those values are labeled as "-" in the table.

#### D.2.4 Persistence

For persistence results in Panel B, we use the month-firm level data and regress the compute productivity measure  $\omega_{im}$  on 1-month, 1-year, and 5-year lagged values separately for overall productivity, idleness productivity, and overprovisioning productivity. Results in Columns (2-4) run the same regressions by adding the corresponding control variable specified in the column title to the regression. In these regressions, standard errors are clustered at the firm level. We report the results for the overall productivity in Table 3 and idleness and overprovisioning productivity in Table OA-6.

#### D.3 Details of Learning Estimation

In our learning analysis, we remove all firms with an average of fewer than 50 VM-days per month over the 2022-2023 timeframe.

## D.3.1 Cross-Sectional Learning Analysis

For the learning analyses that are based on cross-sectional variation (Figure 6, Figure 8(b) and Table 6, Panel A), we begin by computing firm-level productivity for a given time period by averaging each firm's productivity across months, weighted by core-hours. For Figure 6 and Table 6, Panel A, this includes July-September 2022; for Figure 8(b), this includes July 2022-June 2023. We compute each firm's experience as the number of months between their first cloud usage and the beginning of the sample period (July 2022).

We then compute statistics (means and quantiles) and run regressions unweighted across firms. The overall 90-10 percentile ratio in Figure 8(b) is taken from Table 3.

## D.3.2 Timeseries Learning Analysis

For the learning analyses that are based on within-cohort variation in productivity over July 2022-June 2023 (Figures 7 and 8(a) and Table 6, Panel B), we limit to a balanced panel of firms, i.e., firms that have usage in each month from July 2022 to June 2023, that started using the cloud in either June-July 2022, 2021, 2020, or 2019. For Figure 8(a), we only include firms that started using the cloud in June-July 2022 and classify them into five equally sized groups based on their productivity in July 2022. We then compute statistics unweighted across firms.

#### D.3.3 Power Law Estimation

For the power law estimation in Table 6, we regress log productivity on an intercept and log experience in months, given each of the samples described above. Experience is as of the end of the month—that is, a firm that started using the cloud in July 2022 has one month of experience in July 2022. We floor productivity by 0.01 before taking the log to avoid missing values.

#### D.3.4 Normalization and Standard Error Calculation

In several figures in this section, we normalize the productivity estimate for firms in each month by dividing them by the productivity estimate of a specific group of firms. In Figure 6, we normalize by the average productivity of firms in their first month; in Figure 7, we normalize by the average productivity of the June-July 2022 cohort in their first month; and in Figure 8(a), we normalize by the average productivity of the third quintile of initial productivity in their first month.

For plots with standard errors, we then compute the standard errors of the ratio between the productivity estimate of firms in a given month and the productivity estimate of firms in their first month using the delta method. In particular, suppose that  $\overline{\omega}_t$  is the expected productivity of firms that are t months old, and  $\sigma_t$  is the standard error. Using the delta method, a first-order approximation of  $\sigma_t^{\text{norm}}$ , the standard error of  $\overline{\omega}_t/\overline{\omega}_0$ , is:

$$\sigma_t^{\text{norm}} \approx \frac{1}{\overline{\omega}_0} \sqrt{\sigma_t^2 - \frac{2\overline{\omega}_t}{\overline{\omega}_0} \text{cov}(\overline{\omega}_0, \overline{\omega}_t) + \frac{\overline{\omega}_t^2}{\overline{\omega}_0^2} \sigma_0^2}$$
 (17)

To compute an estimated  $\widehat{\sigma}_t^{\text{norm}}$ , we plug in the estimated average productivities, along

with the estimated variances and covariances from the coefficient covariance matrix of regression of productivity on firm experience indicators. In this regression, standard errors are clustered by the firm; this implies a nonzero covariance across months in the first year in Figure 7. In Figure 6, the unit of observation is the firm, and therefore, the standard errors are computed using the empirical standard deviations, and the covariance in the estimates is assumed to be zero. The exception is when t=0, in which case we know that  $cov(\overline{\omega}_0, \overline{\omega}_0) = \sigma_0^2$ , and therefore this expression simplifies to  $\sigma_0^{\text{norm}} = 0$ .

## D.4 Details of Learning Decomposition Analysis

## D.4.1 Within-Firm Learning Decomposition

In our learning decomposition, we restrict our sample to the period from July 2022 to June 2023 to be able to calculate month-to-month productivity growth. Following Melitz and Polanec (2015), we decompose the log productivity change into five components specified in the main text: (i) within, (ii) across, (iii) cross, (iv) entry, and (v) exit. In some rare cases, firm or unit productivity in a given month is zero, reflecting that all VMs are idle. For those months, we set productivity to 0.01 so that we do not drop those observations when we take the logarithm. In other rare cases where a firm or unit does not have any usage in a given month but we observe usage afterward, we do not treat those months as entry and exit, but we impute the productivity of that unit from the previous month, and we set its core hours to zero. We also restrict the sample to firms with at least two units to be able to implement the decomposition.

We first implement the decomposition given in Equation (6) for each firm and calculate the five decomposition components. We then take an unweighted average of each component across firms or units within each firm experience group given in the x-axis of Figure 9(a): 0-1, 1-2, 2-3, 4-6, 7-9 and 10+ in years. The firm experience is measured as of the end of the sample, June 2023.

In the calculations of Figure 9(b), we first subset the data to firms that are more than three years old and have a unit that began using cloud computing in July 2022 and continued usage through June 2023. These units constitute our sample of new units within experienced firms, which are reported in red color. We then subset the units of these firms that started using cloud computing before July 2019 so that these units have at least three years of experience by July 2022, which are reported in black color. These units constitute our sample of experienced units. We then calculate the average productivity of these groups for each month from July 2022 to June 2023 and report the productivity levels by normalizing them relative to the productivity level of experienced units in July 2022.

## D.4.2 Within-Unit Learning Decomposition

The implementation of within-unit decomposition Figure 10(a) proceeds similarly to the within-firm decomposition. Instead of decomposing a firm's month-to-month productivity changes into unit-level components, we decompose a unit's month-to-month productivity into machine type components using the unit productivity estimates for each machine type. Here, a machine type corresponds to a combination of "VM series, data center, and operating system". We make this choice because these are the VM dimensions for which it is most likely learning to occur. This analysis is restricted to firms with multiple units so that the sample is consistent with the sample of within-unit decomposition. We also restrict the sample to the units that use multiple machine types to implement the decomposition.

The implementation of Figure 10(b) follows that of Figure 9(b) with one key distinction. Unlike firms and units—for which we observe the exact dates of entry and exit from the cloud—we lack separate data on when a firm/unit began using a particular machine type. Instead, we infer this information from the VM-level dataset by recording the first time a firm/unit uses a VM type. Since our 2022 data begins in July, we identify new machine types as those first used by a firm in August 2022. This approach may introduce small errors if a firm had used a machine series prior to July 2022 but did not use it in July 2022. However, such cases should be rare, and when they occur, they render our results more conservative. After identifying the first use date of a machine type, we proceed with the analysis as described in the previous paragraph.

## D.5 Details of CPU Utilization and Electricity Relationship Estimation

This section outlines our method of measuring the power consumption of VMs based on their utilization levels and provides background information on the power consumption characteristics of VMs.

One unique aspect of computing hardware is that it consumes a significant amount of electricity even when idle because it needs to maintain essential functions such as operating systems, network connections, and cooling systems (Meisner et al., 2009; Duan et al., 2015).<sup>57</sup> Therefore, understanding the relationship between utilization and electricity consumption is crucial for calculating the overall resource impact of productivity dispersion, as different types of computing inefficiencies (idleness and overprovisioning) result in different levels of inefficient electricity use.

We combine the public CPU utilization and power data provided by Google Cloud (GC)

<sup>&</sup>lt;sup>57</sup>Additionally, peripheral components like hard drives and power supplies continue to draw power, and the servers must remain in a ready state for quick activation.

to estimate the relationship between CPU utilization and power consumption. Appendix B.6 offers a detailed description of the datasets. First, we explain how we aggregate VM-level utilization information to the level at which power consumption is measured. Next, we outline the specifications used to estimate power consumption as a function of utilization and then present the results.

## D.5.1 Aggregating CPU Utilization from VMs by PDU

The GC cluster trace denotes each of the eight clusters contained in the data by a through h. When compressed, the full size of the cluster trace alone is nearly 2.6 terabytes. Therefore, in order to attenuate the computational burden of aggregating and merging the entire data, we focus on cluster a.

In Appendix B.6, we described the "task" as the unit of observation in the usage data of the cluster trace. Each task in the cluster trace is identified by an index relative to a *collection ID*. A collection is either a set of resources where jobs executing tasks run or stand-alone jobs submitted directly to the scheduler to run on a machine. Hence, the unique usage observation is identified by the pairing (collection ID, task ID).

Each PDU is uniquely associated with a cluster. Moreover, each PDU supplies power to a specific subset of physical machines within a cluster. Every task is scheduled on a single machine. As noted in Appendix B.6, CPU utilization (in terms of GCUs) is reported after being normalized. However, the normalizing factor is the same across all observations. Hence, for each 5-minute interval t and PDU p, we compute CPU utilization at the PDU level as

$$U_{pt} = \frac{\frac{1}{c}}{\frac{1}{c}} \cdot \frac{\sum_{m_{jt} \in \mathcal{M}(p,t)} \sum_{i \in m_{jt}} u_{i,m_{jt}}}{\sum_{m_{jt} \in \mathcal{M}(p,t)} \sum_{i \in m_{jt}} r_{i,m_{jt}}},$$
(18)

where c is the resource specific normalizing factor,  $\mathcal{M}(p,t)$  denotes the set of active machines belonging to PDU p at time t, i indexes the pair (collection, task) at t, and  $u_{i,m_{jt}}$  and  $r_{i,m_{jt}}$  are the used and requested CPU resources of i, respectively. Since c enters the reported measures linearly, it gets canceled out in the computation of  $U_{pt}$  to yield a CPU utilization measure in percentage terms.

#### D.5.2 Estimating the Relationship between CPU Utilization and Electricity Consumption

In the computer science and electrical engineering literature, researchers have estimated the relationship between CPU utilization and power consumption through a combination of regression analysis and experimental methods (Husain Bohra and Chaudhary, 2010;

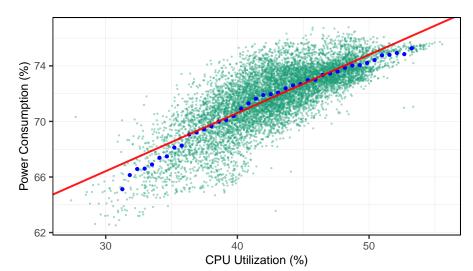


Figure OA-1: Relationship Between Power and CPU Utilization

*Notes:* This figure shows the estimated relationship between CPU utilization and power consumption for VMs. The scatter plot shows individual data points representing power consumption (%) as a function of CPU utilization (%) in 5-minute intervals. Blue points show binned scatter points, and the red line shows the regression line.

Kansal et al., 2010; Waßmann et al., 2013; Jiang et al., 2013). Experimental studies utilize machines with fixed characteristics and controlled computing environments to generate data on CPU utilization and power consumption.

In our paper, we will use a regression-based method to analyze the power consumption of VMs. In particular, we estimate the following regression model:

$$P_{pt} = \alpha + \beta \cdot U_{pt} + \varepsilon_{pt},$$

where  $P_{pt}$  represents the total power consumption of PDU p at time t. The intercept,  $\alpha$ , indicates the baseline power consumption when VMs are idle (i.e., zero CPU utilization), while the coefficient  $\beta$  measures the effect of a one percentage point increase in CPU utilization on power consumption. The term  $\varepsilon_{pt}$  captures the error. We estimate this model using 5-minute interval data on utilization and power consumption via ordinary least squares.

#### D.5.3 Results

Figure OA-1 displays the results from the regression of electricity usage on utilization along with a binscatter plot. The results reveal several noteworthy findings. We see that the relationship between power consumption and CPU utilization is approximately linear with a regression coefficient of 0.5, indicating that every percentage point (pp) increase in

utilization leads to a 0.5 pp increase in power consumption.<sup>58</sup>

In our sample, as can be seen from Figure OA-1, CPU utilization seldom falls outside the range of 30%-50%. This is because, in real-world cluster traces, we rarely observe VMs that consistently use 0% CPU. Therefore, the constant term in the linear model,  $\alpha$ , is estimated through extrapolation of the observed relationship to the utilization at 0% CPU. We estimate this term to be 0.5, which suggests that idle VMs consume about 50% of their full capacity electricity. This value is consistent with the experimental literature discussed above.

#### D.6 Details of Counterfactual Resource Calculations

This section details the counterfactual resource calculations described in Section 8. We first present the methodology for calculating core-hours usage under counterfactual productivity improvements and then detail the corresponding electricity calculations.

## D.6.1 Counterfactual Core-Hour Calculations

Our goal is to calculate the total core-hours that would be saved if all firms below the benchmark productivity level  $\omega_{im}$  reached the productivity level  $\bar{\omega}_{im}$ . For this exercise, we denote the counterfactual productivity  $\omega_{im}^c$  as:

$$\omega_{im}^c = \bar{\omega}_m^c \cdot 1(\omega_{im} < \bar{\omega}_m^c) + \omega_{im} \cdot 1(\omega_{im} \ge \bar{\omega}_m^c). \tag{19}$$

For brevity, we suppress the month subscript m as the time dimension is not important in this analysis. In this analysis, we need to calculate the total core-hours a firm would use if its productivity changes from  $\omega_i$  to  $\omega_i^c$ . This calculation is relatively straightforward because it does not depend on whether firms increase productivity through idleness or overprovisioning; the core-hours that would be saved will be the same regardless of the mechanism of improvements.

Let  $s_i$  denote the total core-hours used by firm i. We categorize these core-hours into three types of machine utilization patterns:

$$s_i = s_i^{id} + s_i^{op} + s_i^{pp} \tag{20}$$

where  $s_i^{id}$ ,  $s_i^{op}$ , and  $s_i^{pp}$  denote idle, overprovisioned, and properly-provisioned core-hours of firm i, respectively. Following the analysis in Section 4.1, we denote the output from

<sup>&</sup>lt;sup>58</sup>Although the relationship becomes nonlinear at the boundary of the utilization support, it is not precisely estimated due to a lack of data. Additionally, the line has to cross the point (1,1) by construction, supporting the linearity assumption.

these different types of VMs as  $y_i^{id} = 0$ ,  $y_i^{op} = 0.5s_i^{op}$ , and  $y_i^{pp} = s_i^{pp}$ ; thus,  $y_i = y_i^{id} + y_i^{op} + y_i^{pp}$  represents the total compute output. Let  $s_i^c$  denote the total core-hours needed for firms to produce the same output under the counterfactual productivity  $\omega_i^c$ . Therefore, we have:

$$\omega_i = \frac{y_i}{s_i}, \qquad \omega_i^c = \frac{y_i}{s_i^c}. \tag{21}$$

By taking the ratio, we can find  $s_i^c$  as:

$$s_i^c = s_i \frac{\omega_i}{\omega_i^c}.$$

This calculation shows that the mechanism by which firms achieve productivity gains does not affect the counterfactual calculations;  $s_i^c$  depends only on the level of counterfactual and factual productivity. By aggregating  $s_i^c$  across firms, we can calculate the total counterfactual core hours,  $s^c$  as:

$$s^c = \sum_i s_i \frac{\omega_i}{\omega_i^c}.$$

The total percentage of resource savings is given by the ratio between counterfactual and actual core-hours:

$$\Delta s = \frac{s - s^c}{s}.$$

## D.6.2 Counterfactual Electricity Calculations

This section describes the calculation of percent electricity savings under counterfactual productivity. Let  $s_{ij}$  denote the core-hour of VM j, used by firm i, and let  $u_{ijt} \in [0, 1]$  denote the utilization at time t, which indicates a five-minute interval. Based on the relationship between utilization and electricity estimated in Section D.5, we assume that the relative power consumption related to CPU utilization according to the following form:

$$p_{ijt} = (0.5 + 0.5u_{ijt})k_{ij}^{max}, (22)$$

where  $k_{ij}^{max}$  represents the power consumption when VM j is utilized at 100%. This functional form assumes that when the VM is idle, the power consumption is 50% of maximum power consumption and then increases linearly as utilization increases.

We further assume that  $k_{ij}^{max} = k \cdot c_{ij}$ , where  $c_{ij}$  is the number of cores of VM j. This assumption is reasonable because the computation power required for a VM typically

increases linearly with the number of cores. We further normalize k=1 as we are interested in percent savings relative to observed baseline consumption.

The functional form in Equation (22) is particularly convenient because additivity is preserved under integration, meaning that the core hours of a VM and average utilization are sufficient statistics to calculate total power consumption. To see this, the power consumption of VM j during its duration is given by:

$$p_{ij} = \int p_{ijt} dt = \int (0.5 + 0.5u_{ijt})c_{ij} dt = 0.5c_{ij}T_{ij} + 0.5c_{ij} \int u_{ijt} dt$$
$$= 0.5(1 + \bar{u}_{ij})s_{ij}$$

where  $\bar{u}_{ij}$  is the average utilization of VM j,  $T_{ij}$  is its duration, and  $s_{ij} = c_{ij}T_{ij}$  is the total core-hours of VM j. Furthermore, we can aggregate this at the firm level as follows:

$$p_i = \sum_{j(i)} 0.5(1 + \bar{u}_{ij})s_{ij} = 0.5 \sum_{j(i)} s_{ij} + 0.5 \sum_{j(i)} \bar{u}_{ij}s_{ij}$$
$$= 0.5s_i + 0.5\bar{u}_i s_i$$

where  $\bar{u}_i$  is the firm i's average utilization and j(i) is the set of VMs used by firm i. This form suggests that a firm's total power requirement depends on the number of core-hours they use and the average utilization. This makes counterfactual power calculations challenging because the change in the average utilization will depend on whether the firm reaches counterfactual productivity by improving idleness or overprovisioning.

To make progress, we introduce additional notation to separate efficiency gains from changes in idleness and over-provisioning. Let  $s_i^{id,c}$ ,  $s_i^{op,c}$ , and  $s_i^{pp,c}$  denote the counterfactual idle, overprovisioned, and productive core-hours respectively, and  $\Delta s_i^{id} = s_i^{id} - s_i^{id,c}$ , similarly for other utilization types. We have that:

$$\frac{s_i^{pp} + 0.5s_i^{op}}{s_i} = \omega_i, \qquad \frac{s_i^{pp,c} + 0.5s_i^{op,c}}{s_i^c} = \omega_i^c.$$
 (23)

Moreover,

$$s_i^{pp} + 0.5s_i^{op} = s_i^{pp,c} + 0.5s_i^{op,c}$$
 (24)

since we require the counterfactual core-hours to produce the same observed output. This

implies that:

$$\Delta s_i^{pp} = -0.5 \Delta s_i^{op}.$$

Therefore, an X core-hours reduction in overprovisioned VMs should add X/2 core-hours of properly-provisioned VMs. Using Equations (23) and (24), we also obtain:

$$\frac{s_i^{pp} + 0.5s_i^{op}}{s_i} = \omega_i, \qquad \frac{s_i^{pp,c} + 0.5s_i^{op,c}}{s_i - (0.5\Delta s_i^{op} + \Delta s_i^{id})} = \omega_i^c.$$

where the denominator in the second equation specifies the total core-hours used under the counterfactual productivity. This gives:

$$0.5\Delta s_i^{op} + \Delta s_i^{id} = s_i \left( \frac{\omega_i^c - \omega_i}{\omega_i^c} \right).$$

This provides an equation with two unknowns  $\Delta s_i^{op}$  and  $\Delta s_i^{id}$ , so it is not sufficient to identify  $\Delta s_i^{op}$  and  $\Delta s_i^{id}$  separately. We need another assumption to identify  $\Delta s_i^{op}$  and  $\Delta s_i^{id}$ . We make the following assumption:

$$\frac{s_i^{id} - \Delta s_i^{id}}{s_i^{id}} = \frac{s_i^{op} - \Delta s_i^{op}}{s_i^{op}} \qquad \Longrightarrow \qquad \frac{\Delta s_i^{id}}{s_i^{id}} = \frac{\Delta s_i^{op}}{s_i^{op}}.$$
 (25)

The underlying idea behind this assumption is that core-hour savings from each mechanism are proportional to the initial inefficiencies from each mechanism. Without additional information on how firms would reach counterfactual productivity, this assumption seems reasonable and assumes that firms split efforts equally between different mechanisms. Now, under the assumption given in Equation (25), one can compute  $\Delta s_i^{id}$  and  $\Delta s_i^{op}$  as follows:

$$\Delta s_i^{id} = s_i \left( \frac{\omega_i^c - \omega_i}{\omega_i^c} \right) \left( \frac{s_i^{id}}{s_i^{id} + 0.5 s_i^{op}} \right), \qquad \Delta s_i^{op} = s_i \left( \frac{\omega_i^c - \omega_i}{\omega_i^c} \right) \left( \frac{s_i^{op}}{s_i^{id} + 0.5 s_i^{op}} \right).$$

These equations provide the counterfactual values of idle, overprovisioned, and properly provisioned core-hours. We can calculate the average counterfactual utilization of firm *i* as follows:

$$\bar{u}_i^c = \bar{u}_i \frac{s_i}{s_i^c}.$$

Thus, we can calculate both factual and counterfactual firm-level power consumption:

$$p_i^c = 0.5s_i^c + 0.5\bar{u}_i^c s_i^c, \qquad p^c = \sum_i p_i^c.$$

The total power saving in the economy is given by:

$$\Delta p = \frac{p - p^c}{p}.$$

#### **E** Robustness Checks

This appendix provides the details of robustness checks summarized in Section 5.3.

#### **E.1** Robustness to Other Utilization Measures

In cloud computing, network and memory utilization are commonly monitored alongside CPU utilization to measure the performance and efficiency of VMs.

Network utilization refers to the amount of data being transferred in and out of a VM relative to its capacity. High network utilization reflects significant data traffic, while low utilization indicates minimal use of the available bandwidth. Memory utilization measures the amount of allocated memory actively being used by a VM relative to the total memory allocated to that VM.

In calculating our measure of computing productivity, we focus on CPU utilization because it is the most relevant metric in the industry, and the CPU is the most resource-intensive component of computing infrastructure. CPUs typically consume the majority of power in servers, making their efficient use crucial for minimizing energy consumption. By concentrating on CPU utilization, we align our analysis with industry practices and address the most significant aspect of resource management in cloud environments.

Still, one potential concern is that firms with high CPU utilization efficiency might underperform in memory or network resource usage, creating inefficiencies in other VM performance dimensions. To address this, we conduct a robustness check to verify that memory or network utilization patterns do not contradict our CPU utilization findings.

We have limited data on memory and network utilization, covering one-month periods in 2022 and 2023. Using these data, we estimate the correlation between CPU utilization and other utilization measures. The direction of this correlation is unclear in advance. Some jobs may be memory-intensive, using more memory and less CPU, while others may be compute-intensive, relying more on CPU than memory. This variation could result in a negative correlation between these utilization measures. Conversely, if a job is truly idle,

it would likely use neither memory nor CPU, potentially resulting in a positive correlation between the two measures.

In Figure OA-16, we report the correlation between utilization measures and find that CPU utilization is positively correlated with both network and memory utilization. This result suggests that firms identified as inefficient in terms of CPU utilization also tend to be inefficient in other dimensions of computing resource utilization.

#### **E.2** Robustness to Duration of Peak Utilization Measurement

As mentioned in Section 4.1 and detailed further in Appendices C.1 and D.1, we define productivity and inefficiency using peak VM utilization over a seven-day period. This approach ensures our measure remains conservative regarding potential costs associated with short-term provisioning adjustments, especially given the predictable volatility in load related to days of the week. Additionally, this definition aligns with the internal measures used by cloud providers.

However, one might be concerned about the sensitivity of our results to this choice. To address this, we re-estimate our productivity measures using alternative periods for calculating peak productivity: one-day, three-day, and 15-day intervals. We then repeat our analyses using these alternative productivity measures to verify that our primary findings are robust to these different definitions. Figures OA-11 and OA-14, as well as Table OA-7, present the outcomes of these robustness checks, which are broadly consistent with the results from our main specification.

## E.3 Robustness to Controlling for VM Characteristics

As explained in Section 4.1, we first estimate the productivity of individual VMs based on their idleness and overprovisioning, and then aggregate these measures to the firm level at different frequencies. In our main specification, we treat all VMs equally, simply summing their VM-level efficiencies to the firm level. One potential concern with this approach is that VMs may differ in characteristics that could influence utilization. We believe focusing on peak utilization mitigates this concern, as peak utilization is less sensitive to VM type. For example, memory-intensive or network-intensive workloads naturally exhibit lower average utilization because the CPU may spend idle time waiting for data transfers; however, such factors should not significantly impact peak utilization. Nevertheless, we conduct several robustness checks to confirm that our findings are not driven by differences in VM characteristics.

To account for these differences, as described in Appendix D.1, we aggregate VM-day-level productivity to the firm level using a weighted regression that controls for several

job characteristics, as follows:

$$\omega_{ijt} = \omega_{im} + \beta' Z_{jt} + \varepsilon_{ijt}.$$

This regression essentially estimates firm-month level fixed effects  $\omega_{im}$  while controlling for systematic productivity differences across VM types within various control bins.

Our first control includes day-of-week and holiday fixed effects to account for temporal variations in productivity differences. For example, if less productive firms, for unrelated reasons, tend to run jobs on weekends—and if weekend jobs are systematically less productive—this specification would accommodate such patterns. Our second control adds product fixed effects by interacting day-of-week and holiday fixed effects with VM configurations. We then gradually introduce additional controls, including machine fixed effects and region-by-machine fixed effects. These VM characteristics help account for potential differences arising from hardware specifications.

In these fixed-effect regressions, we can only compare firm fixed effects within a connected set (Abowd et al., 1999; Metcalfe et al., 2023). This means that firms must be directly or indirectly linked through the graph of firm-to-machine characteristics. In our context, due to the large number and variety of VMs used by firms, we either have all firms in one connected set or one large connected set covering more than 99% of firms, along with a few smaller sets consisting of firms that utilize only specialized VMs. Consequently, we can compare nearly all firms, even when controlling for detailed VM characteristics.

The results from these robustness checks are reported in Figure OA-10, Figure OA-13, and Table OA-6. The findings remain similar to our main specification, with the notable exception that controlling for VM characteristics reduces the magnitude of long-term learning in the cohort-by-cohort analysis. This reduction likely occurs because part of the observed learning arises from firms improving their choice of VM types, as documented in Section 7. Consequently, controlling for VM types captures this mechanism, reducing the estimated learning effect, particularly in the long run when VM types undergo significant changes over time.

#### E.4 Robustness to Compute Load Volatility Measures

One important identification threat in our analysis is that inefficiency might be rational if firms maintain idle capacity to handle volatile workloads, thus reducing the risk of hitting capacity constraints. Although we argue that, given the nature of cloud computing and available tools such as autoscaling, firms have no reason to maintain idle VMs, we nevertheless examine whether productivity measures correlate with key outcomes related

to load volatility and capacity constraints.

To address this concern, we compute the following volatility measures: (1) standard deviation; (2) coefficient of variation; (3) fourth moment; (4) tail event type 1, defined as the probability of experiencing a load greater than mean + 2×standard deviation; (5) tail event type 2, defined as the probability of experiencing a load greater than mean + 3×standard deviation; and (6) tail event type 3, defined as the probability of experiencing a load greater than mean + 4×standard deviation. In these calculations, the load refers to the firm's daily compute load, which is estimated by integrating the area under the CPU utilization curve.

We then regress firm-month level compute productivity on these measures of time-varying firm-level demand volatility. This regression suggests that demand volatility measures explain only 1.8% of the variation in firm productivity across firms.

## E.5 Robustness to Measurement of Downsizability

An important aspect of measuring compute productivity is the concept of downsizability: identifying alternative VMs that a firm could select if a VM is overprovisioned. When discussing downsizability in VMs, it is important first to establish the criteria for an appropriate substitute with fewer cores. A good substitute VM should maintain equivalent performance across all specifications, except having a reduced number of CPU cores.

Several key factors should be considered when defining a substitute VM. These are primarily memory, VM family, operating system, region, and data center. For example, the memory capacity should remain the same or be higher to ensure that the job can run in the alternative VM. The operating system should also remain the same to maintain software compatibility. Another less clear dimension is the VM family. VMs are different in many dimensions, including family, manufacturer, and series. In principle, the same job can be run on different hardware versions and even on hardware from different manufacturers. However, firms might prefer to maintain the same VM family for consistency, performance predictability, and ease of management.

Another critical factor when considering VM downsizing is a geographical region or data center. The location of the data center might be important as firms tend to choose data centers close to their customers or employees to reduce latency (Greenstein and Fang, 2020). Moreover, firms might prefer to use a particular data center because their data is stored there. Finally, regulatory compliance and data sovereignty requirements can dictate the need for specific regional or data center locations.

Given these factors, we define various levels of downsizability. In each measure, we maintain the constraint that the alternative VM should have the same memory and

operating system while allowing for variations in VM family and location.

- "Data Center-Machine Series-OS-Memory" Downsizing: This is the most restrictive measure, requiring VMs to be in the same data center, VM type, and series, with identical OS and memory.
- "Region-Machine Series-OS-Memory" Downsizing: This variation relaxes the data center requirement to the regional level while maintaining other restrictions.
- "Region-Machine Family-OS-Memory" Downsizing: This measure allows for different machine series within the same region, family, OS, and memory specifications.
- "Region-OS-Memory" Downsizing: This variation permits downsizing across different machine families within the same region, maintaining OS and memory consistency.
- "OS-Memory Downsizing": The least restrictive measure, allowing downsizing across different regions, only requiring the same OS and memory specifications.

In our baseline specification, we choose "Region-Machine Family-OS-Memory Down-sizing" to balance the need for consistent performance with the flexibility of using different machine families within the same region. However, we also conduct robustness checks using other downsizability measures to ensure the robustness of our findings. The results for these robustness checks are given in Table OA-8.

# E.6 Correlation Between Idleness and Overprovisioning Productivity

In this robustness check, we analyze the relationship between idleness and overprovisioning productivity. A positive relationship between these two productivity measures would suggest that inefficiency is not driven by a particular mechanism that generates only one type of inefficiency. For example, one explanation for inefficiency could be that a firm's workload is volatile, so firms overprovision to ensure they can meet additional demand. However, this explanation is less likely to account for idleness because an efficient firm could easily manage volatility across VMs using available tools.

For this robustness check, we regress overprovisioning productivity on idleness productivity using firm-month-level data, controlling for industry and time fixed effects. This regression yields a coefficient of 0.064 with a standard error (clustered at the firm level) of 0.004, suggesting that firms with idle VMs also tend to have overprovisioned VMs. This result indicates that underlying factors driving inefficiency in computing lead simultaneously to both idleness and overprovisioning, providing evidence that inefficiency does not originate from a single source.

## E.7 External Validity: Relationship Between Productivity and Firm Exit

There is an extensive literature demonstrating that less productive firms are more likely to exit (Foster et al., 2016). Although we do not observe actual firm exits, we can conduct a similar analysis by examining the relationship between a firm's compute productivity and its probability of leaving the cloud. It is important to note that our measure of exit captures only when a firm leaves our specific cloud provider and does not necessarily indicate that the firm stops using cloud services entirely, as it might switch to another provider. Nevertheless, this interpretation remains consistent with the intent of our analysis: firms with lower productivity at our cloud provider are more likely to exit that provider.

This result also provides evidence against the demand volatility hypothesis for productivity dispersion. Cloud computing is particularly advantageous for firms that experience significant demand volatility. If demand volatility were the primary driver behind low productivity, we would expect that low-productivity firms, which benefit most from the cloud's flexibility, would be less likely to exit.

## E.8 External Validity: Dispersion in Publicly Available CPU Utilization Data

We use publicly available CPU utilization datasets, described in Appendix B, to assess the external validity of our findings. These datasets consist of short panels and lack user-specific information, limiting our analysis to only productivity dispersion.

The datasets, sourced from Google Cloud and Microsoft Azure, differ from our primary data in both structure and duration. Therefore, we provide detailed explanations of how we construct the samples used for productivity analysis in each dataset. In processing both traces, we either directly apply the assumptions used in cleaning our primary data or select observations that closely resemble the operational focus of our analysis.

## E.8.1 Azure Cloud Trace

The 2019 Azure dataset provides one month of VM utilization data and characteristics. Regarding utilization, we observe average and maximum CPU utilization recorded at five-minute intervals throughout the VM's lifetime. For VM characteristics, we have data on the number of requested cores and amount of memory, as well as timestamps indicating when each VM was created and deleted. Additionally, the dataset includes a "machine category" variable that describes whether a VM is "delay insensitive," "interactive," or "unknown."

As expected, we observe core and memory levels that primarily scale by factors of two. For cores, we observe request levels of 2, 4, 8, 16, and 30. For memory, we observe request levels of 2, 4, 8, 32, 64, and 70 gigabytes. As in the main text, we define downsizeability

in terms of cores for a given set of VM characteristics. Specifically, given a VM's memory request level and machine category, the VM is considered downsizeable if there exists another VM with the same memory and category but with half as many cores. This definition slightly differs from our main downsizeability definition, as we lack certain VM features in the Azure data, such as VM series and data center region. Additionally, consistent with our main analysis, we measure productivity based on the 95th percentile of maximum CPU utilization.

Before computing productivity, we clean the trace data following the same sampling procedures used for our primary dataset. Specifically, we drop all users who are observed with fewer than 10 VMs throughout the trace period, resulting in a loss of 2.8% of users. Additionally, we remove VMs with lifetimes of less than 20 minutes, eliminating approximately 39% of the available VMs in the data. The final sample contains resource usage information from 3,503 users operating a total of 1,632,952 VMs.

Next, for VM j of user i on day t, we define a productivity measure  $\omega_{ijt} \in [0,1]$ , consistent with the definition provided in Section 4. Using this measure, we aggregate VM-level productivity to obtain user-day-level productivity. Specifically, the productivity for user i on day t across the set of VMs  $J_{it}$  is defined as follows:

$$\omega_{it} = \frac{\sum_{j \in J_{it}} \omega_{ijt} c h_{ijt}}{\sum_{j \in J_{it}} c h_{ijt}},$$
(26)

where  $ch_{ijt}$  is the core-hours of job j on day t. Unfortunately, the Azure trace only contains timestamps in seconds, and it is unknown when the trace began. Hence, we have no mapping between timestamps and particular dates. Thus, we determine the days where observations fall to be the modulus of the timestamp divided by the number of seconds in a day.

Appendix Figure OA-17(a) shows the distribution of user-day-level productivity throughout the duration of the Azure trace. There is a notable concentration at the productivity level of one-half, primarily due to the relatively small sample size in the data. Nonetheless, both the dispersion and the overall distribution of productivity are broadly similar to our main results shown in Figure 3.

## E.8.2 Google Cluster Trace

Similar to the Azure trace, the cluster data provided by GC traces one month of CPU usage and characteristics from May 2019. The Google cluster trace concerns cluster usage by jobs submitted by Google engineers and services (see Appendix Section B.6). We use the detailed information in the trace provided by GC to focus on jobs resembling the structure

of VMs as closely as possible.

As described in Appendix Section B.6, the task is the fundamental unit of observation in the usage data in this trace. Tasks are executed as instances of jobs that either run independently and directly on a physical machine or as part of a *alloc set*, which represent sets of fixed resources. In the GC trace, jobs and alloc sets are referred to as *collections*. For each collection, we observe whether auto-scaling is enabled and whether, if enabled, it is constrained. For this data, we take collections without auto-scaling enabled to be our VM-like objects. Henceforth, we will refer to these collections as VMs. We focus on these VMs because the provisioning decisions for CPU and memory are made by the user rather than the cluster manager. In this way, this subset of collections helps us focus on compute resources most similar to our sample and enables us to focus on user-made provisioning decisions.

The GC trace contains observations of nearly 5.2 million collections. Only for about 360,000 (6.8%) of these, the requested CPU capacity is fixed. Since these VMs run on a cluster, they start using compute resources when scheduled on a machine. Thus, we consider the lifetime of the VM as beginning at its scheduled time. We remove all collections that do not have an explicit scheduling event. This preserves 99.5% of the collections. We also know exactly when the trace started and ended, so we do not deal with the timestamp-to-date conversion difficulties as with the Azure trace.

Some VMs have multiple scheduling events observed. To the best of our knowledge, these cases correspond either to VMs that failed and were restarted or to VMs that were booted from a VM due to a higher-priority VM needing to be scheduled. For these kinds of VMs, we take the minimum scheduling event observed as the start time of the VM. As in the main text, we remove VMs with a lifetime of less than 20 minutes and all users with less than 10 VMs. This results in a sample of 24,909 VMs. While this is a small subset of all available collections, it was created so that the VM-like objects we analyze resemble the VMs in our data as much as possible.

In our data and the Azure trace, we observe core and memory requests that scale by a factor of two. This is not the case in this trace. Since our VMs are cluster jobs, they are able to request memory in terms of bytes rather than just gigabytes, and therefore, requests can differ at a much more granular level. Given the availability of provisioning resources at such a granular level, users are able to provision VMs efficiently at virtually any level of compute usage. Thus, we consider all VMs to be downsizeable, and hence, the productivity of a given VM will be solely based on its CPU utilization.

As in the main text, we define the productivity of the VM j of user i on the day t by the measure  $\omega_{ijt}$ . In this case,  $\omega_{ijt}$  is zero for VMs with CPU utilization under 10%, one-half

for VMs with between 10% and 45% utilization, and one for VMs with greater than 45% utilization. As normal, we consider the 95th percentile of maximum CPU utilization. With this, we aggregate VM level productivity to the user-day level using a similar notation as above:

$$\omega_{it} = \frac{\sum_{j \in J_{it}} \omega_{ijt} c h_{ijt}}{\sum_{j \in J_{it}} c h_{ijt}}.$$
(27)

Figure OA-17(b) presents the distribution of productivity calculated in Google Cloud. A few points to note: First, similar to Azure traces, we observe a mass at 0.5, coming from users with only over-provisioned resources. Second, we see that the productivity distribution is more skewed to the right than our main result in Figure 3. This is likely due to the fact that Google Cloud data only includes internal users or jobs of external customers implemented by Google engineers. It is likely that Google engineers are more productive than typical firms. However, despite this, we still see substantial productivity dispersion even in this sample, where productivity ranges from 0 to 1, with a substantial mass between 0.5 and 1.

## E.9 Long-Term Learning

Our primary dataset contains one consecutive year of data, from mid-2022 to mid-2023. Using these data, we characterize the productivity improvements of different cohorts over that year in Section 7. By comparing the productivity growth of different cohorts over that year, we are able to estimate long-term learning in a way that minimizes the amount of cross-cohort variation in our estimates. However, estimating learning over a period longer than a year using one year of data necessarily requires comparing the productivity growth of firms in different cohorts.

To address this problem, we can use our limited data from between 2017 and 2019 to estimate the productivity growth of a single cohort of firms over a longer period of time. To do so, we need enough data for one period to reliably estimate the productivity of a group of firms in their first month. Given the intermittency and timing of our data, the best opportunity to do so is in 2019, when we have a consecutive month of data that is at a similar time of year to the data at the end of our sample.

We find that firms that joined the cloud in mid-2019 have a 27.6% higher productivity at the end of our sample roughly four years later. While still providing clear evidence of learning, this estimate is lower than the 44.0% long-term productivity improvement that we find in our cohort analysis. This difference could be in part due to survivorship bias: we are able to condition on firms in the 2019 cohort we study surviving for four

years, whereas we can only condition on the June-July 2022 cohort surviving for one year, which—since exit is negatively correlated with productivity—implies a higher base rate of productivity for the 2019 cohort. Another reason could be differences across cohorts: firms that are initially more productive may join the cloud earlier, which reduces the scope of learning. Consistent with both interpretations, we find that the difference in estimates is driven in large part by differences in initial productivity: firms in the 2019 cohort that survive for four years have a 13.8% higher productivity in their first month than firms in the June-July 2022 cohort that survive for one year in their first month. Due to the sampling procedure applied to the raw data, we are unable to compare the unconditional distributions of firms in their first months across cohorts, which would help indicate which effect is more prevalent in this setting.

# F Additional Figures

Nachine family

Machine family

Machine family

Machine family

Machine Configuration

Machine Configuration

Figure OA-2: Explanatory Power of VM Characteristics in Productivity Dispersion

*Notes*: This figure displays adjusted  $R^2$  from a regression of VM-day level productivity on increasingly detailed levels of fixed effects. Fixed effects included in bars to the right always nest the fixed effects used in preceding (left) bars.

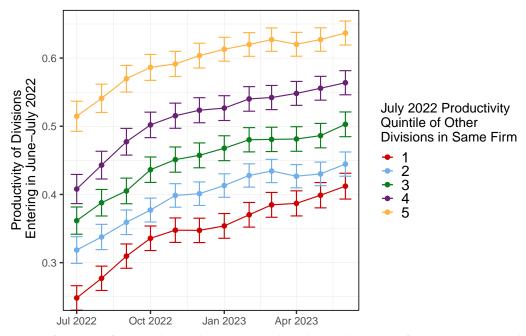
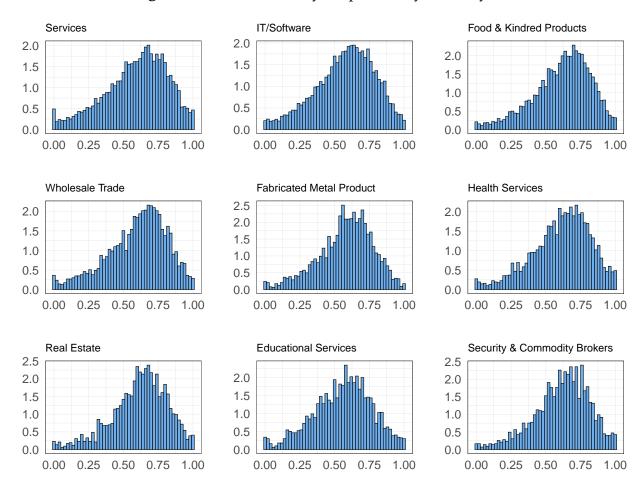


Figure OA-3: Productivity Trajectories of Units in Existing Firms

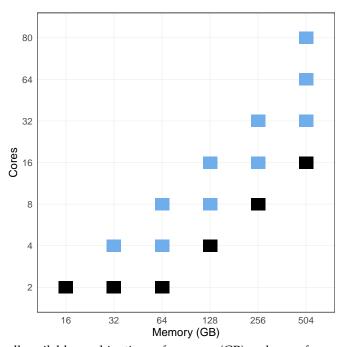
*Notes*: We group firms into five evenly sized groups based on the productivity of existing units in July 2022 and then plot the average productivity of the new units over time.

Figure OA-4: Productivity Dispersion by Industry



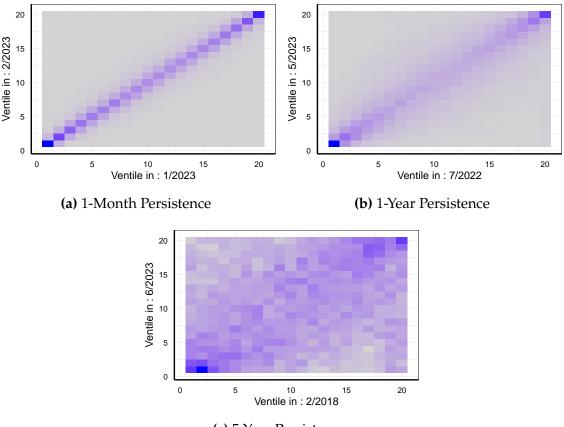
*Notes*: This figure displays the productivity distribution by industry, calculated in the same way as in Figure 3. Industry classification is based on 1-digit SIC codes.

Figure OA-5: Downsizability Example: Memory and Core Combinations



*Notes*: This figure displays all available combinations of memory (GB) and cores for one VM series from our data. Each point represents a specific VM configuration. The blue-colored points indicate downsizable machines, where an alternative VM exists with the same memory capacity but fewer cores.

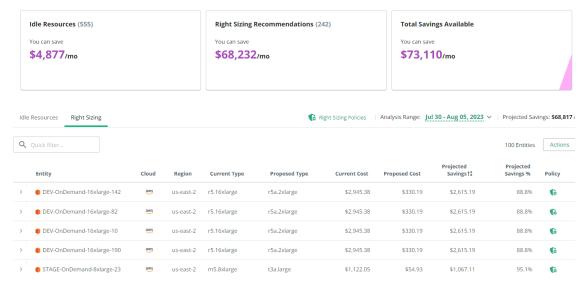
Figure OA-6: Persistence of Productivity in the Short, Medium, and Long Run



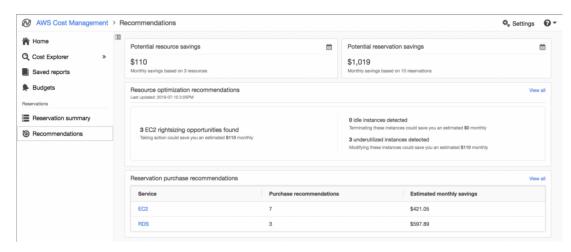
(c) 5-Year Persistence

*Notes*: This figure presents heatmaps illustrating productivity persistence across three different time horizons: (a) 1-month, (b) 1-year, and (c) 5-year. Each heatmap's axes are divided into 20 equally sized bins, representing the ventiles of the productivity distribution. The x-axis shows the ventile at the start of the period, while the y-axis shows the ventile at the end of the period. Each cell's color intensity corresponds to the frequency of firms moving from one ventile to another over the specified time horizon. Panel (a) depicts 1-month persistence from January 2023 to February 2023, panel (b) shows 1-year persistence from July 2022 to June 2023, and panel (c) illustrates 5-year persistence from 2018 to June 2023.

Figure OA-7: Examples of First- and Third-Party Cost Management Tools



(a) Virtana Cost Management Tool

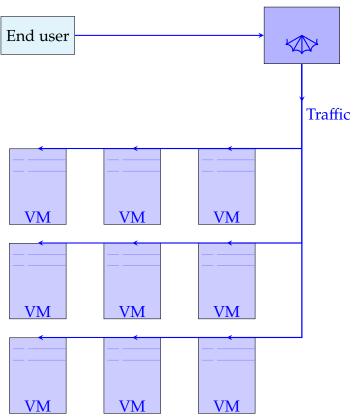


(b) AWS

*Notes*: This figure presents two examples of tools for detecting idleness and overprovisioning in cloud computing. Panel (a) shows a dashboard from cloud optimization startup Virtana, taken from Virtana Cloud Cost Management while Panel (b) displays the cost management interface of AWS, obtained from AWS Resource Optimization Recommendations.

Figure OA-8: Representation of Load Balancer

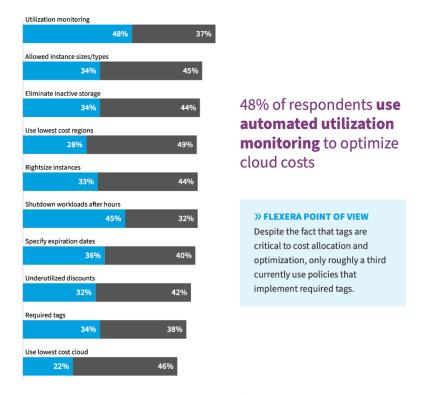
## Virtual load balancer



*Notes*: This figure illustrates a virtual load-balancing architecture in cloud computing. It depicts the flow of traffic from end users through a virtual load balancer, which then distributes the requests across multiple VMs. The load balancer directs traffic (indicated by a blue arrow) to three rows of VMs, each row containing three VMs. This architecture is designed to optimize resource utilization and improve system performance by efficiently distributing incoming requests across available compute resources.

Figure OA-9: Surveys About Cloud Optimization

# What types of policies do you use to optimize cloud costs?



#### (a) Survey Response to a Question about Cloud Optimization Tools



**(b)** Survey Response to a Question about Spending

*Notes*: This figure is a screenshot from a survey conducted by Flexera titled "State of the Cloud" (Flexera, 2023). It shows the responses to two questions asked in the survey. Panel (a) illustrates the types of policies companies use to optimize cloud costs, while Panel (b) displays the respondents' estimates of their wasted cloud spend.

## G Additional Tables

Table OA-2: List of Machine Families Offered by Major Cloud Providers

VM Family	AWS	Azure	GCP	
General Purpose	M5, T3	B-series, Dsv3-series	E2, N1, N2, N2D	
Compute Optimized	C5	Fsv2-series	C2	
Memory Optimized	R5, X1	Esv3-series, Mv2-series	M1, M2	
Storage Optimized	I3, D2	Lsv2-series	-	
GPU	P3, G4	NC-series, NV-series	A2	
High Performance	-	H-series	-	
Shared-core	-	-	f1-micro, g1-small	

*Notes*: This table summarizes the main families of virtual machines offered by Amazon Web Services (AWS), Microsoft Azure, and Google Cloud Platform (GCP). The categories are general and may not be exhaustive. Each provider offers multiple sizes and series within each family. "-" indicates that the provider doesn't have a direct equivalent or the information wasn't specified in the given context.

Table OA-3: Advertised Use Cases of Different Machine Families

VM Family Key Considerations		Ideal For			
General Purpose	Cost-effective, balanced CPU, memory, temporary storage	Web servers, application servers, development environments, small to medium databases			
Compute Optimized	High core counts, faster CPUs	Scientific computing, HPC, video editing, simulations			
Memory Optimized	Large RAM capacities	Databases, caching layers, in-memory analytics			
Storage Optimized	Local SSDs, high I/O performance	Large databases, data warehousing, Big Data analytics, real-time applica- tions			
GPU	Diverse GPU types and configurations	Machine learning, deep learning, video editing, scientific simulations			
High-Performance	Exceptionally high compute power, massive memory, ultra-fast storage	Scientific modeling, simulations, weather forecasting			

Source: www.cloudoptimo.com

 Table OA-4: First-Party Cloud Cost Optimization Tools

Cloud Provider	<b>Cost Optimization Tool</b>	Description
	AWS Cost Explorer	Interface to view costs, usage, and ROI for AWS services, with data for the past 13 months and forecasting capabilities.
AWS	AWS Budgets	Allows setting and enforcing budgets for AWS services, with notifications when budgets are exceeded or reached.
	AWS Trusted Advisor	Provides automated recommendations for cost optimization, including EC2 reserved instance optimization and idle resource identification.
	Amazon CloudWatch	Monitoring service that can set alarms based on metrics, commonly used for cost optimization by identifying underutilized resources.
	AWS Instance Scheduler	Automates starting and stopping of EC2 and RDS instances based on defined schedules to save costs.
	AWS Pricing Calculator	Estimates the cost of use cases on AWS, helping to model solutions and explore pricing points before deployment.
Azure	Azure Cost Management and Billing	Provides cost analysis, budgeting, and recommendations for cost optimization, integrated with Azure portal.
	Azure Advisor	Offers personalized best practices and recommendations to optimize Azure resources, including cost optimization.
	Azure Pricing Calculator	Helps estimate costs for Azure services and solutions, allowing users to model and forecast expenses before deployment.
GCP	Google Cloud Cost Management Google Cloud Pricing Calculator	Includes tools for cost visibility, budgeting, and recommendations to optimize cloud spending. Estimates costs for Google Cloud services, allowing users to model and forecast expenses before
	Google Cloud Recommender	deployment. Provides recommendations for cost optimization, including rightsizing VM instances and identifying idle resources.
	Google Cloud Budgets and Alerts	Allows setting budgets and receiving alerts when costs exceed predefined thresholds, integrated with Google Cloud Console.

*Notes*: This table summarizes the main cost optimization tools offered by Amazon Web Services (AWS), Microsoft Azure, and Google Cloud Platform (GCP).

Table OA-5: Relationship Between Firm Centralization and Compute Productivity

Indep. var.	(1)	(2)
HHI (0 to 1)	0.102	
	(0.007)	
HHI quartile 2		0.016
		(0.004)
HHI quartile 3		0.031
		(0.004)
HHI quartile 4		0.069
-		(0.005)

*Notes*: The coefficients in this table come from a regression where the dependent variable is productivity in 2022-2023, and each observation is a multi-unit firm. In regression (1), the independent variable is the firm's HHI of usage across all units, while in regression (2), there are independent dummy variables for four equally sized groups based on the firm's unit usage HHI (with the lowest HHI the omitted group). Both regressions control for industry (2-digit SIC) and cohort year fixed effects. Standard errors clustered by industry and cohort year in parentheses.

## **H** Robustness Results

sof Firms

0.5

0.0

0.0

0.4 Productivity

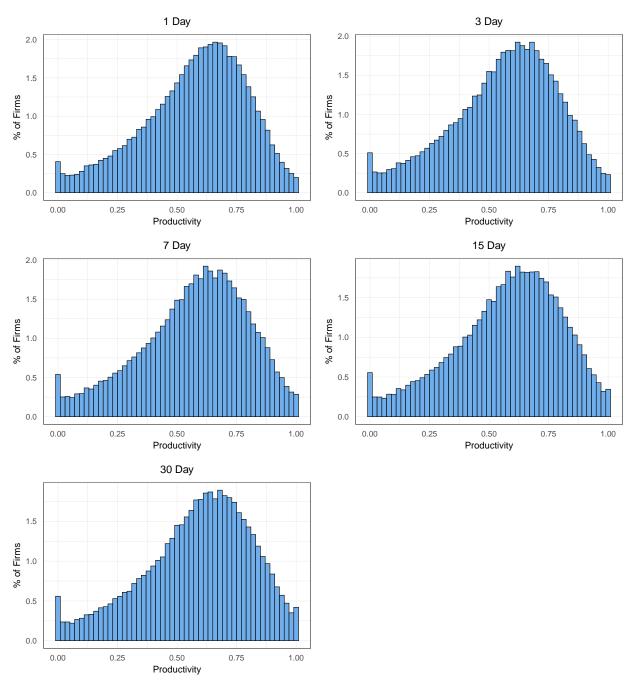
No Controls Day, Holiday 2.0 1.5 % of Firms % of Firms 1.0 1.0 0.5 0.5 0.0 0.0 0.00 0.00 Productivity Productivity Day, Holiday, Product Day, Holiday, Machine Characteristics 2.0 2.0 % of Firms % of Firms 1.0 1.0 0.5 0.5 0.0 0.0 0.0 1.0 0.0 0.8 0.5 0.4 Productivity Productivity Day, Region, Machine Characteristics 2.0

Figure OA-10: Productivity Distribution Under Different Controls

*Notes*: This figure presents the distribution of firm-level productivity estimates using productivity measures that control for different machine characteristics, as detailed in Section E.3. The histograms show the dispersion in productivity under various control specifications, including the day of the week, holiday, product ID, and machine family.

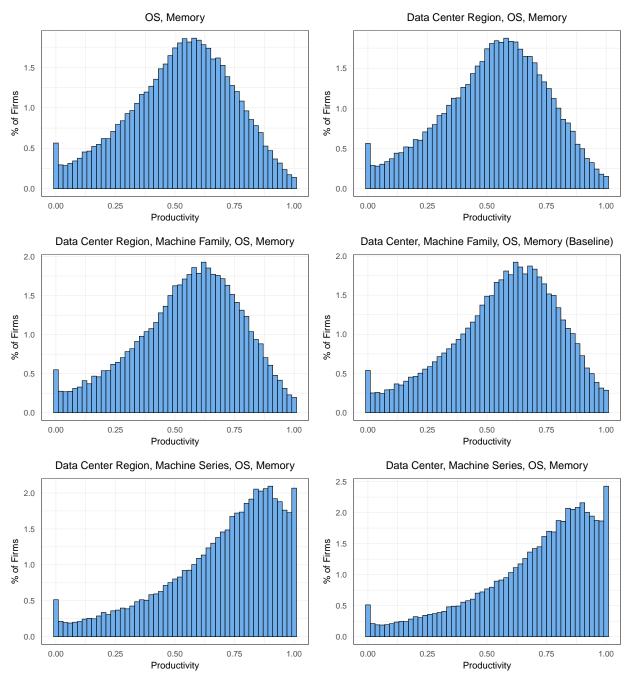
0.8

Figure OA-11: Productivity Distribution Under Different Peak Utilization Durations



*Notes*: This figure presents the distribution of firm-level productivity estimates using productivity measures that control for different days of measurement of peak utilization as detailed in Appendix E.2.

Figure OA-12: Productivity Distribution Under Different Downsizability Definitions



*Notes*: This figure presents the distribution of firm-level productivity estimates using productivity measures that use different downsizability definitions as detailed in Appendix E.5.

**Table OA-6:** Productivity Dispersion and Persistence Under Different Controls

	No Controls	Day Holiday	Day, Holiday, Product	Day, Holiday, Machine Char.	Day, Region, Machine Char
	(1)	(2)	(3)	(4)	(5)
			Panel A. Dispersio	on	
Dispersion:					
Mean	0.60	0.60	0.58	0.59	0.59
Median	0.62	0.62	0.60	0.61	0.62
10-90th perc ratio	3.51	3.51	3.08	3.41	3.39
Interquartile Range	1.72	1.72	1.65	1.71	1.70
Within-Firm:					
Within-firm	33.08	33.10	30.00	33.12	33.10
Between-firm, within-industry	66.92	66.90	70.00	66.88	66.90
Within-Firm-Between-Region:					
Within-region	5.88	5.89	5.70	5.82	5.89
Between-region, within-industry	94.12	94.11	94.30	94.18	94.11
		Panel B. P	Persistence (AR(1)	Coefficients)	
1-month persistence:					
Productivity	0.93	0.93	0.92	0.93	0.93
•	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
Idleness	0.93	0.93	0.92	0.93	0.93
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
Overprovisioning	0.91	0.91	0.90	0.91	0.91
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
1-year persistence:					
Productivity	0.64	0.64	0.59	0.64	0.64
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
Idleness	0.66	0.66	0.61	0.66	0.66
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
Overprovisioning	0.60	0.60	0.55	0.58	0.58
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
5-year persistence:					
Productivity	0.32	0.32	0.26	0.34	0.34
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
Idleness	0.33	0.33	0.24	0.33	0.33
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
Overprovisioning	0.10	0.10	0.14	0.12	0.12
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)

*Notes*: This table reports the dispersion and persistence of productivity measures across different specifications that differ by the control variables included in Equation (16). Panel A presents the dispersion of compute productivity. Panel B shows the persistence of productivity, idleness, and overprovisioning measures with 1-month, 3-month, and 5-month autoregressive (AR(1)) coefficients, including their standard errors in parentheses. The control variables in each column are (2) day-of-week and holiday fixed effects, (3) day-of-week, holiday, and product ID fixed effects, (4) day-of-week, holiday, and machine family fixed effects, (5) day-of-week, holiday, data center region, and machine family fixed effects.

**Table OA-7:** Productivity Dispersion and Persistence Under Different Peak Utilization Durations

	1 Day (1)	3 Days (2)	7 Days (3)	15 Days (4)	30 Days (5)			
	Panel A. Dispersion							
Dispersion:								
Mean	0.60	0.59	0.60	0.60	0.61			
Median	0.62	0.61	0.62	0.62	0.63			
10-90th perc ratio	3.23	3.47	3.51	3.48	3.42			
Interquartile Range	1.68	1.72	1.72	1.71	1.69			
Within-Firm:								
Within-firm	33.46	33.08	33.08	32.96	32.93			
Between-firm, within-industry	66.54	66.92	66.92	67.04	67.07			
Within-Firm-Between-Region:								
Within-region	5.98	5.90	5.88	5.84	5.79			
Between-region, within-industry	94.02	94.10	94.12	94.16	94.21			
	Panel B. Persistence (AR(1) Coefficients)							
1-month persistence:								
Productivity	0.94	0.94	0.93	0.93	0.94			
Troductivity	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)			
Idleness	0.94	0.94	0.93	0.93	0.94			
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)			
Overprovisioning	0.91	0.92	0.91	0.91	0.92			
•	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)			
1-year persistence:								
Productivity	0.66	0.65	0.64	0.64	0.64			
•	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)			
Idleness	0.68	0.67	0.66	0.65	0.65			
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)			
Overprovisioning	0.61	0.62	0.60	0.59	0.58			
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)			
5-year persistence:								
Productivity	0.32	0.32	0.32	0.31	0.31			
-	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)			
Idleness	0.34	0.34	0.33	0.33	0.32			
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)			
Overprovisioning	0.10	0.11	0.10	0.10	0.10			
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)			

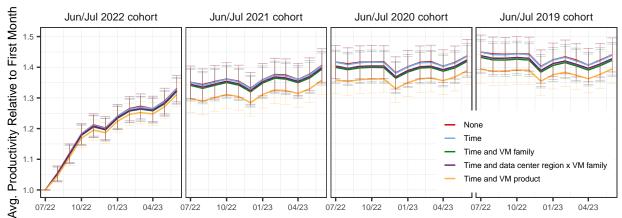
*Notes*: This table reports the dispersion and persistence of productivity using productivity measures that control for different days of measurement of peak utilization as detailed in Appendix E.2. Panel A presents the dispersion of compute productivity across different productivity measures. Panel B shows the persistence of productivity, idleness, and overprovisioning measures with 1-month, 3-month, and 5-month autoregressive (AR(1)) coefficients, including their standard errors in parentheses.

**Table OA-8:** Productivity Dispersion and Persistence Under Different Downsizability Definitions

	OS, mem	Region, OS, mem	Region, family, OS, mem	DC, family, OS, mem	Region, series, OS, mem	DC, series, OS, mem
	(1)	(2)	(3)	(4)	(5)	(6)
			Panel A.	Dispersion		
ispersion:						
Mean	0.55	0.56	0.58	0.60	0.71	0.72
Median	0.56	0.57	0.60	0.62	0.77	0.78
10-90th perc ratio	3.76	3.70	3.56	3.51	3.06	3.01
Inter Quartile Range	1.82	1.81	1.75	1.72	1.64	1.63
lithin-Firm:						
Within-firm	33.87	33.98	33.31	33.08	32.34	32.23
Between-firm, within-industry	66.13	66.02	66.69	66.92	67.66	67.77
lithin-Firm-Between-Region:						
Within-region	5.76	5.76	5.71	5.88	5.42	5.45
Between-region, within-industry	94.24	94.24	94.29	94.12	94.58	94.55
		Pan	el B. Persistence	(AR(1) Coeffici	ients)	
month persistence:						
Productivity	0.93	0.93	0.93	0.93	0.93	0.93
•	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
Idleness	0.93	0.93	0.93	0.93	0.93	0.93
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
Overprovisioning	0.90 (0.00)	0.90 (0.00)	0.91 (0.00)	0.91 (0.00)	0.93 (0.00)	0.93 (0.00)
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
year persistence:						
Productivity	0.65	0.65	0.65	0.64	0.64	0.65
Idleness	(0.00) 0.66	(0.00) 0.66	(0.00) 0.66	(0.00) 0.66	(0.00) 0.66	(0.00) 0.66
Tuteriess	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
Overprovisioning	0.60	0.61	0.61	0.60	0.58	0.58
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
year persistence:		, ,	, ,	, ,	` ,	. ,
Productivity	0.32	0.32	0.32	0.32	0.32	0.32
	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)	(0.00)
Idleness	0.33	0.33	0.33	0.33	0.33	0.33
						(0.00)
Overprovisioning						0.19 (0.00)
Overprovisioning	(0.00) 0.11 (0.00)	(0.00) 0.10 (0.00)	(0.00) 0.09 (0.00)	(0.00) 0.10 (0.00)	(0.00) 0.16 (0.00)	

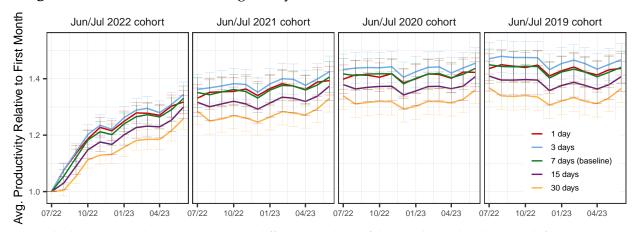
Notes: This table reports the dispersion and persistence of productivity measures under different downsizability definitions given in Appendix E.5. Panel A presents the dispersion of compute productivity across different productivity measures. Panel B shows the persistence of productivity, idleness, and overprovisioning measures with 1-month, 3-month, and 5-month autoregressive (AR(1)) coefficients, including their standard errors in parentheses. The columns represent different downsizability definitions: (1) "OS, mem" for OS and memory; (2) "Region, OS, mem" for data center region, OS, and memory; (3) "Region, family, OS, mem" for data center region, machine family, OS, and memory; (4) "DC, family, OS, mem" for data center, machine family, OS, and memory; and (6) "DC, series, OS, mem" for data center, machine series, OS, and memory.

Figure OA-13: Cohort Learning Analysis Under Different Controls



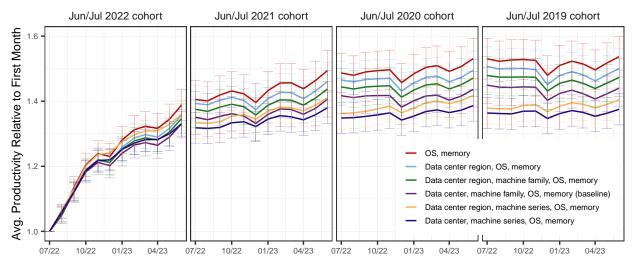
*Notes*: This figure shows the learning results on Figure 7 using different control variables in the productivity estimation.

Figure OA-14: Cohort Learning Analysis Under Different Peak Utilization Durations



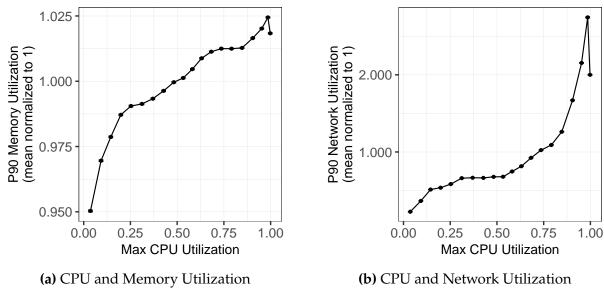
Notes: The learning results in Figure 7 using different numbers of days in the peak utilization definition.

Figure OA-15: Cohort Learning Analysis Under Different Downsizability Definitions



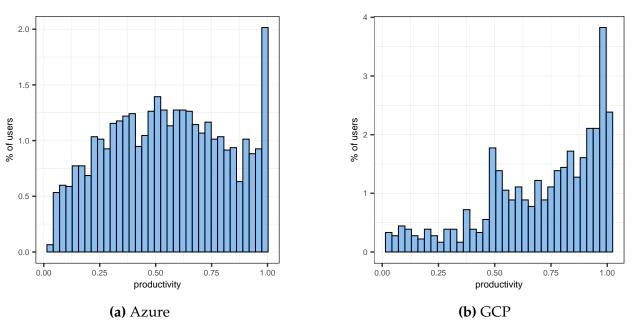
Notes: This figure shows the learning analysis of Figure 7 using different downsizability definitions.

Figure OA-16: Correlation of CPU Utilization with Memory and Network Utilization



*Notes*: This figure illustrates the correlation between max CPU utilization and other resource measures. For each figure, we divide VM-days into twenty equally sized bins based on max CPU utilization, then plot the average max CPU utilization of VMs in that bin against the max memory utilization and 90th percentile network utilization of VMs in that bin. The average max memory and the average 90th percentile network across all bins are normalized to 1.

Figure OA-17: Productivity Distribution in Publicly Available CPU Utilization Data



*Notes*: These figures illustrate the distribution of user-level compute productivity, estimated using the entire sample, weighting each VM by core-hours as shown in equations (26) and (27) for Azure and GCP, respectively. The x-axis represents productivity levels ranging from 0 to 1, while the y-axis shows the percentage of firms. Each observation corresponds to a user, and the histogram bars reflect the unweighted distribution of users across different productivity intervals.

# **References for Online Appendix**

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